

Cusp-core problem

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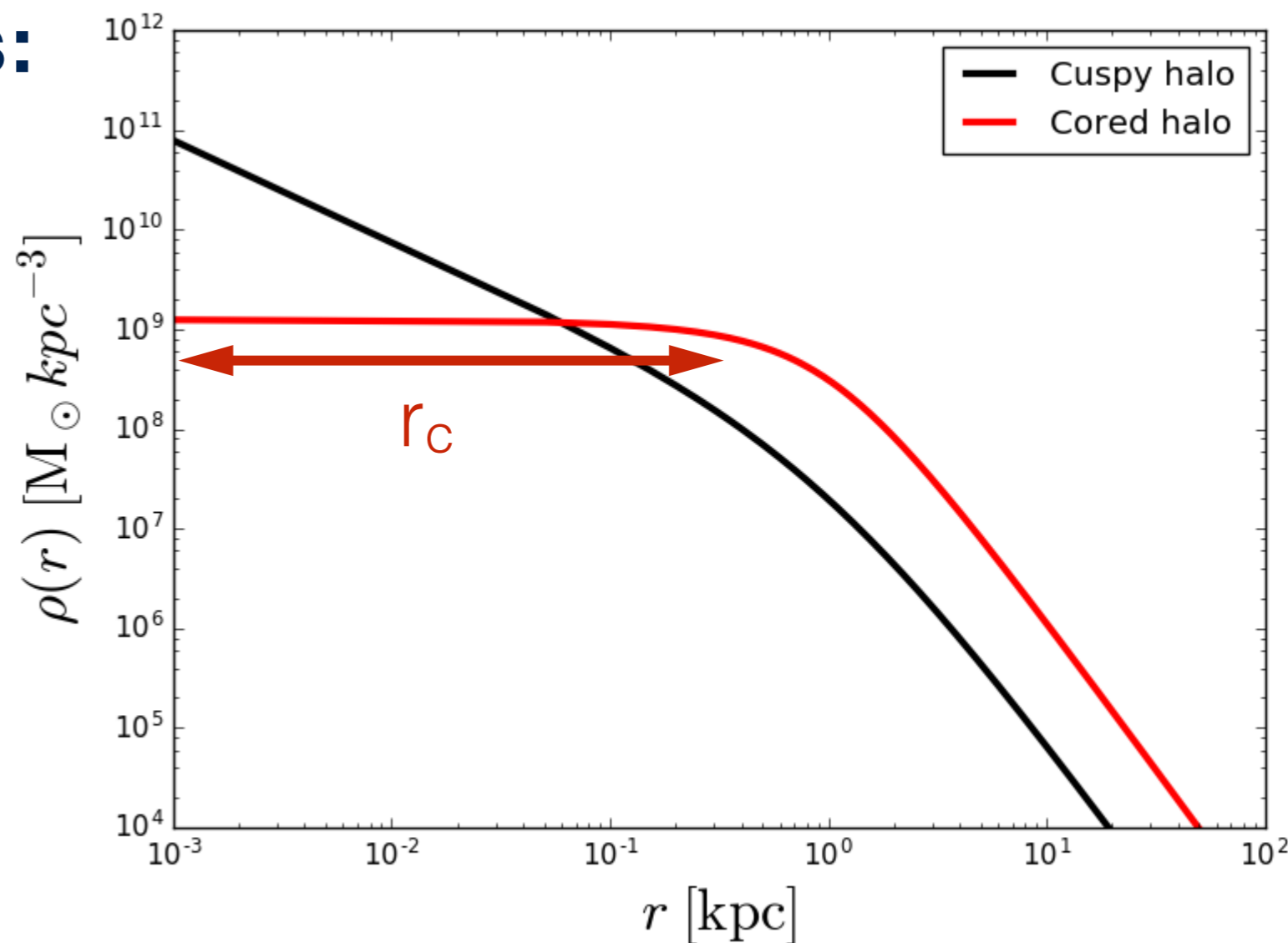
Nature of dark matter

- **Cold Dark Matter**
- **Warm Dark Matter**
- **Fuzzy Dark Matter**
(Hu et al. 2000, Hui et al. 2016)
- **Self-Interacting Dark Matter**
(Spergel & Steinhardt 2000)

Cusp-core problem

Astrophysical constraints:

- **Large-scale constraints**
e.g. CMB
- **Small-scale constraints**
e.g. Number of satellite galaxies,
Dark matter density profile

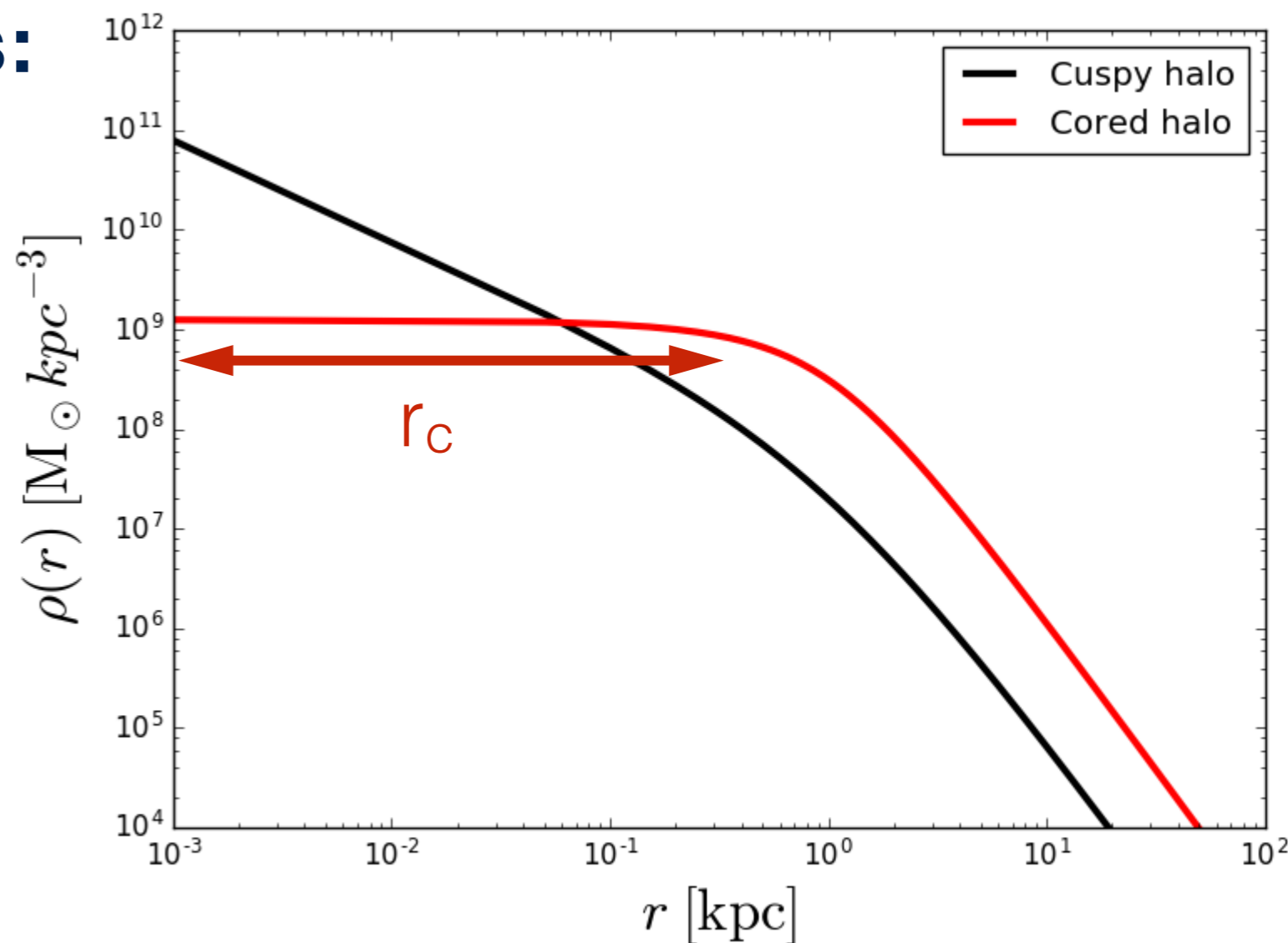


Cusp or core?

Cusp-core problem

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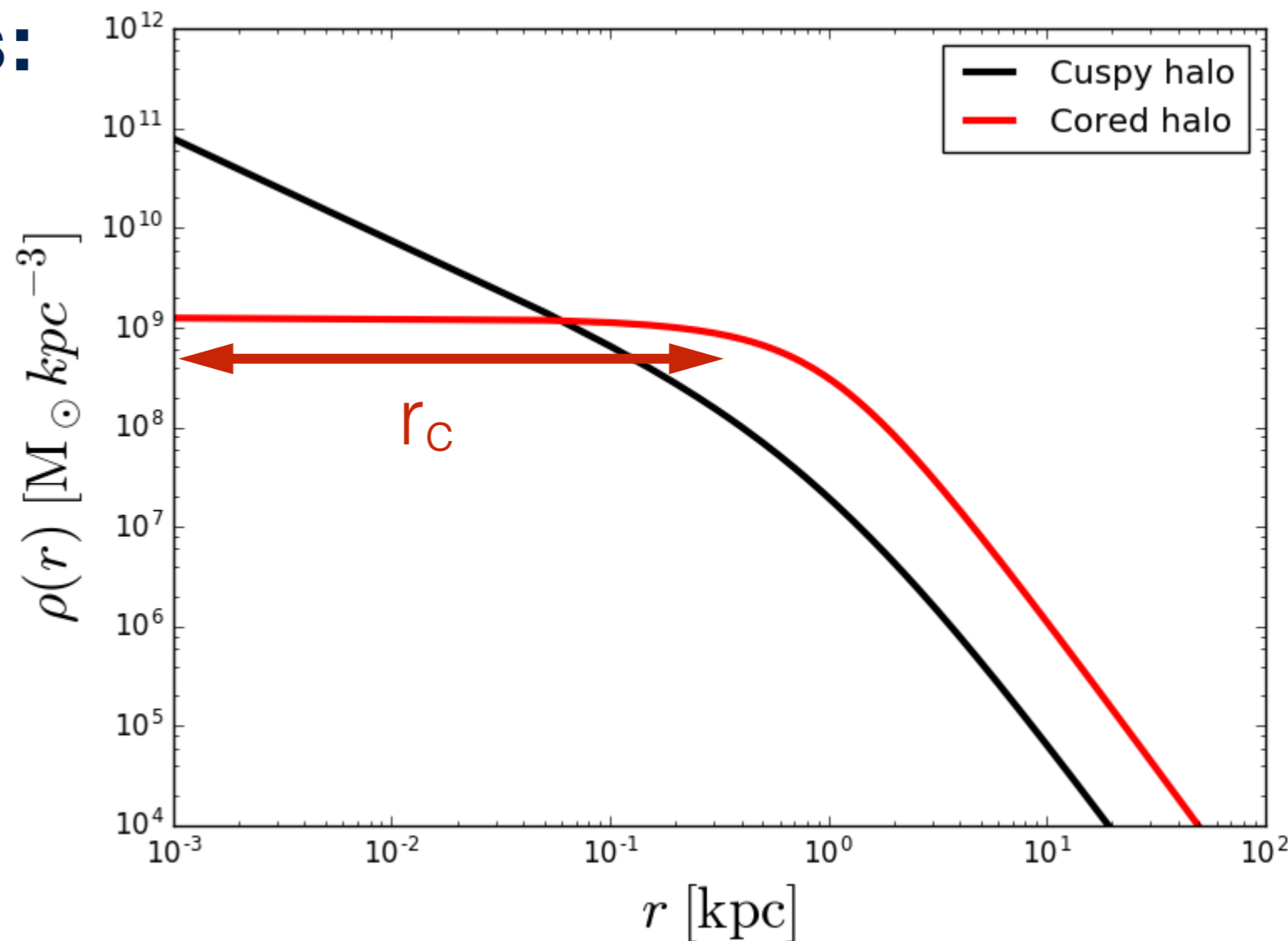


Cusp or core?

Cusp-core problem

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- **Large-scale constraints**
e.g. CMB
- **Small-scale constraints**
e.g. Number of satellite galaxies,
Dark matter density profile



Cusp or core?



Nature of dark matter: cusp or core

- **Cold Dark Matter** **Cusp**
- **Warm Dark Matter** **Core**
(Colin et al. 2000; Bode et al. 2001)
- **Fuzzy Dark Matter** **Core**
(Hu et al. 2000; Hui et al. 2017)
- **Self-Interacting Dark Matter** **Core**
(Vogelsberger et al. 2012)

Projets de thèse

5 projets:

1 achevé,
2 en cours,
2 nouveaux

M31



Fornax



Sextans



Eridanus II



Projets de thèse

5 projets:

- 1 CPU N-body,
- 3 GPU N-body
- 1 HST data analysis

M31



Fornax



Sextans



Eridanus II



Projets de thèse

5 projets:

2 IAP,
1 IAP-LERMA,
1 IAP-ITC Tokyo,
1 IAP-LERMA-ROE

M31



Fornax



Sextans



Eridanus II



Projets de thèse

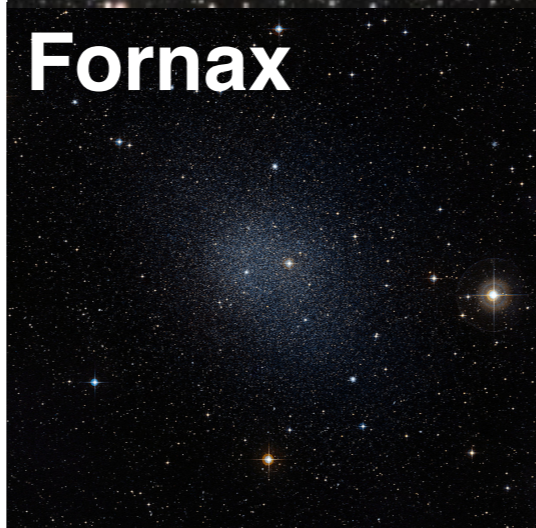
5 projets:

- P1. Fornax: cusp or core?
- P2. Primordial black holes
- P3. Remnant galaxy in M31
- P4. Subhalos of GCs
- P5. Star cluster relics

M31



Fornax



Sextans



Eridanus II



Projets de thèse

5 projets:

- **P1. Fornax: cusp or core?**
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M31



Fornax



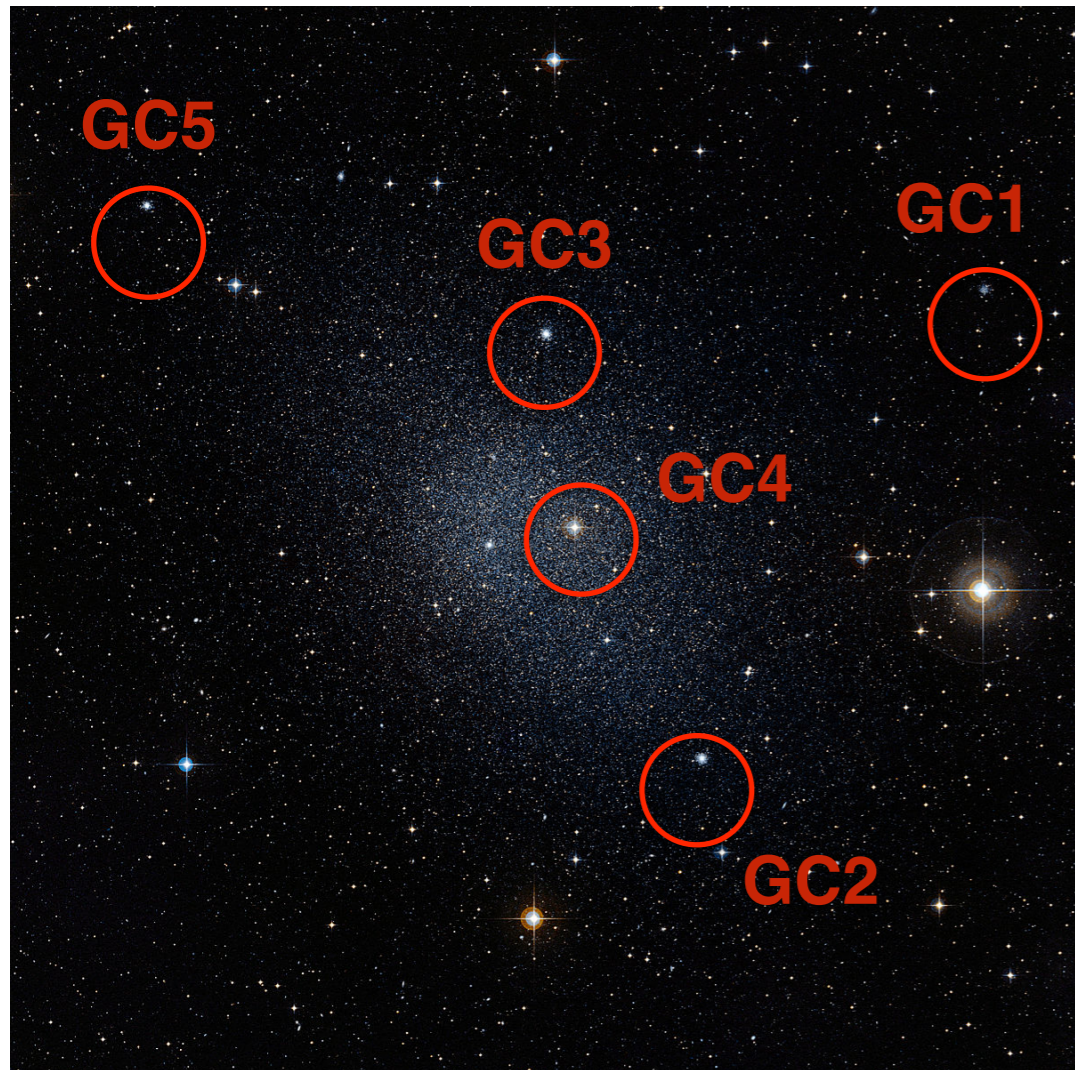
Sextans



Eridanus II



P1. Fornax: cusp or core?

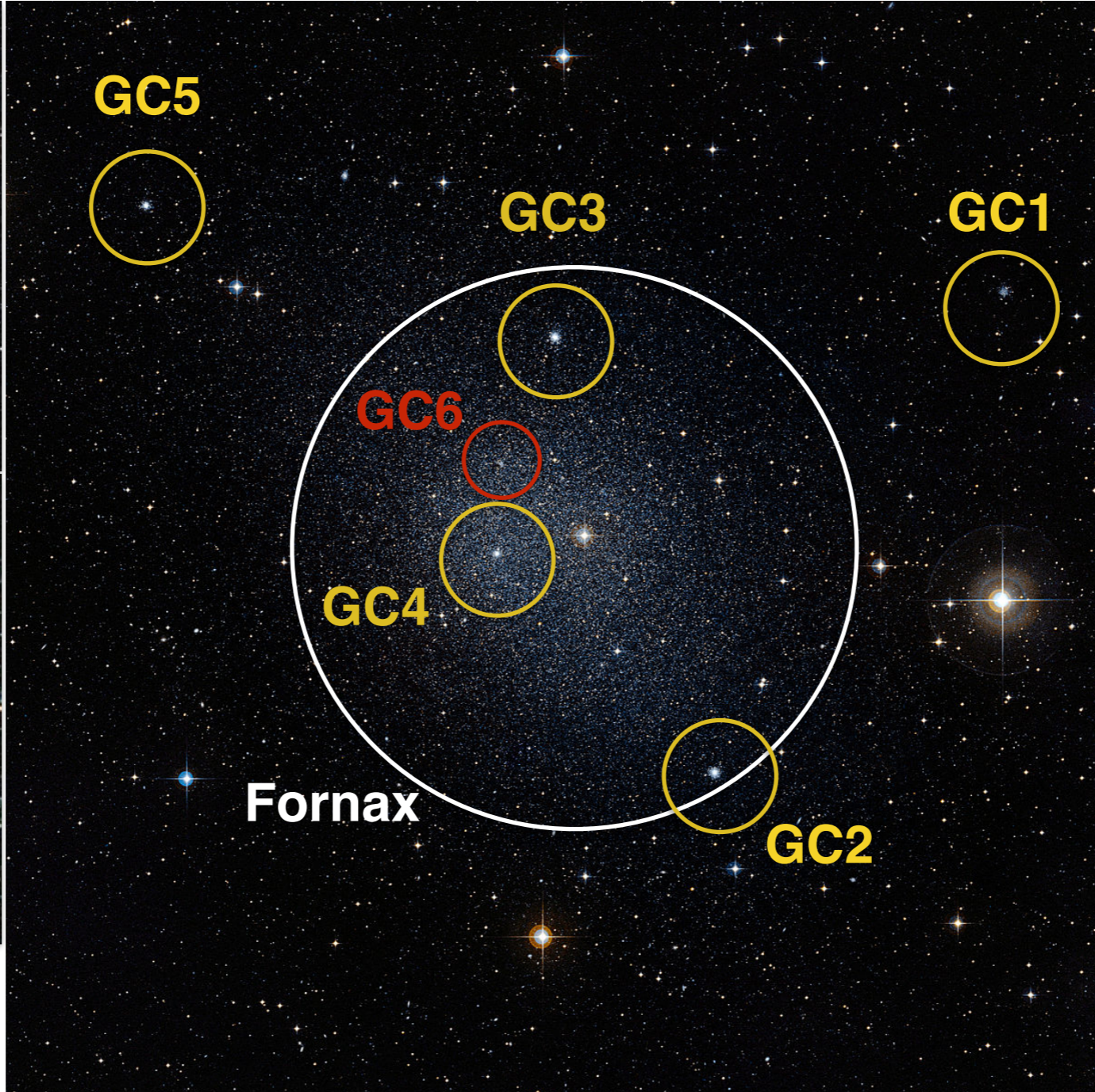


Credit: ESO/Digitized Sky Survey 2

| Object | M^a [$10^5 M_\odot$] | r_c^b [pc] | $r_t^{d,e}$ [pc] | D_p^b [kpc] | D_{MW}^a [kpc] |
|--------|-----------------------------|------------------|---------------------|------------------|---------------------|
| Fornax | 382 ± 12 | 668 ± 34^c | - | - | 147 ± 4 |
| GC1 | 0.42 ± 0.10 | 10.03 ± 0.29 | 59.06 ± 1.70 | 1.6 | 147.2 ± 4.1 |
| GC2 | 1.54 ± 0.28 | 5.81 ± 0.19 | 108.19 ± 3.54 | 1.05 | 143.2 ± 3.3 |
| GC3 | 4.98 ± 0.84 | 1.60 ± 0.07 | 108.17 ± 4.73 | 0.43 | 141.9 ± 3.9 |
| GC4 | 0.76 ± 0.15 | 1.75 ± 0.18 | 115.62 ± 11.89 | 0.24 | 140.6 ± 3.2 |
| GC5 | 1.86 ± 0.24 | 1.38 ± 0.11 | 25.69 ± 2.05 | 1.43 | 144.5 ± 3.3 |

Globular cluster data:
positions, masses

Cusp or core?



P1. Fornax: cusp or core?

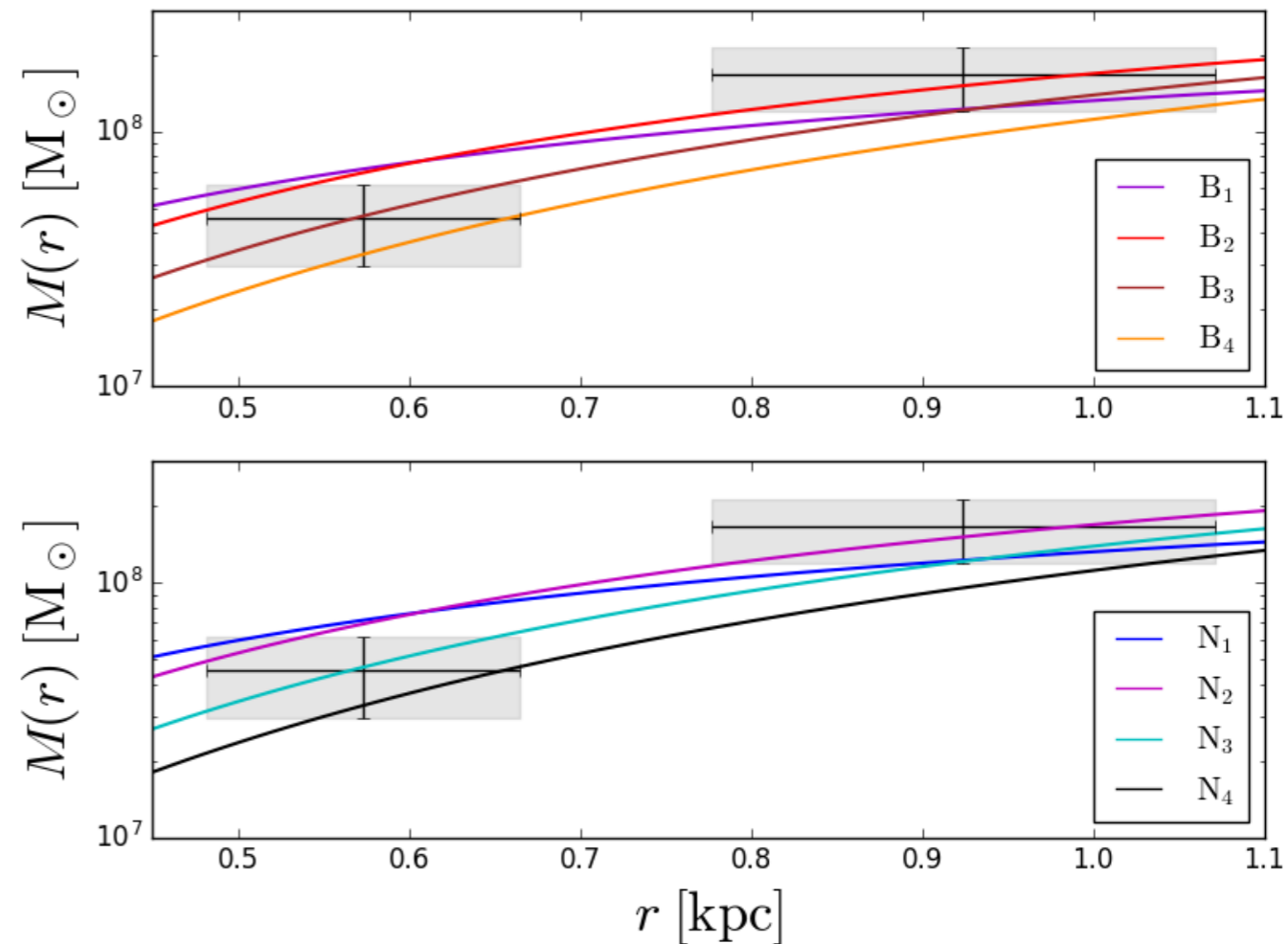
Live simulations:

Halo + stars $\sim 6 \times 10^6$

5 GCs $\sim 10^3 - 10^4$

MW static potential

| Model | Density profile | r_s [kpc] | M_h [M_\odot] | r_t [kpc] | m_p [M_\odot] |
|-------|-----------------|----------------|------------------------|----------------|------------------------|
| B_1 | Burkert | 0.25 | 0.318×10^9 | 2.81 | 89 |
| B_2 | Burkert | 0.5 | 0.88×10^9 | 3.95 | 230 |
| B_3 | Burkert | 0.75 | 1.1×10^9 | 4.52 | 285 |
| B_4 | Burkert | 1 | 1.28×10^9 | 4.98 | 329 |
| N_1 | NFW | 0.5 | 0.6×10^9 | 3.87 | 160 |
| N_2 | NFW | 1.0 | 1.2×10^9 | 4.87 | 310 |
| N_3 | NFW | 1.5 | 1.6×10^9 | 5.25 | 410 |
| N_4 | NFW | 2 | 2.0×10^9 | 5.77 | 510 |



Walker & Penarrubia (2011)

P1. Fornax globular clusters

75 N-body simulations with Gadget2:

- $R_i = [1, 1.5, 2.0, 2.5, 3.0]$ kpc **x 5 initial radii**
- $M_i = [2.5, 5.0, 7.5, 10]$ M_\odot **x 4 masses**
- $e = [0, 0.9]$ **x 2 eccentric parameters**

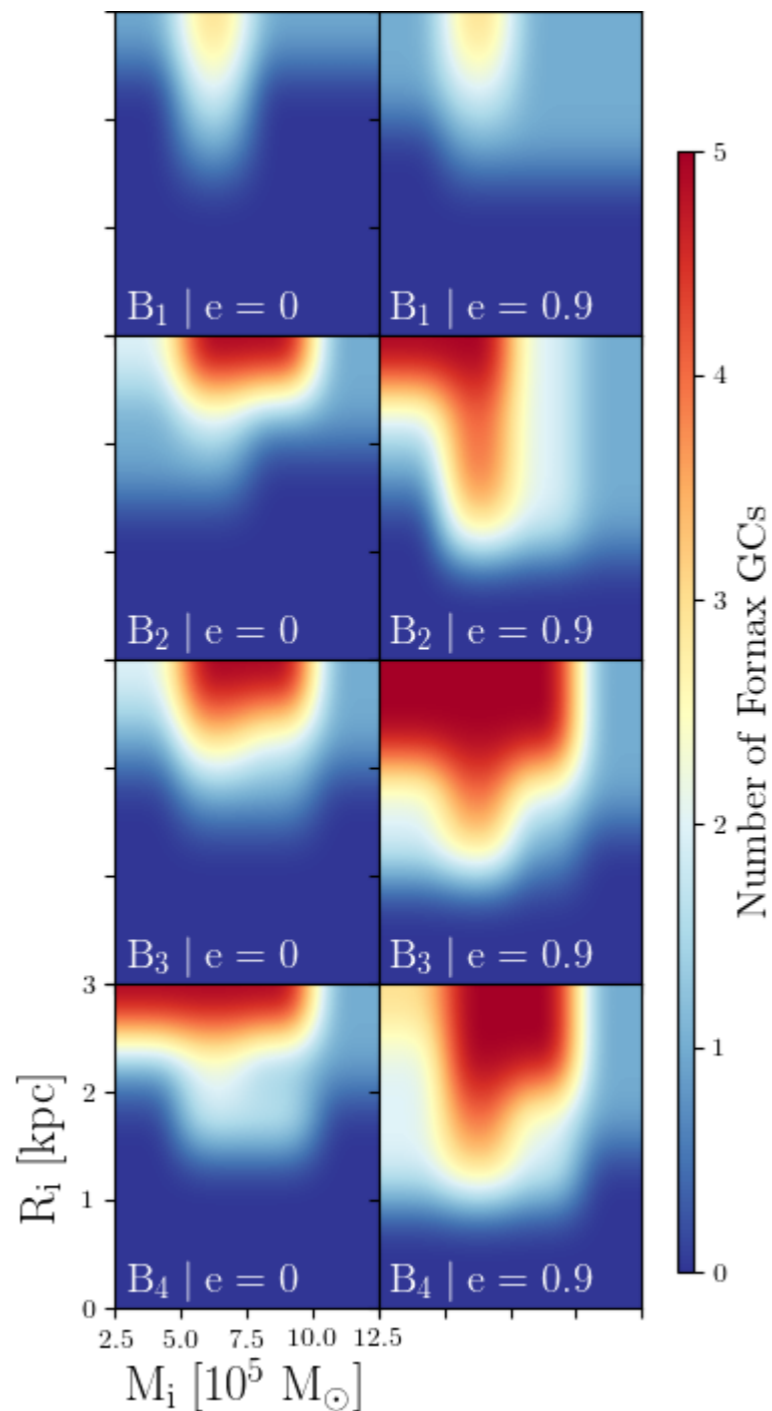
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x 8 models/ 5 GCs

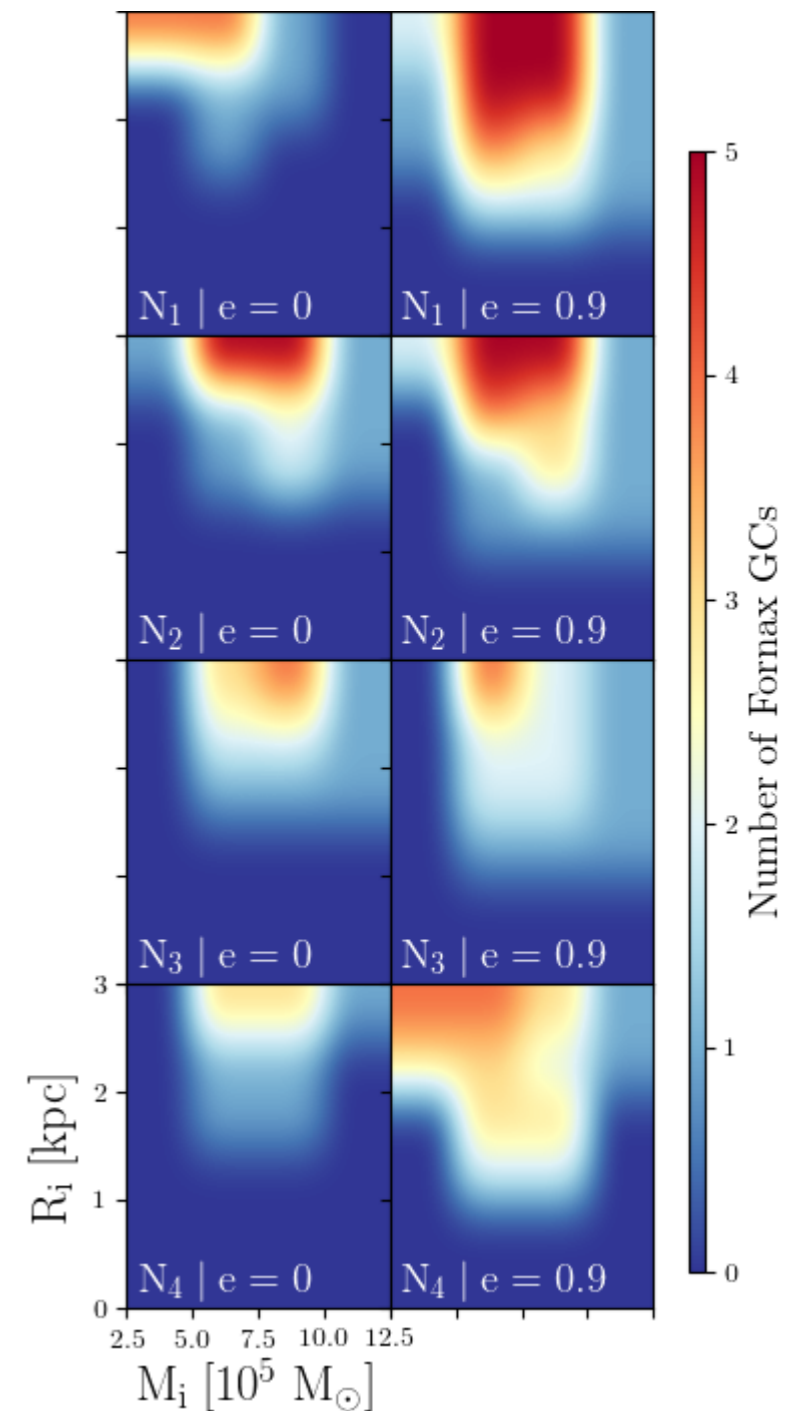
Over 11 Gyr

P1. Fornax: cusp or core?

Cored
halo

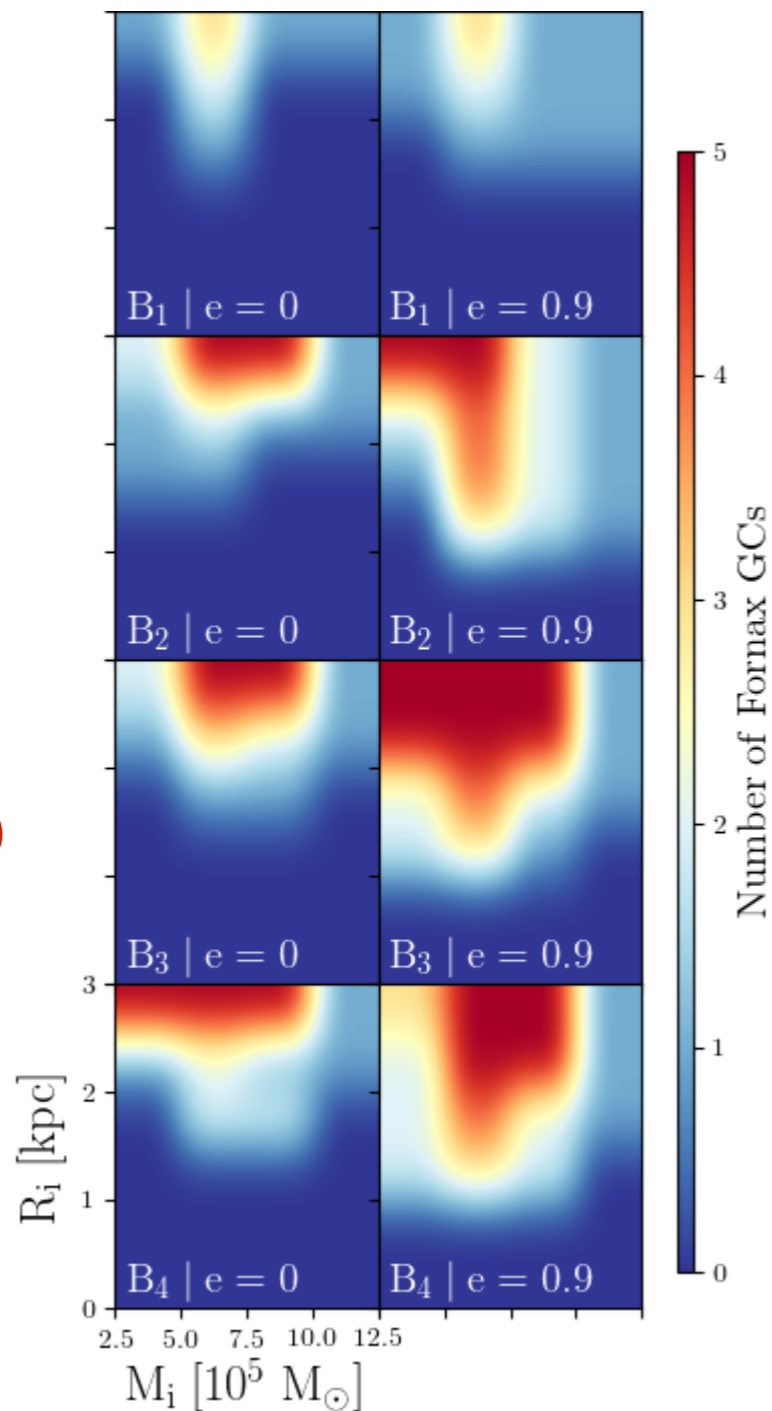


Cuspy
halo



P1. Fornax: cusp or core?

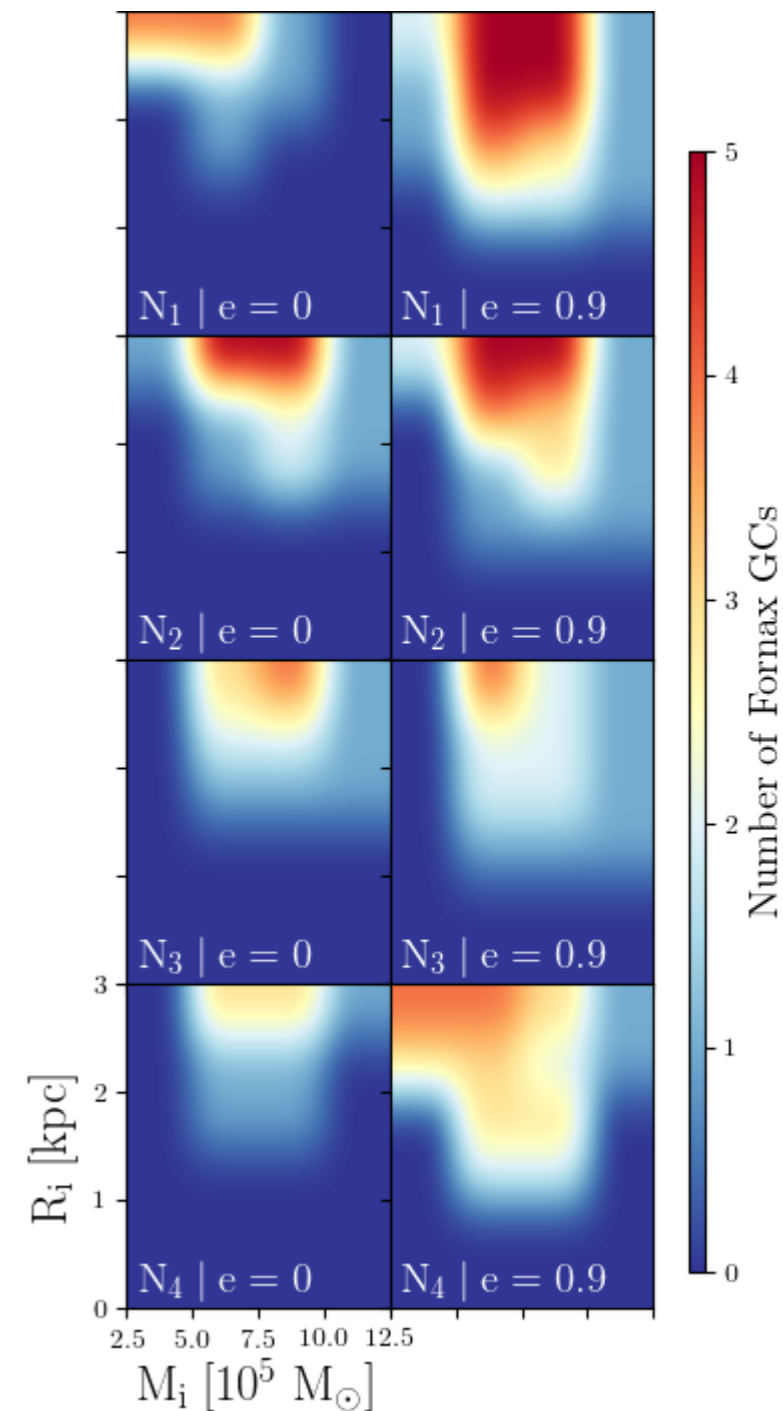
Cored
halo



$r_c \gtrsim 0.5$

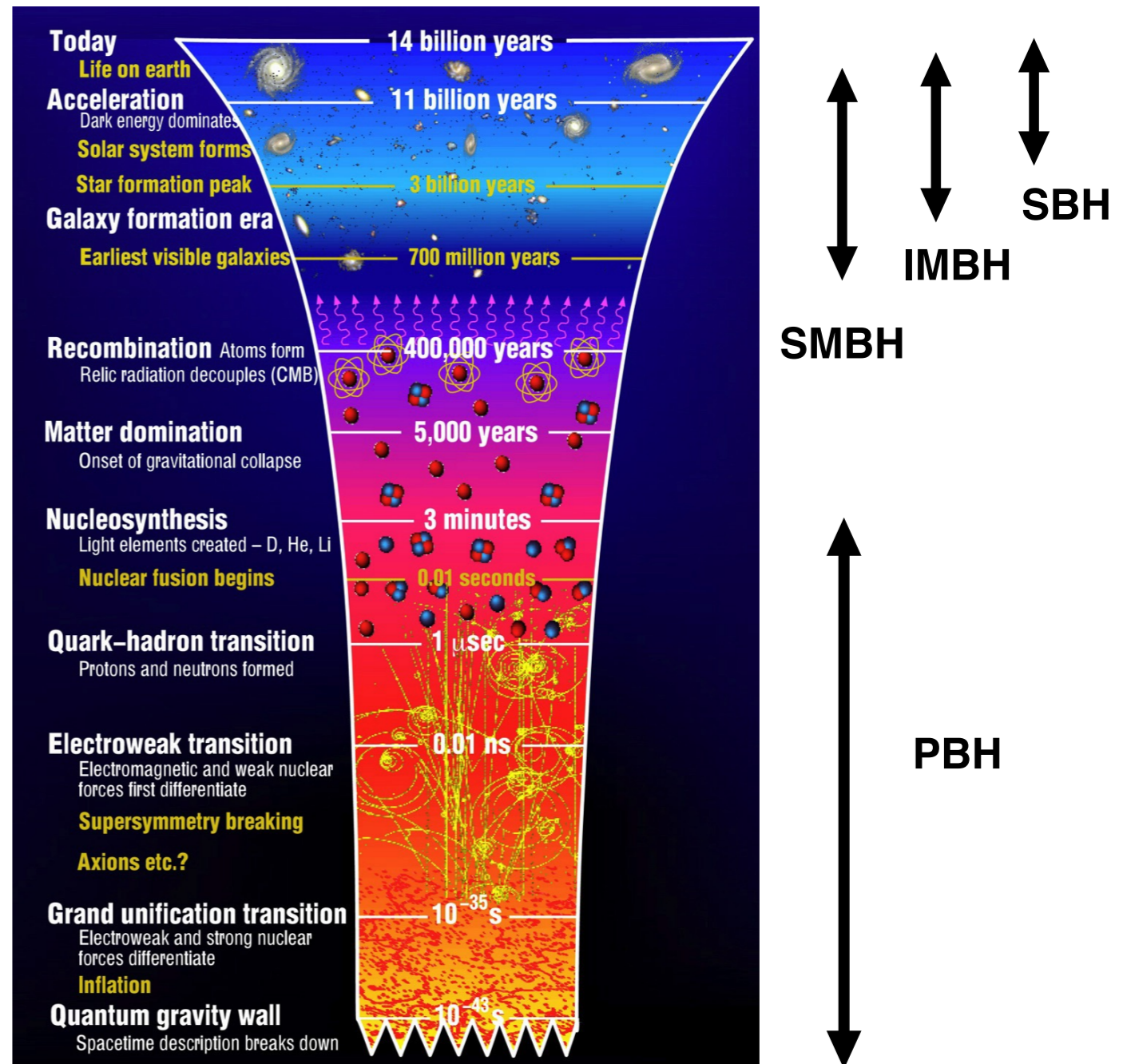
Cuspy
halo

**NFW
profile
not
ruled
out**



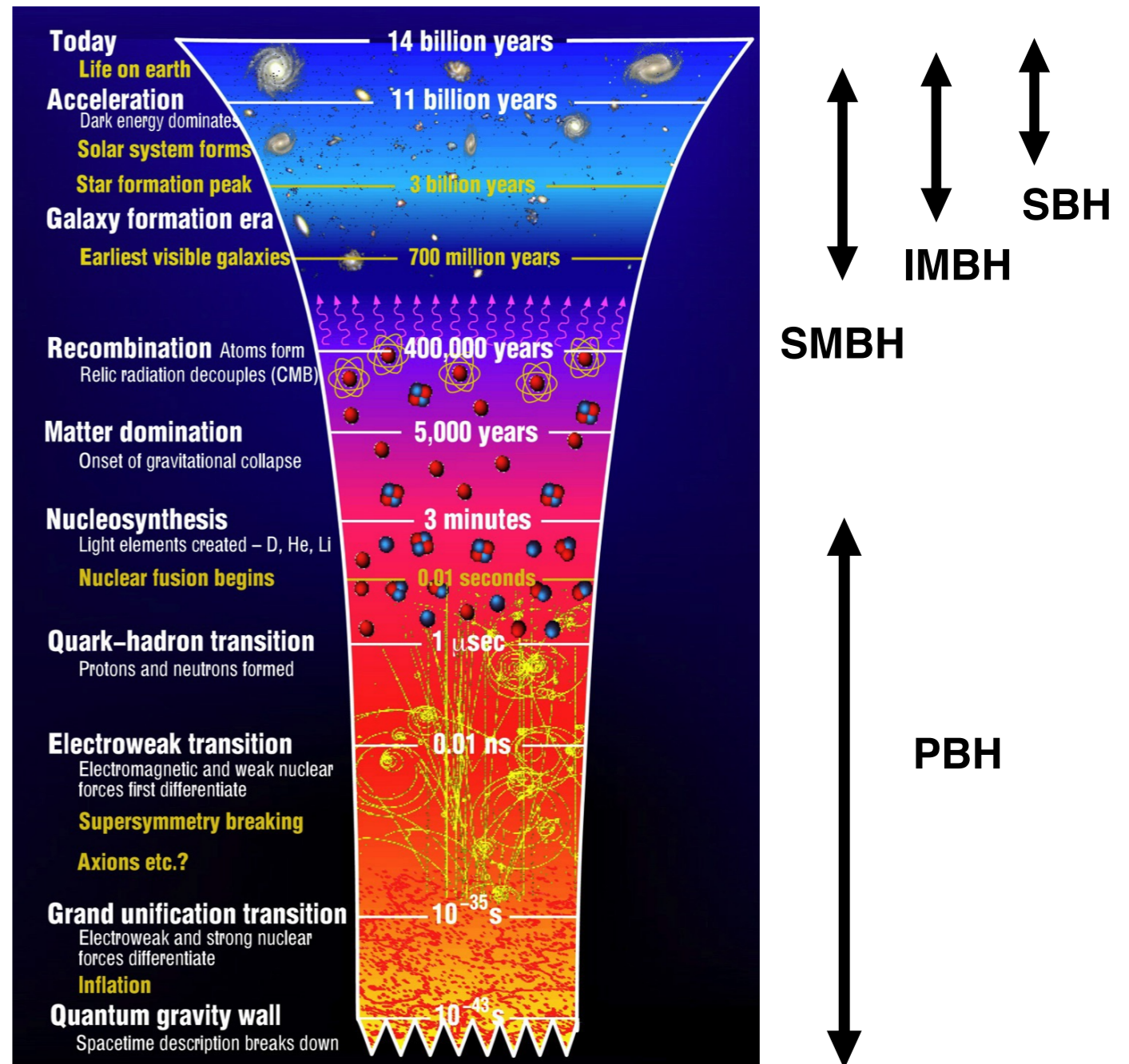
P2. Primordial black holes

- Stellar black hole (SBH)
 $10^1\text{-}10^2 M_{\odot}$
- Intermediate-mass black hole (IMBH)
 $10^3\text{-}10^5 M_{\odot}$
- Supermassive black hole (SMBH)
 $10^6\text{-}10^9 M_{\odot}$
- Primordial black hole (PBH)
 $5 \times 10^{-16} M_{\odot}$, $2 \times 10^{-14} M_{\odot}$ & $25\text{-}100 M_{\odot}$



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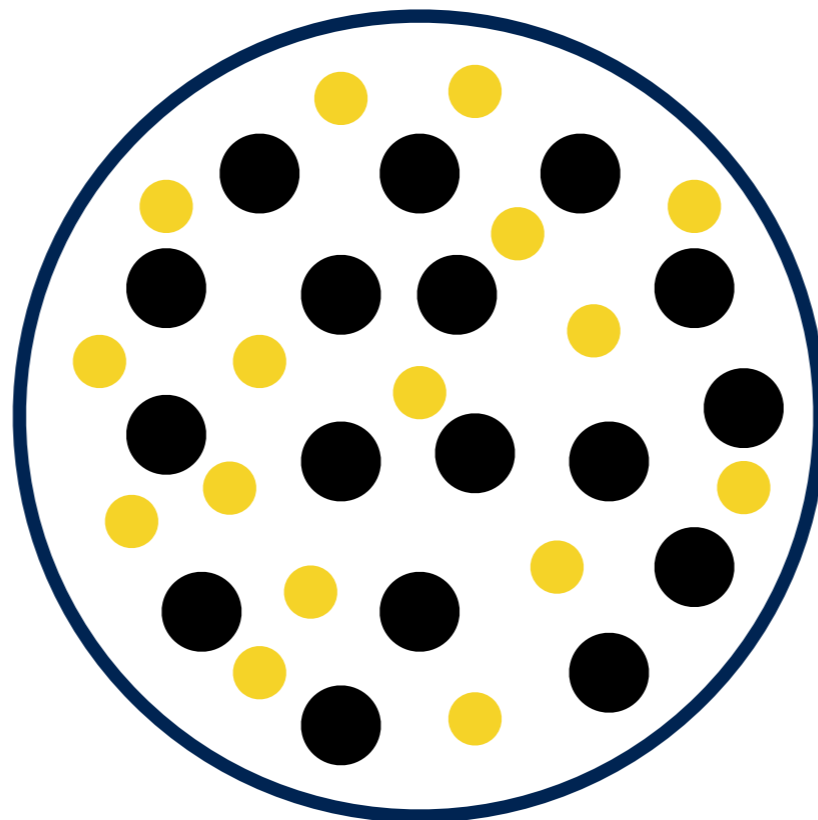


P2. Primordial black holes

DM being composed of PBHs

LIGO detection $\sim 10\text{-}50 M_{\odot}$

Mass window $\sim 25\text{-}100 M_{\odot}$



$$f = M_{\text{PBH}} / M_{\text{DM}}$$

P2. Primordial black holes

Simulations with GOTHIC:

- $f = [1, 0.1, 0.01, 0]$
- $m_{\text{PBH}} = [25, 50, 75, 100] M_{\odot}$ & $m_{\text{DM}} = 1 M_{\odot}$
- $M_{\text{H}} = [10^7, 10^8, 10^9] M_{\odot}$
- $r_s^{\text{PBH}} = [1, 0.5] r_s^{\text{DM}}$

P2. Primordial black holes

Scattering DM by PBHs

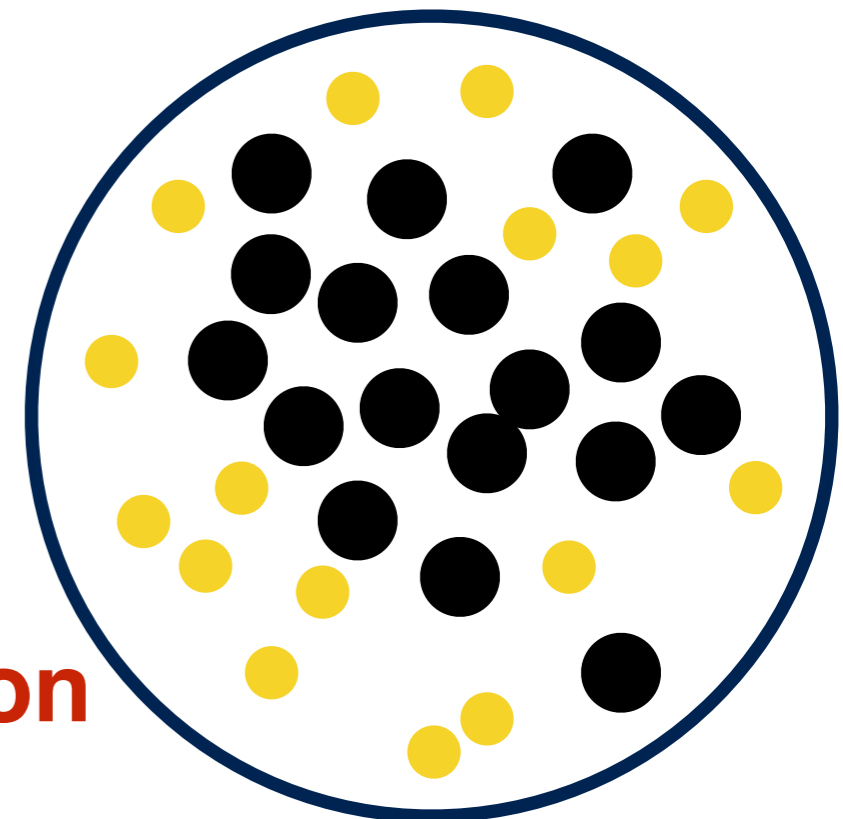
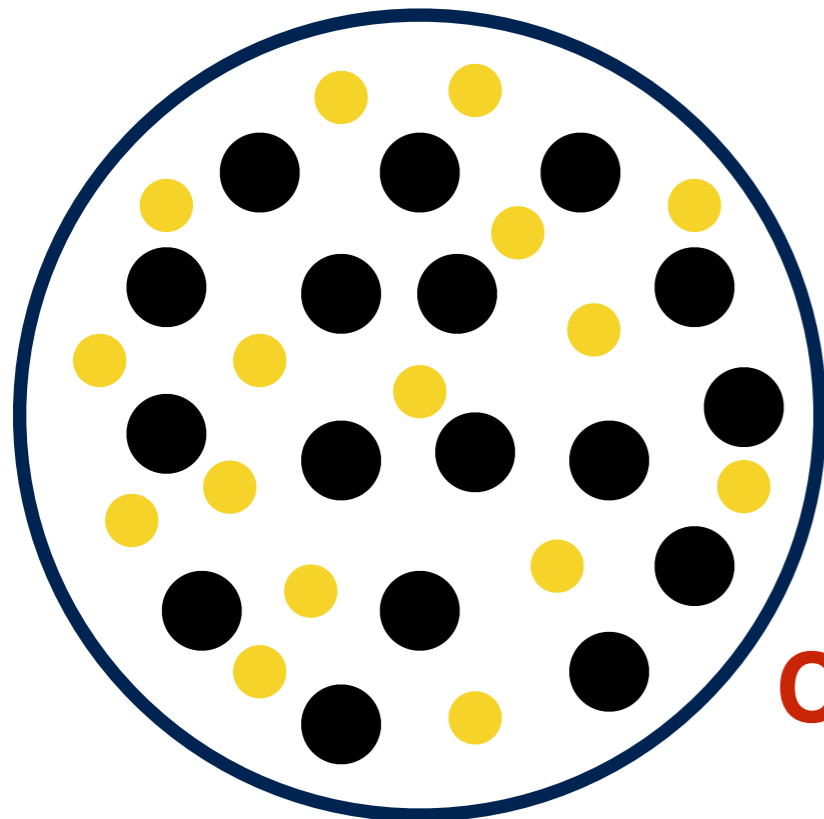


Two-body relaxation

$$f = M_{\text{PBH}} / M_{\text{DM}}$$



Mass segregation



Cusp-to-core transition

P2. Primordial black holes

Relaxation times

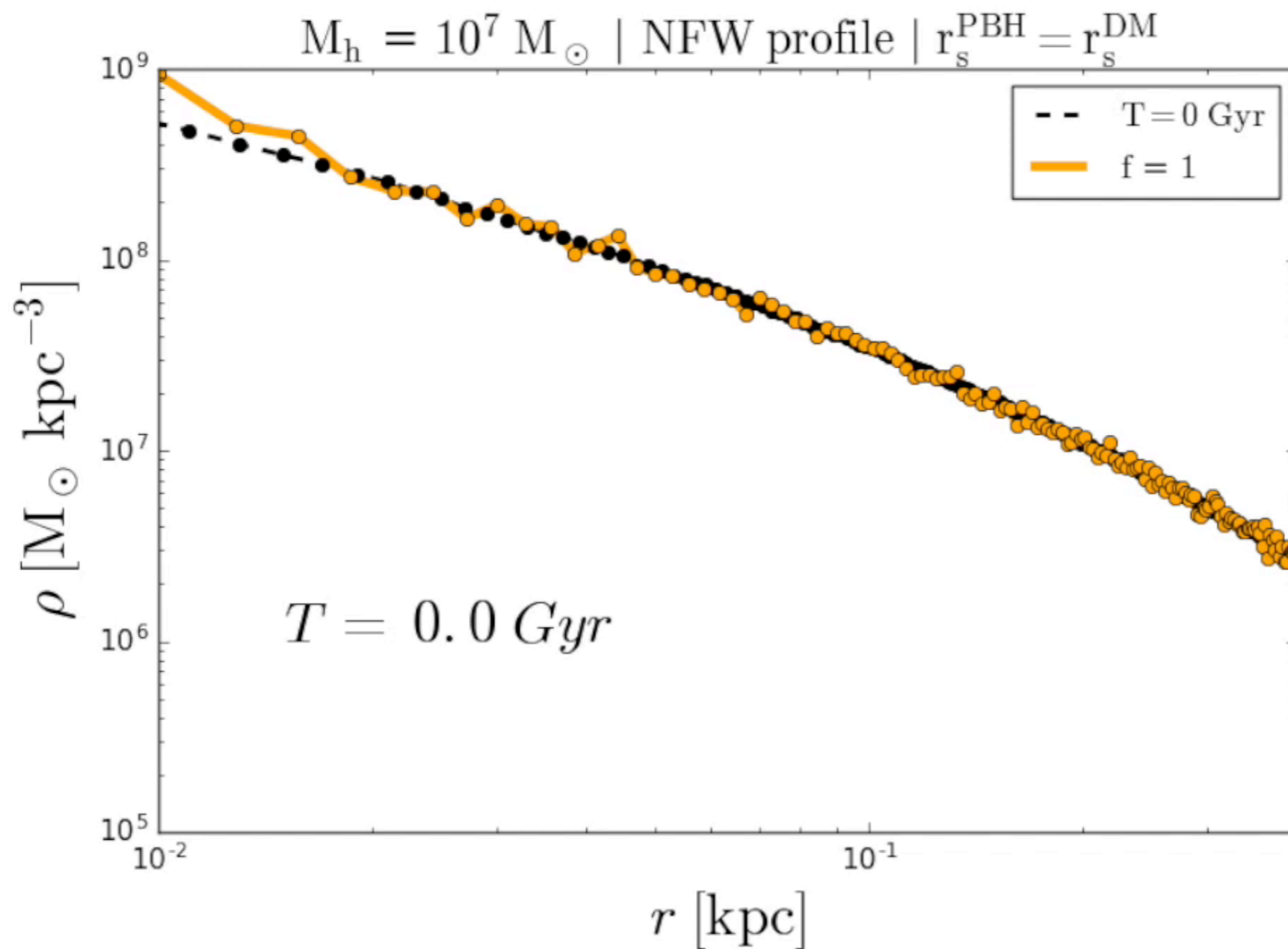
| | $f = 1$ | $f = 0.1$ | $f = 0.01$ | $f = 0$ |
|---------------------------------|---------|-----------|------------|---------|
| $T_R(r = r_s)$ [Gyr] | 14.32 | 85.55 | 344.58 | 1432.33 |
| $T_R(r = 100 \text{ pc})$ [Gyr] | 2.0 | 12 | 48.36 | 201 |
| $T_R(r = 30 \text{ pc})$ [Gyr] | 0.24 | 1.46 | 5.88 | 24.42 |

Table 1. Relaxation times for dark matter ($m_d = 1 M_\odot$) and primordial black holes ($m_p = 100 M_\odot$) for fractions $f = 1, 0.1, 0.01$ and 0 based on the two different formulas

$$T_R \simeq \frac{v^3}{8\pi(n_d m_d^2 + n_p m_p^2)G^2 \ln\left(\frac{b_{max}}{b_{min}}\right)}$$

$$T_R \simeq \frac{v^3}{8\pi n_d m_d^2 G^2 \ln\left(\frac{b_{max}}{b_{min}}\right)}$$

P2. Primordial black holes



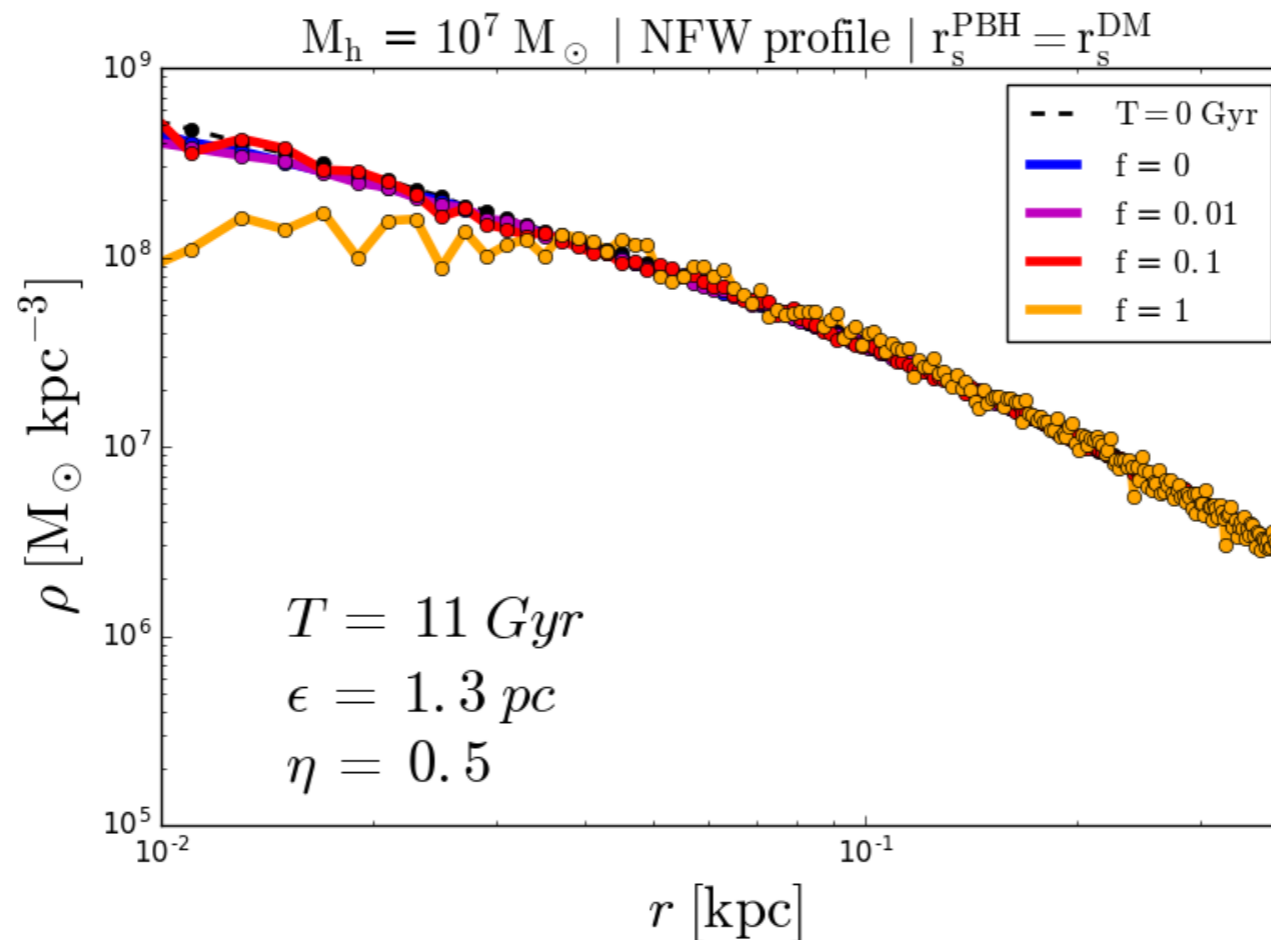
$$m_{\text{PBH}} = 100 M_\odot$$

$$f = M_{\text{PBH}} / M_{\text{DM}}$$

P2. Primordial black holes

| | $f = 1$ | $f = 0.1$ | $f = 0.01$ | $f = 0$ |
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$$m_{\text{PBH}} = 100 M_\odot$$

$$f = M_{\text{PBH}} / M_{\text{DM}}$$

Formations scientifiques

Cours doctoraux (60h):

- Amas de Galaxies et grandes structures de l'Univers, Collège de France (**10h**) 
- Préparation au forum de recrutement PhD Talent Career Fair 2018, IFD (**4h**) 
- Climats extrêmes et analogues actuels : des derniers millénaires à l'optimum holocène, Collège de France (**7h**) 
- Neutrino Astrophysics, IAP (**13h**) 
- Cours d'éthiques (**8h**) 

Winter school (30h):

- KMI School: Dark Matter, Nagoya, Japon (**24h**) 

Presentation:

- ICAP meeting juin 2018 



Publications

Publication (1^{ère} année)

- « ***Fornax globular cluster distributions: implications for the cusp-core problem*** », Boldrini, Mohayaee & Silk (**MNRAS, submitted 2018, submitted revised version 2019**)

Projets de publications (2^{ème} année)

- « ***Primordial black hole as dark matter: cusp-to-core transition*** », Boldrini, Miki, Wagner, Mohayaee & Silk
- « ***Where is the satellite galaxy, which merged with M31 to form the GSS?*** », Boldrini, Valls-Gabaud, Mohayaee & Silk

Projets de publications (3^{ème} année)

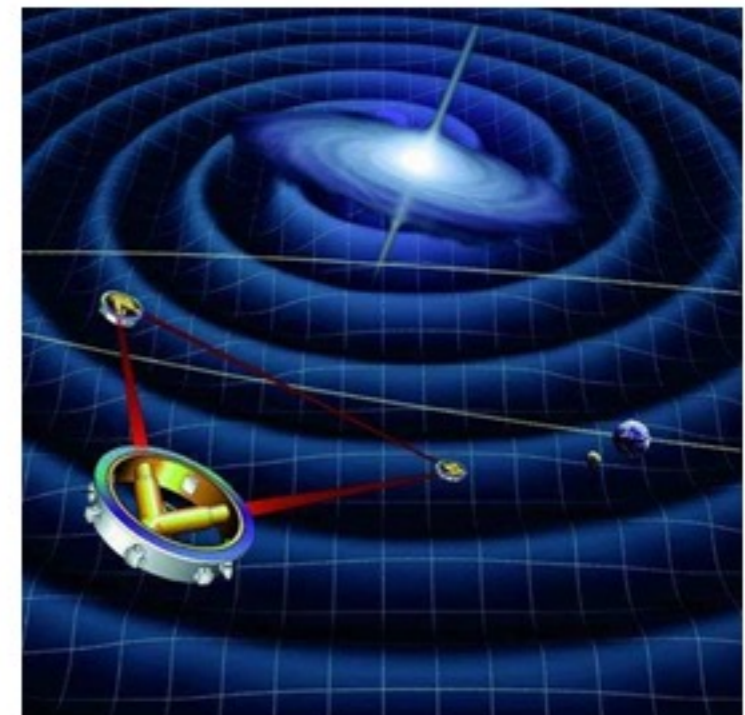
- « ***Star cluster relics: implications for the cusp-core problem*** », Boldrini, Mohayaee & Silk
- « ***Dynamics of MW globular clusters with subhalos*** », Boldrini, Valls-Gabaud, Peñarrubia, Mohayaee & Silk

Collaboration

Full member of the LISA consortium & LISA FRANCE (since 2019)

LISA Work Packages

- Analysis of IMBHs and IMRIs



Questions?

**C'est quoi ton
problème?**

**Cusp or
Core?**

