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## **Dynamical models**

**Model of the Galaxy** and of each of its components (stellar populations, gas, dark matter) through DF-potential pair => fundamental Galactic parameters enter the model  $(V_0, V_{sun}, R_d, ...)$ 

#### **Collsionless Boltzmann Equation for the DF:**

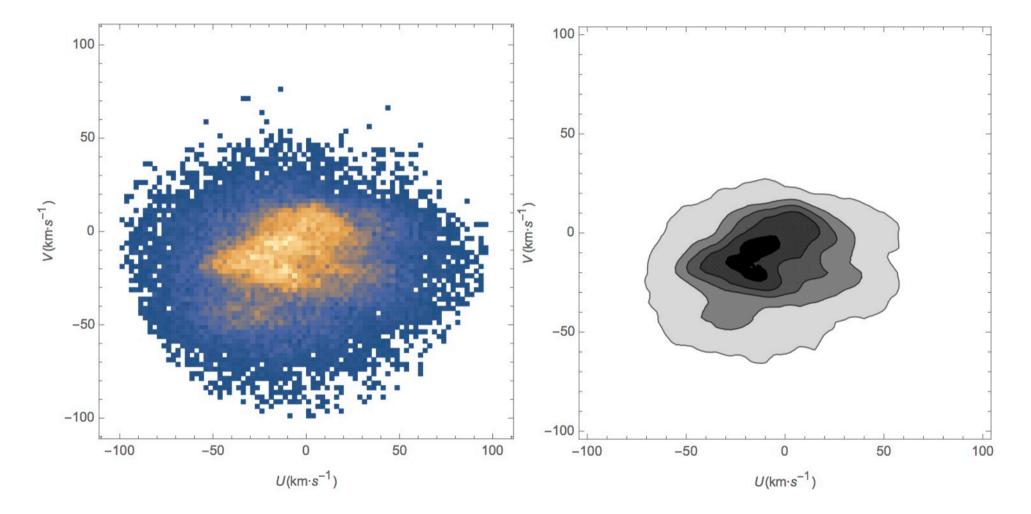
df/dt = 0

Moments of f (integrate over velocity space) give observables

If in axisymmetry and equilibrium :

 $f = f(\mathbf{J})$  useful because  $\mathbf{J}$  adiabatic invariants

#### The Galaxy is not axisymmetric



Gaia DR1 ( $\sigma_{\pi}/\pi < 0.1$ ) + RAVE DR5

### **Non-axisymmetric modelling**

For the thin disk, we use the epicyclic approximation:

$$J_R = E_R/\kappa$$
,  $J_\Phi = L_z$ ,  $J_z = E_z/\nu$ 

Start from a parametrized axisymmetric DF  $f_{\theta}$ , for instance:

$$f_0(J_R,J_\phi,J_z) = rac{\gamma ilde{\Sigma}_0 ext{exp}(-R_ ext{g}/h_ ext{R})}{4\left(2\pi
ight)^{3/2} ilde{\sigma}_R^2 ilde{\sigma}_z z_0} ext{exp}\left(-rac{J_R\kappa}{ ilde{\sigma}_R^2}-rac{J_z
u}{ ilde{\sigma}_z^2}
ight)$$

Then fit also the non-axisymmetric potential parameters to get the best possible  $f_{\theta} + \varepsilon f_{I}$  fit :  $\Phi_{1}(J, \theta, t) = \operatorname{Re}\left\{\mathcal{G}(t) \sum_{n} c_{n}(J) e^{in \cdot \theta}\right\}$  $\mathcal{G}(t) = g(t)h(t)$ 

## **Non-axisymmetric modelling**

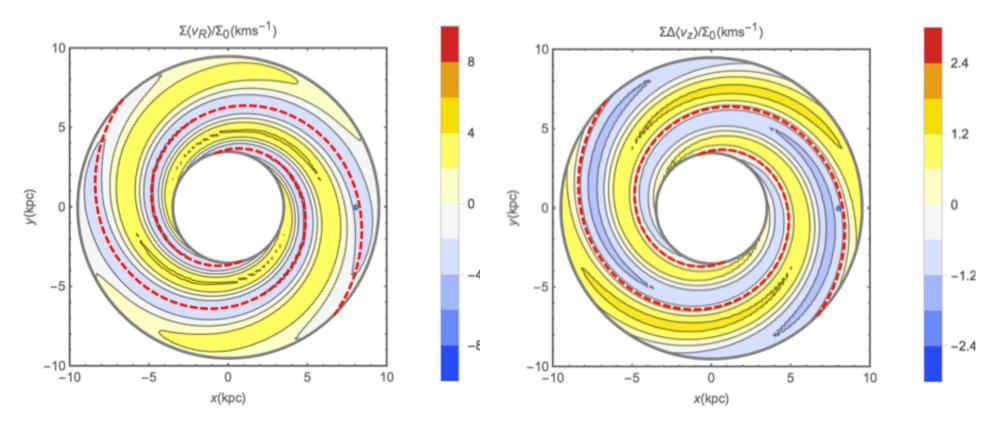
Linearized CBE: 
$$\frac{\mathrm{d}f_1}{\mathrm{d}t} + [f_0, \Phi_1] = 0$$
  
 $\frac{\mathrm{d}f_1}{\mathrm{d}t} = \frac{\partial f_0}{\partial \mathbf{J}} \cdot \frac{\partial \Phi_1}{\partial \boldsymbol{\theta}}$   
 $\Rightarrow f_1(\mathbf{J}, \boldsymbol{\theta}, t) = \operatorname{Re}\left\{\frac{\partial f_0}{\partial \mathbf{J}}(\mathbf{J}) \cdot \sum_n nc_n(\mathbf{J}) \frac{h(t)\mathrm{e}^{\mathrm{i}n \cdot \boldsymbol{\theta}}}{n \cdot \boldsymbol{\omega} + \omega_p}\right\}$ 

Assumption: we are currently in plateau of max amplitude

Take BT08 MW potential for  $\Phi_0$ , Schwarzschild DF for  $f_0$ , 3D log spiral with local amplitude of 60% of backgd for  $\epsilon\Phi_1$ , compute DF moments

## First order moments for log spirals

Monari, Famaey & Siebert (2016)



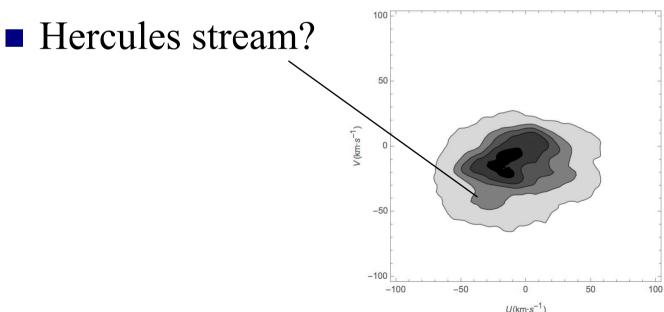
Breathing mode with  $\Delta < v_z > \sim 1$  km/s (up to 3 km/s when coupled w bar)

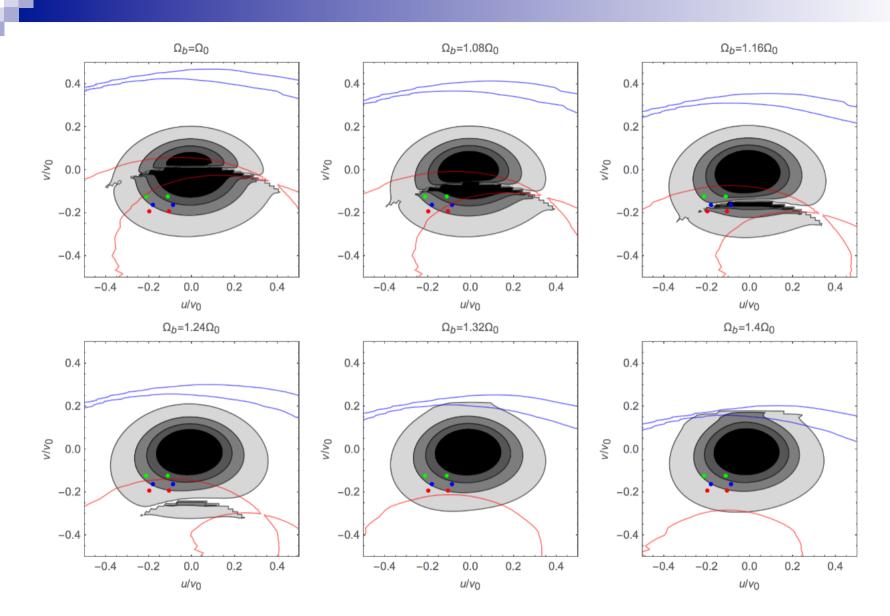
**Could be larger for transient spirals? (work in progress)** 

## **Recover bar and spiral parameters**

- Pattern speed of the bar?
- 3D density of RC stars + gas kinematics
- $\Rightarrow$  long extension of the bar reaching R~5 kpc
- $\Rightarrow \Omega_0 < \Omega_b < 1.45 \ \Omega_0$

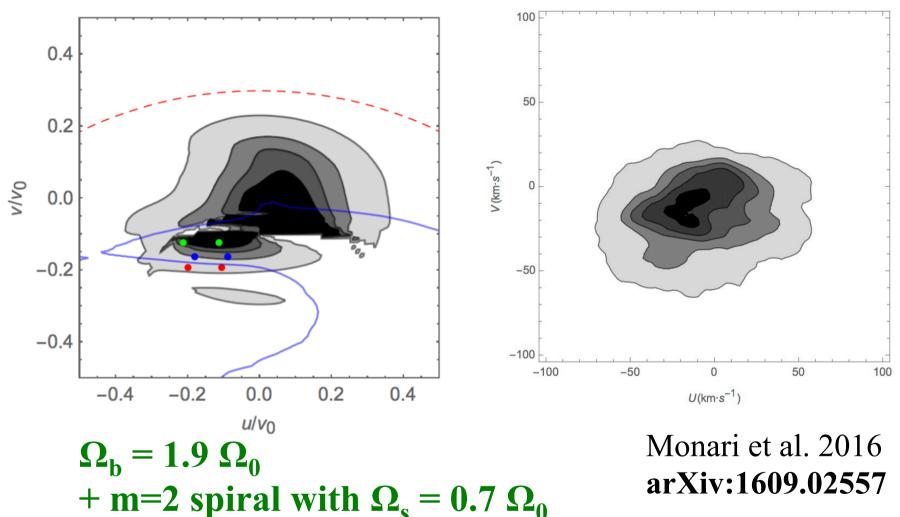
(Portail, Wegg, Li, Gerhard et al.)





Quadrupole, ratio of bar/axisym radial force at the Sun = 1%,  $\phi_b = 25^{\circ}$ 

Not a fit...



Bar pattern speed in accordance with all the old results from Dehnen, Minchev, Bovy, etc. + N-body simulations of Quillen et al (2011)

# Conclusions

- Include the effect of the bar and spirals in the DF in action-angle coordinates => will be able to directly fit the DF and pot. parameters to observations
- Spirals produce non-zero mean vertical motions (breathing modes), more important when coupled with bar or when spirals are strongly transient
- No alternative to a fast bar (Ω<sub>b</sub> > 1.8 Ω<sub>0</sub>) found to explain shape of local velocity space. Has to be >1.3 Ω<sub>0</sub> to avoid signature of bar corotation
- Antoja et al. (2014) based on RAVE between ~0.9 and ~1.1 R0 => Hercules consistent with bar's OLR