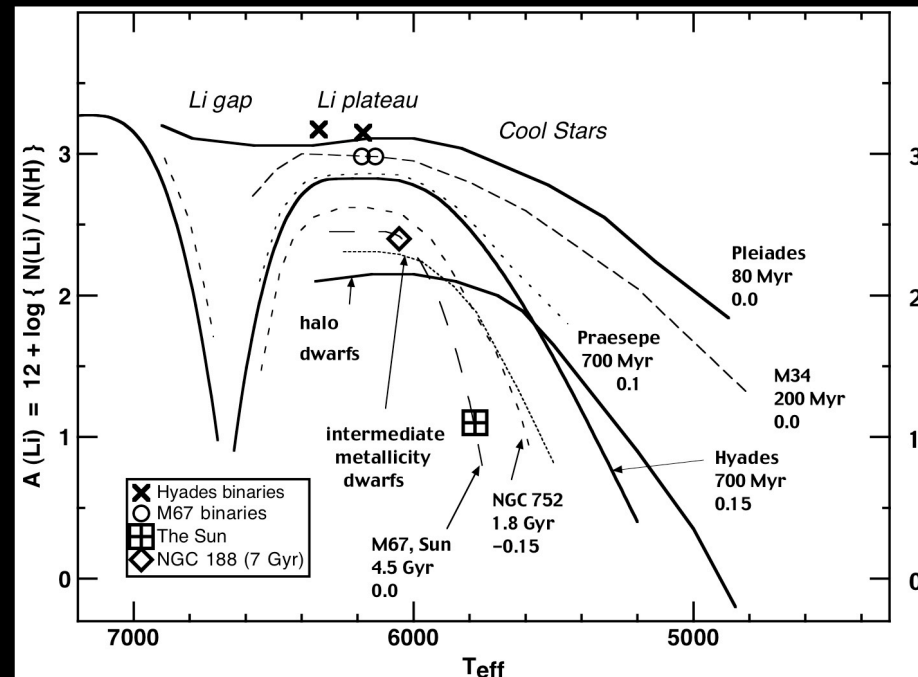
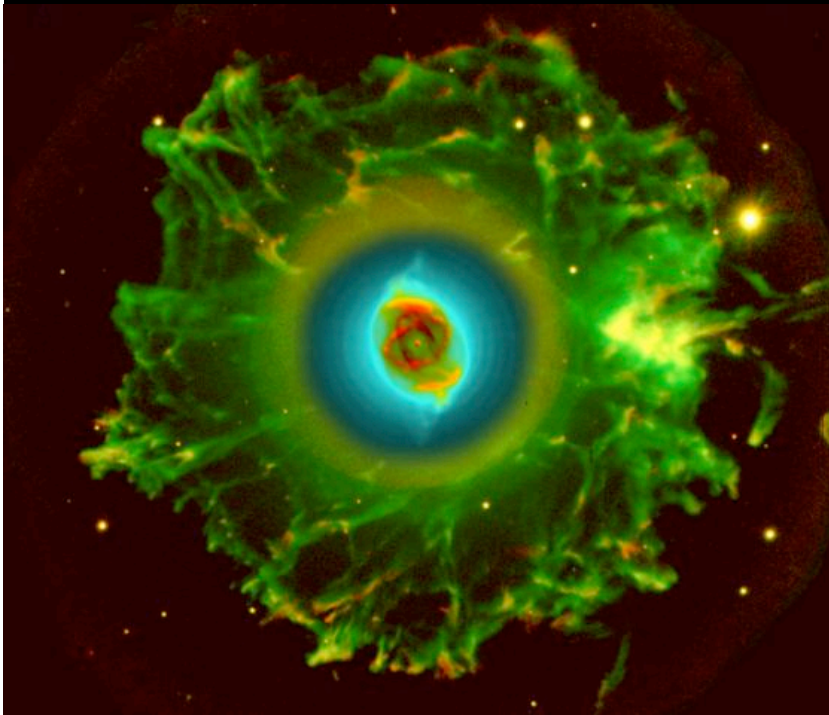


Lithium processing in stars

Diagnosis for stellar structure and evolution



Corinne Charbonnel

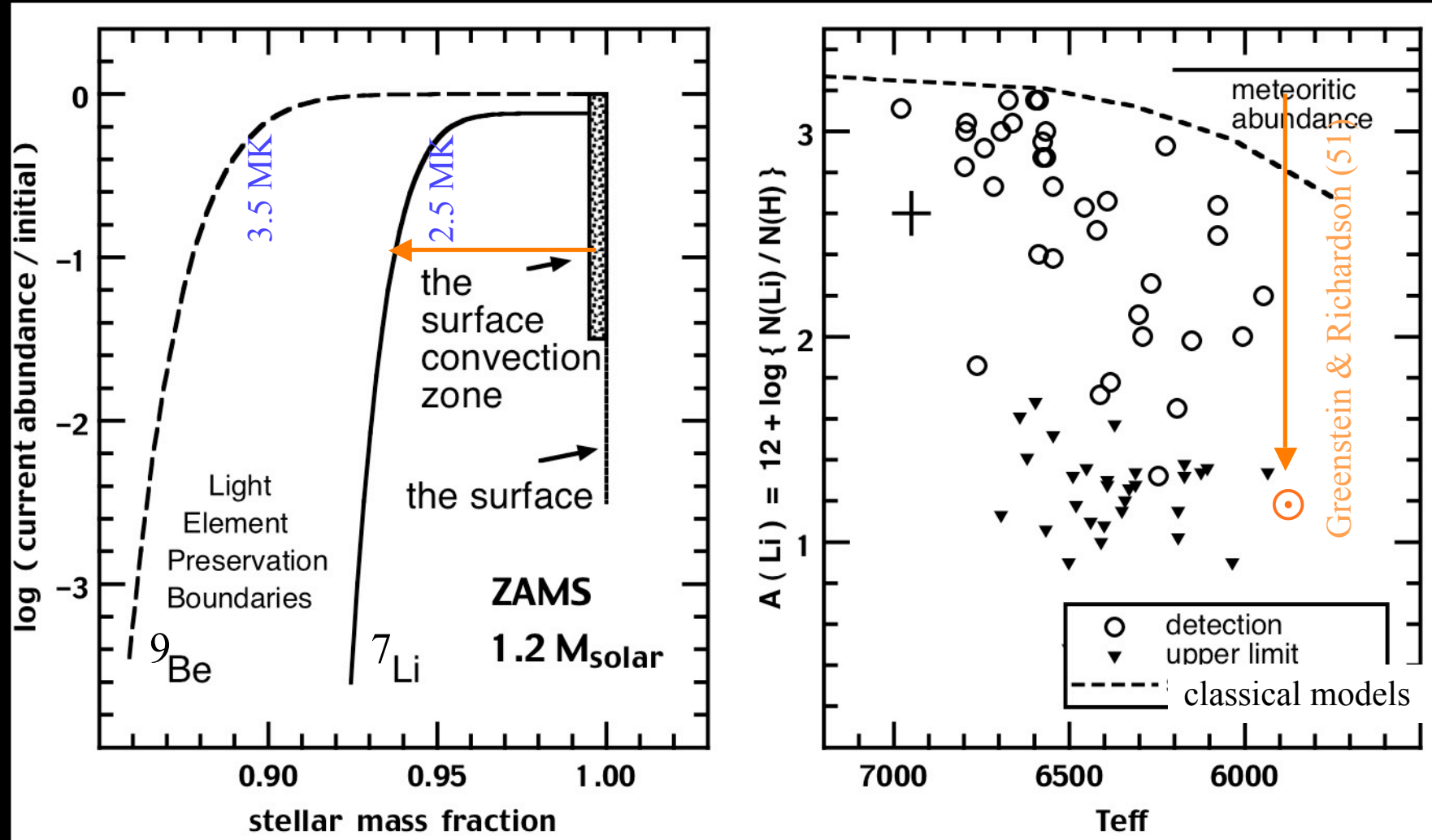
Geneva Observatory (Switzerland) & CNRS (France)

S.Talon, T.Decressin, P.Eggenberger, S.Mathis

Montreal (Canada), Geneva (Switzerland), CEA (France)



Abundance tomography in low-mass stars

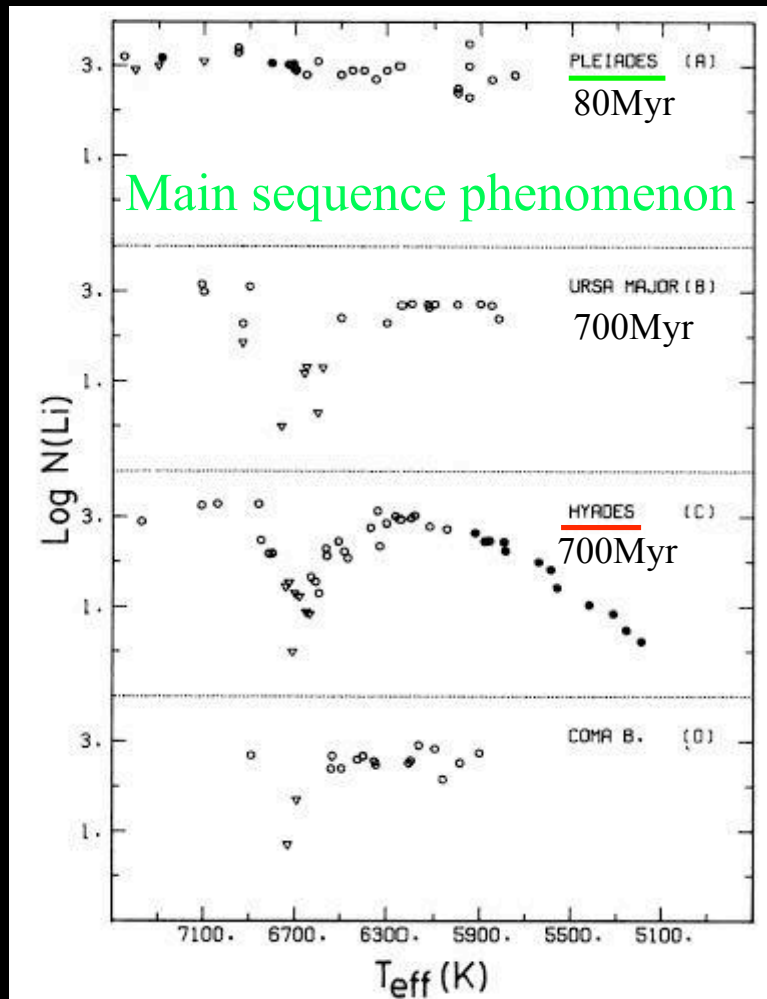


Data in field stars
by Boesgaard & Tripicco (86b)

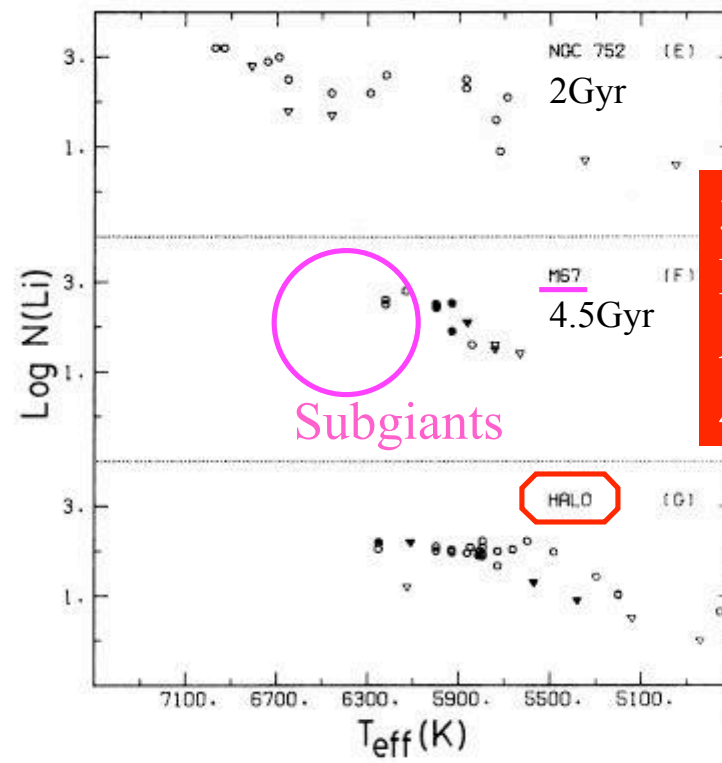
Fig. from Deliyannis, Pinsonneault & Charbonnel (00)

The lithium dip

First observed in the Hyades (Wallerstein, Herbig & Conti 65; Boesgaard & Tripicco 86a)



Observed in all open clusters older than ~ 200 Myr and in field stars (Balachandran 95)



3 parameters:
 M_* ($\sim T_{\text{eff}}$)
Age
 Z

Fig. from Charbonneau & Michaud (88)

The lithium dip - Atomic diffusion

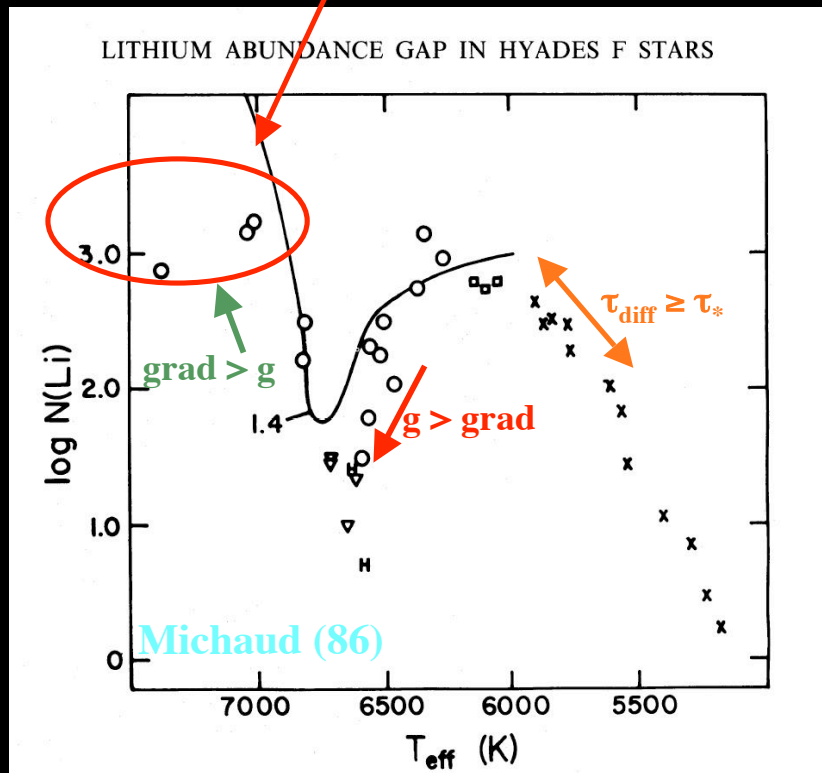
New radiative force calculations (Richer et al. 99)

→ $\dot{M}_{\text{loss}} \sim 10^{-15} \text{ M}_{\odot} \text{ yr}^{-1}$

Michaud (86) → Michaud et al. (00)

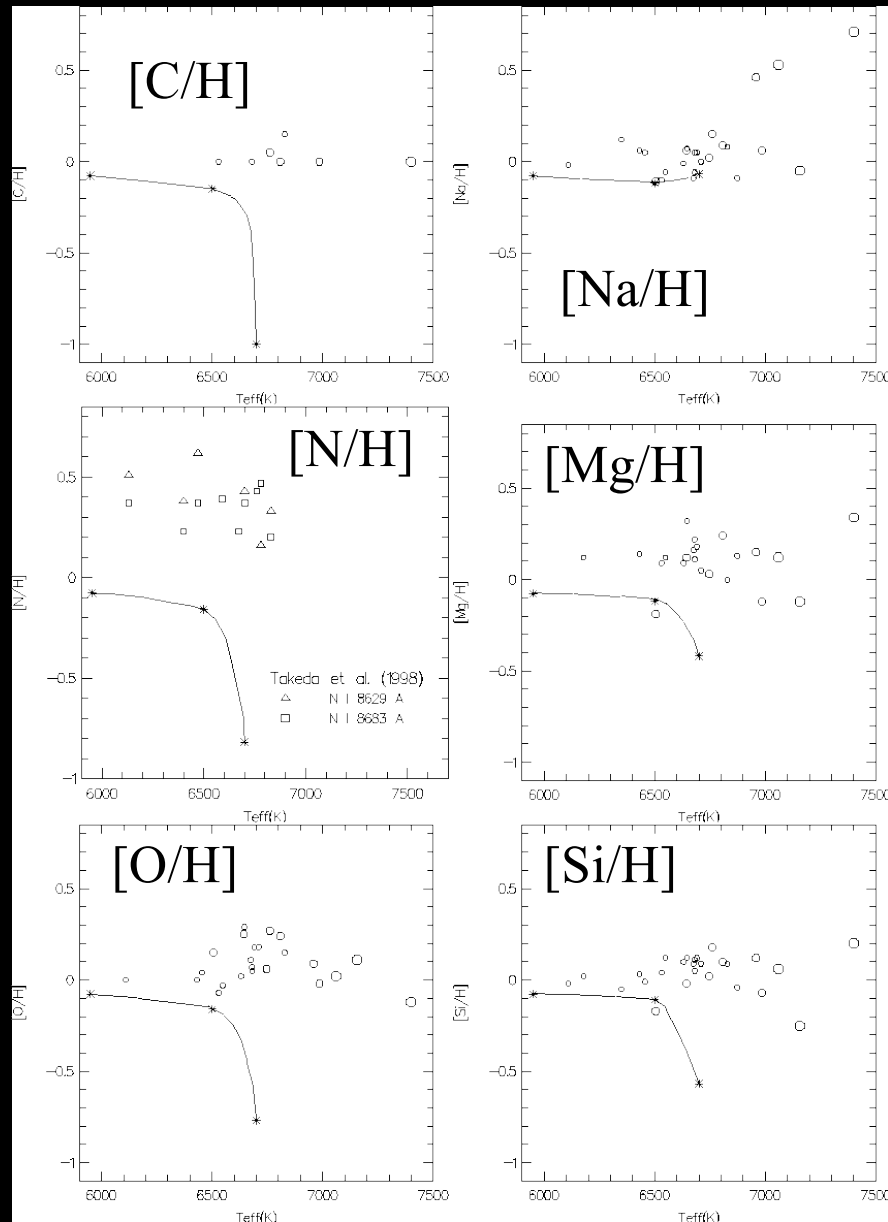
+ Gravit. settling, thermal diffusion (↓)
& radiative acceleration (↑)

+ Calculated entirely from first principles



Diffusion becomes increasingly efficient with decreasing density below the CE, i.e., with increasing T_{eff}

The lithium dip - Atomic diffusion



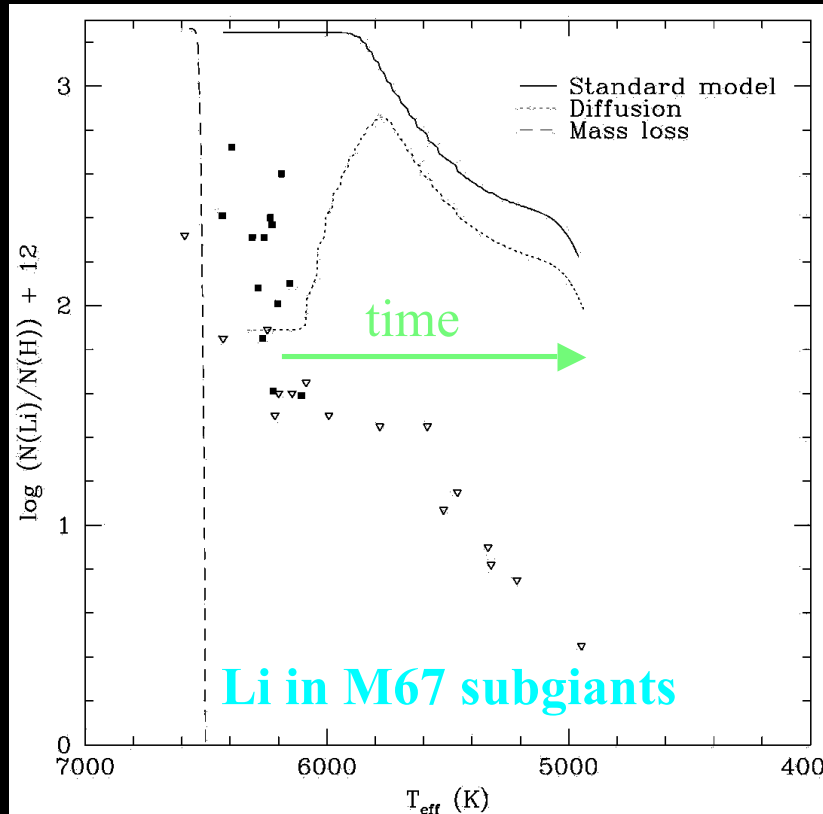
Problems :

- ✓ Heavy elements are also expected to settle down in Li-deficient stars
- Incompatible with the observational data across the dip

Fig. and data in the Hyades
from Varenne & Monier (99)
Predictions by Turcotte et al. (98)

See also Gebran, Monier & Richard (08)
for the Pleiades and ComaB

The lithium dip - Atomic diffusion



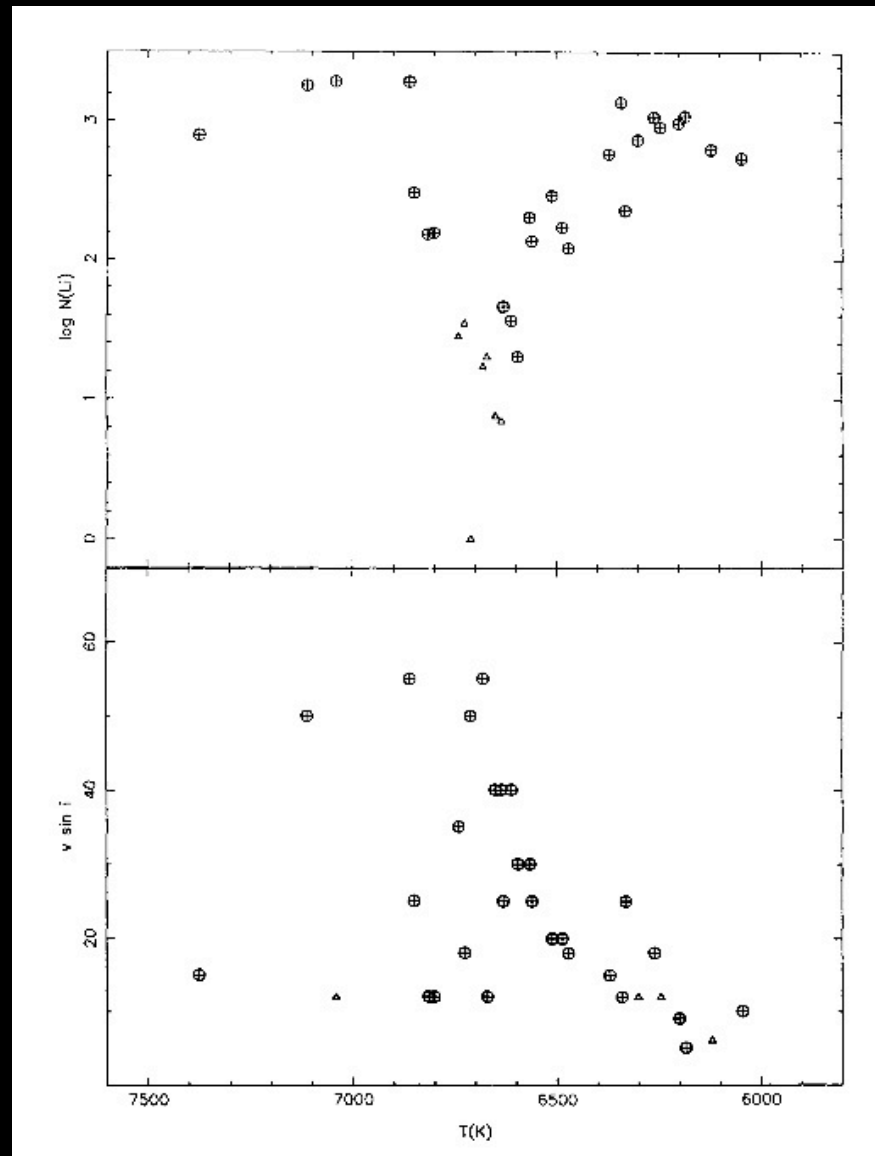
Deliyannis et al. (97)
See also Pilachowski et al. (88)
& Balachandran (95)

Problems :

- ✓ Li is not destroyed, it just settles out of the convective envelope
- Incompatible with the Li data in the Hertzsprung gap (field and open cluster subgiants)
- Strongly favours explanations relying on nuclear destruction of Li

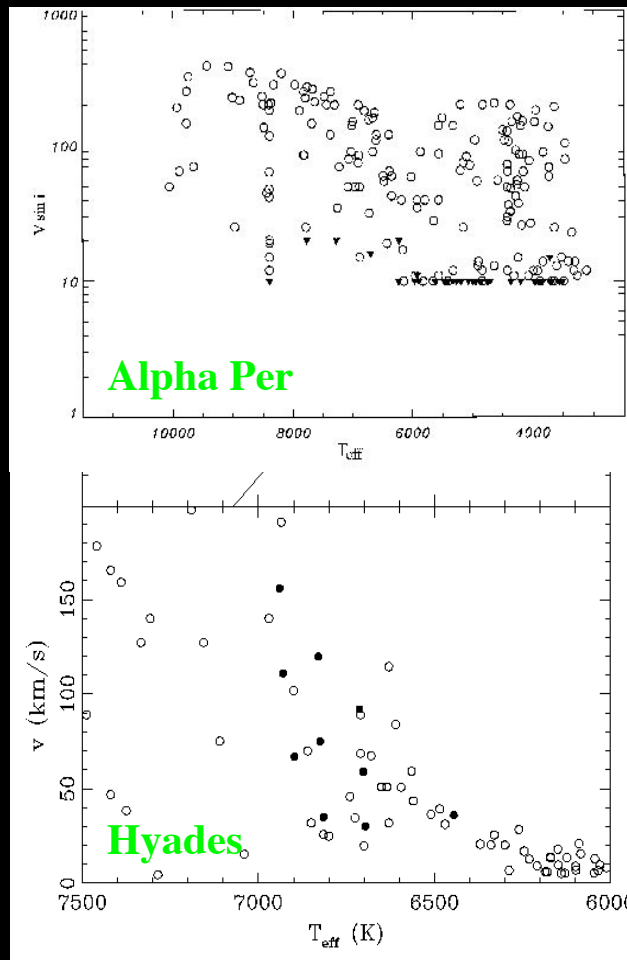
**Atomic diffusion is
not the only process responsible
for the Li dip in open clusters**

The lithium dip - Rotation



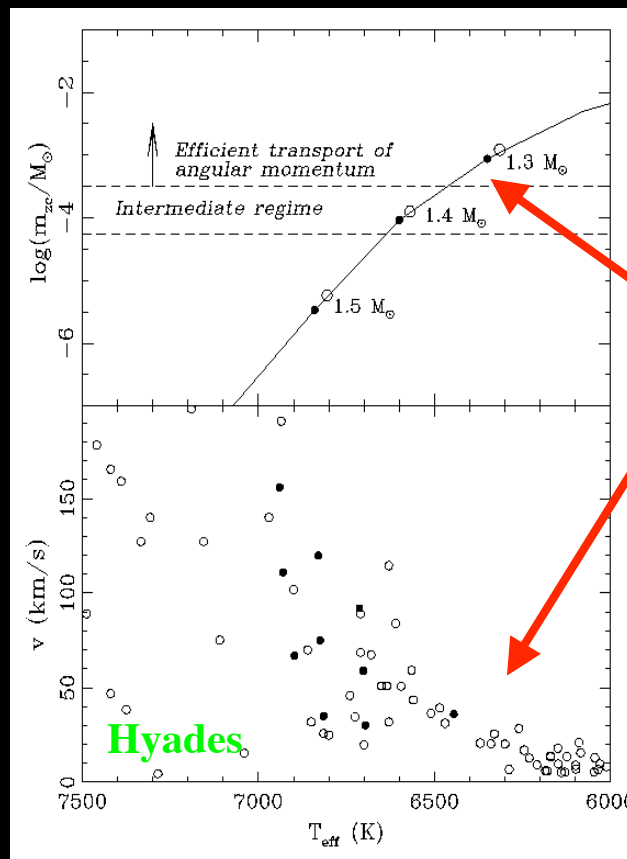
Boesgaard (87)

The lithium dip : A pivotal T_{eff} for stellar structure and rotational history



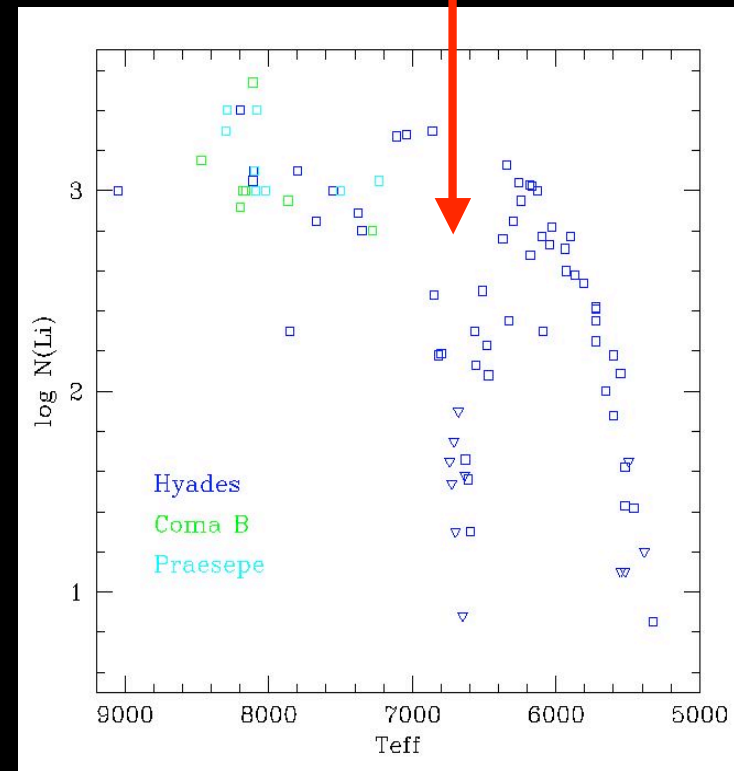
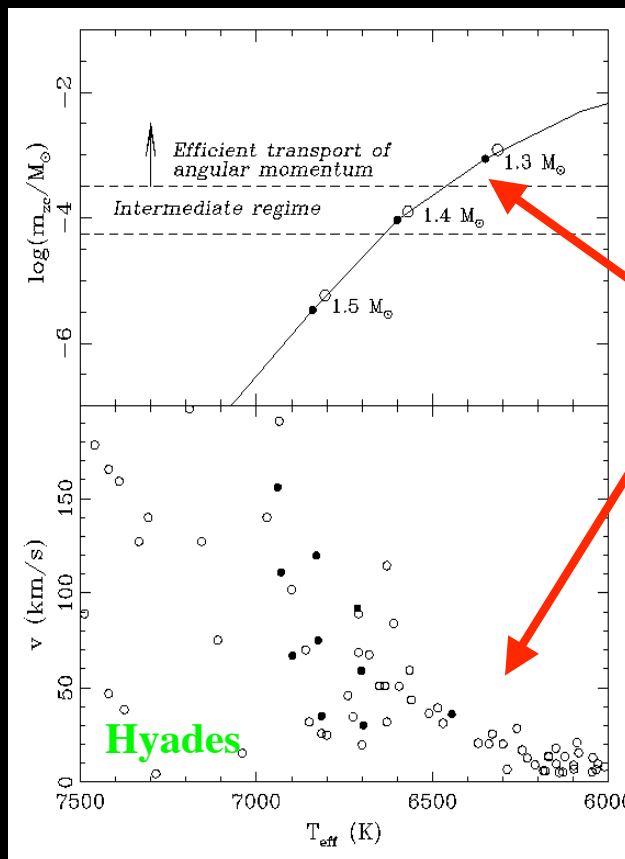
Physical processes for the evolution of the surface velocity are different, or operate on different timescales on each side of the dip

The lithium dip : A pivotal T_{eff} for stellar structure and rotational history



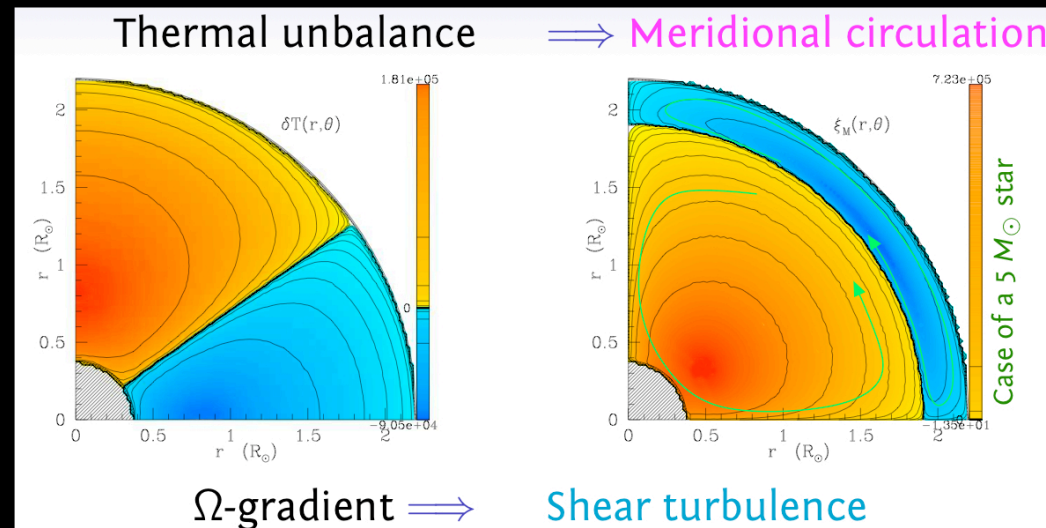
Deep enough surface convective region
to sustain a dynamo
and to produce a surface magnetic field
that is then responsible for efficient braking

The lithium dip : A pivotal T_{eff} for stellar structure and rotational history



Transport of angular momentum (advection + turbulence)

$$\underbrace{\frac{d}{dt} [r^2 \Omega]}_{\text{Contraction or expansion}} = \underbrace{\frac{1}{5r^2} \frac{\partial}{\partial r} [r^4 \Omega U_2]}_{\text{Advection (MC)}} + \underbrace{\frac{1}{r^2} \frac{\partial}{\partial r} [v r^4 \frac{\partial \Omega}{\partial r}]}_{\text{Diffusion (shear)}}$$



Transport of chemicals

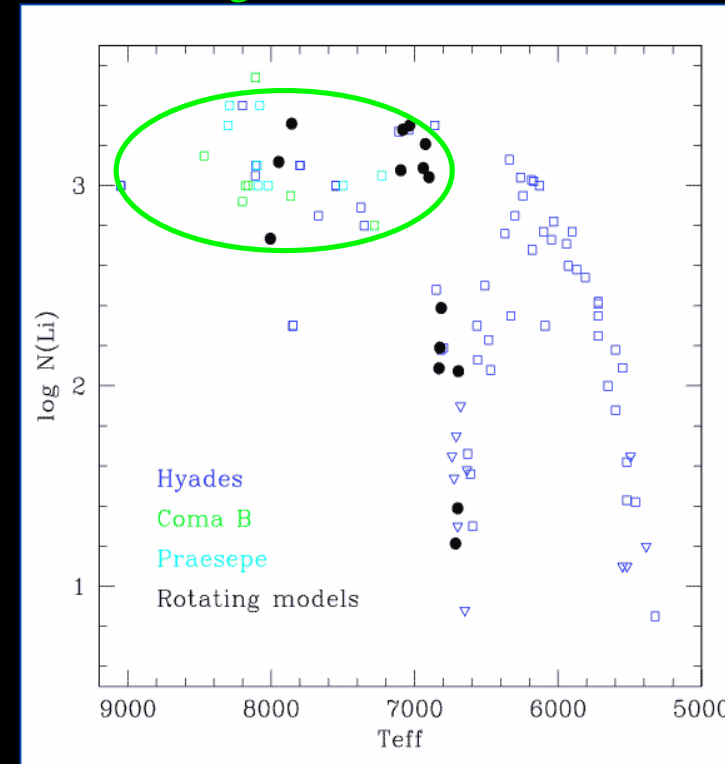
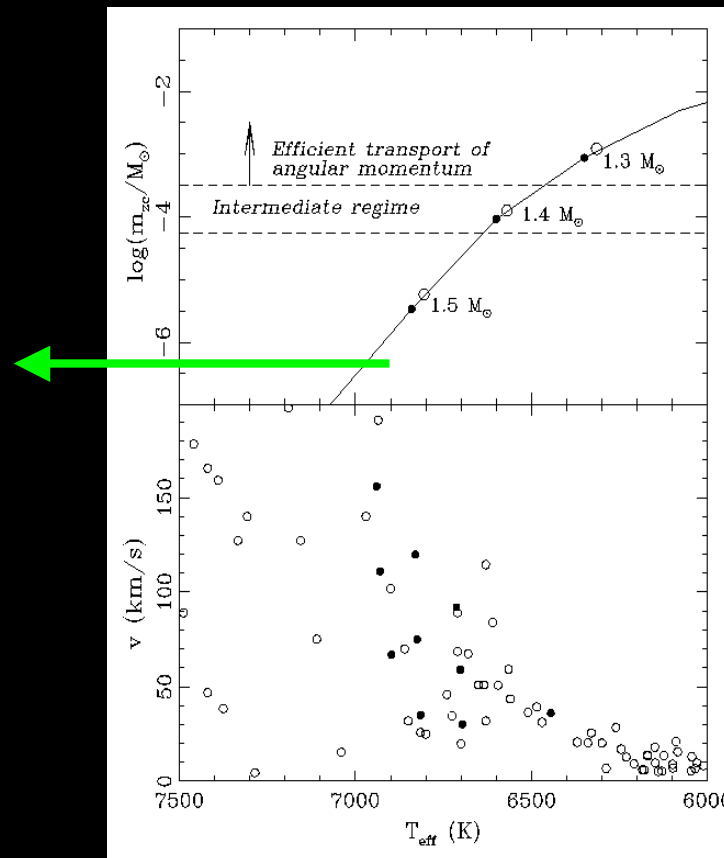
$$\rho \frac{dY_i}{dt} = \underbrace{\rho \frac{dY_i}{dt}}_{\text{nuclear}} + \underbrace{\frac{1}{r^2} \frac{\partial}{\partial r} \left[r^2 \rho (D_{\text{eff}} + D_v) \frac{\partial Y_i}{\partial r} \right]}_{\text{diffusion by MC and shear}}$$

Zahn (1992), Chaboyer & Zahn (1992), Talon & Zahn (1997),
Maeder & Zahn (1998), Mathis & Zahn (2004), Decressin et al. (2009)

Rotation-induced mixing : The hot side of the lithium dip

Teff \geq 6900 K : Very shallow surface convective zone
 Unefficient magnetic generation via a dynamo process
 Not slowed down by a magnetic torque

Angular momentum loss
 drives circulation and depletes Li
 Regime with no net angular momentum flux
 The weak mixing counterbalances atomic diffusion

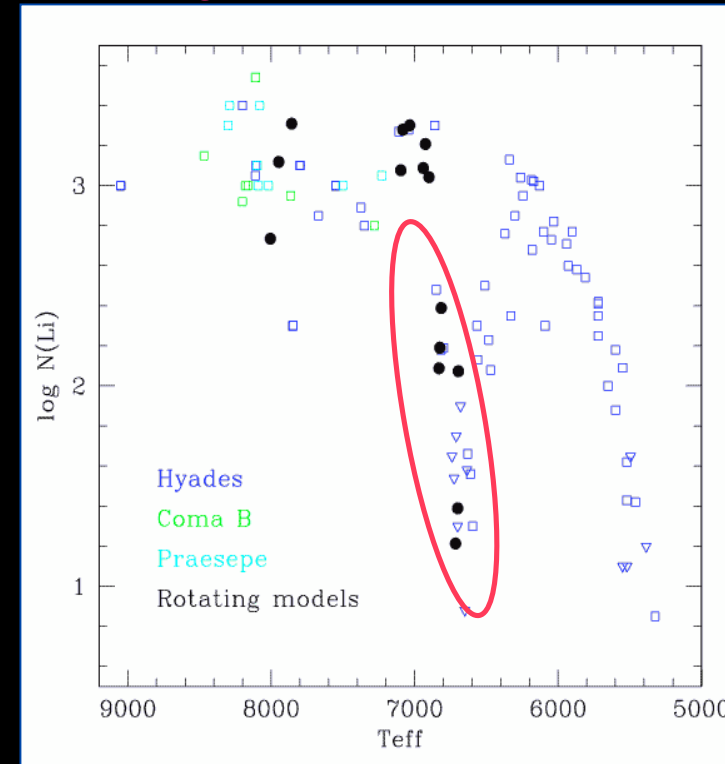
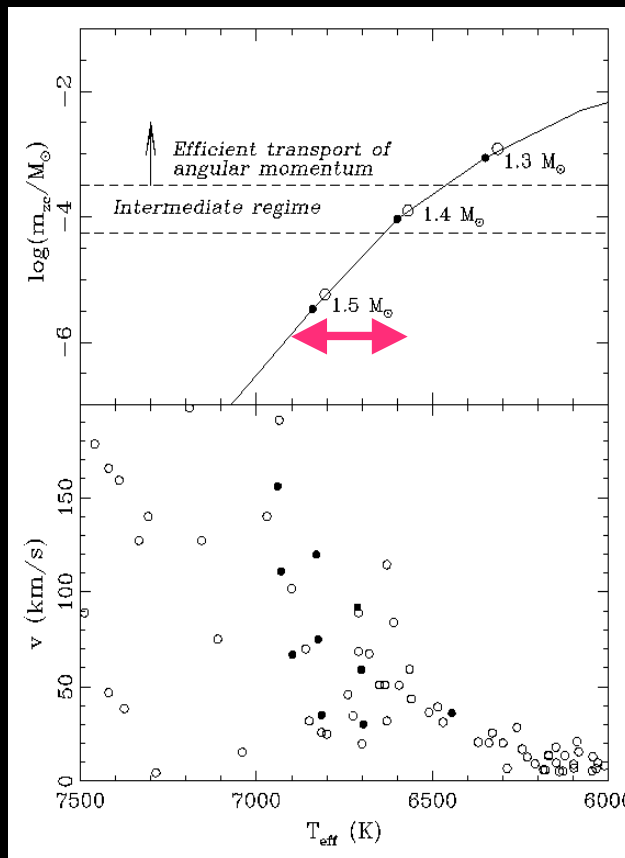


Talon & Charbonnel (98), Palacios et al. (03)

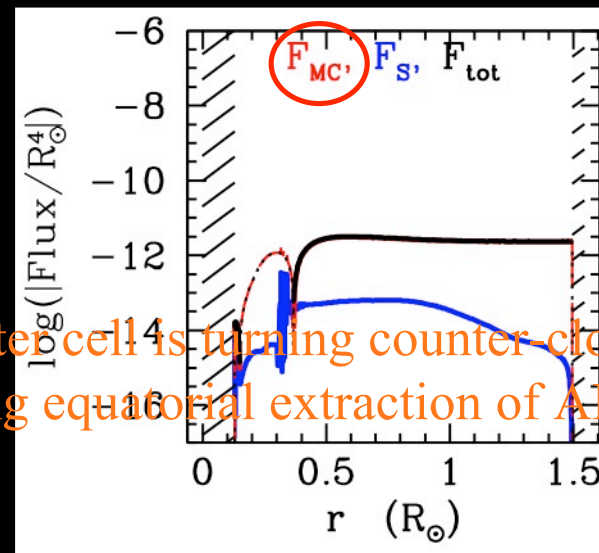
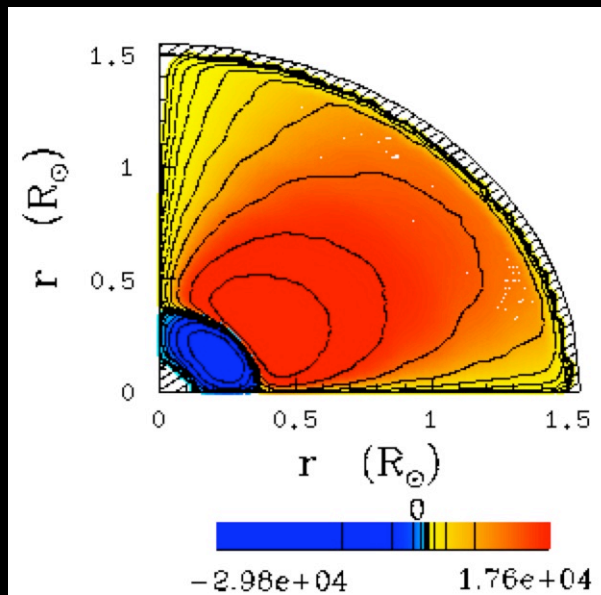
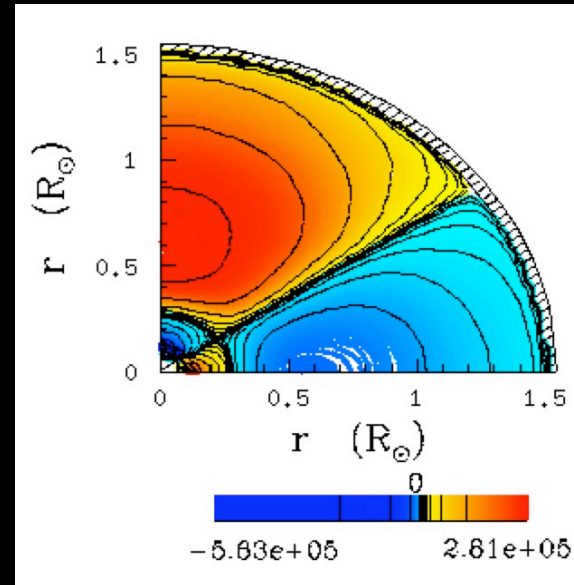
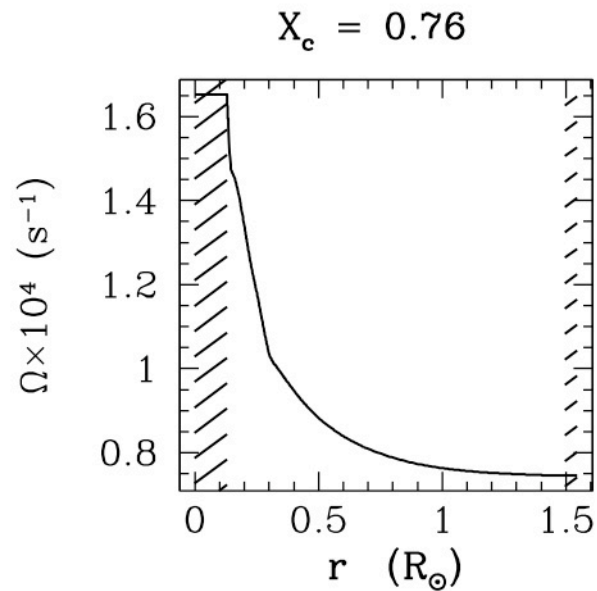
Rotation-induced mixing : The hot side of the lithium dip

6600 K \leq T_{eff} \leq 6900 K : Deeper convective envelope
Weak magnetic torque slows down the outer layers

Angular momentum loss
drives circulation and depletes Li
Meridional circulation and shear increase
 \Rightarrow Larger destruction of Li



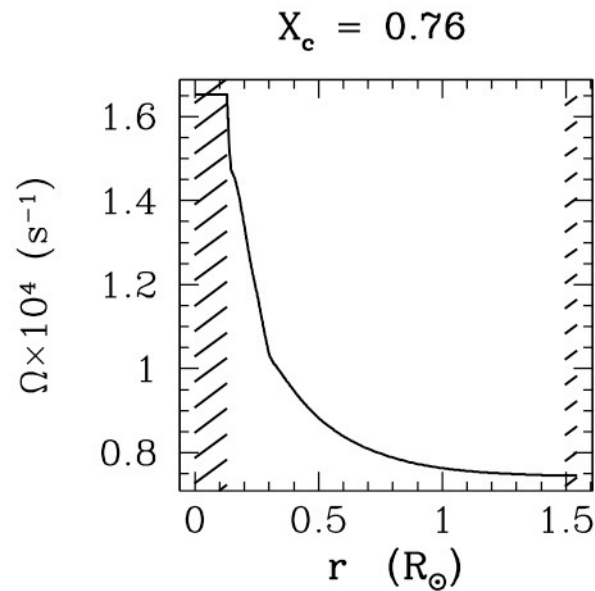
Talon & Charbonnel (98), Palacios et al. (03)



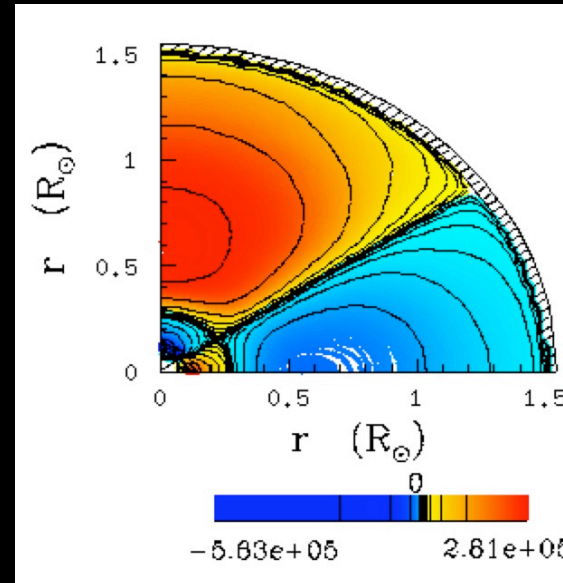
STAREVOL
Mathis et al. (06)
Decressin et al. (08)

$1.5M_{\odot}, Z_{\odot}$
 $V_{ini}=100 \text{ km s}^{-1}$
 t (Hyades) :
 $T_{eff} = 7020\text{K}$
 $V = 80 \text{ km s}^{-1}$
 $Li = 2.9$

The outer cell is turning counter-clockwise
 allowing equatorial extraction of AM by the wind



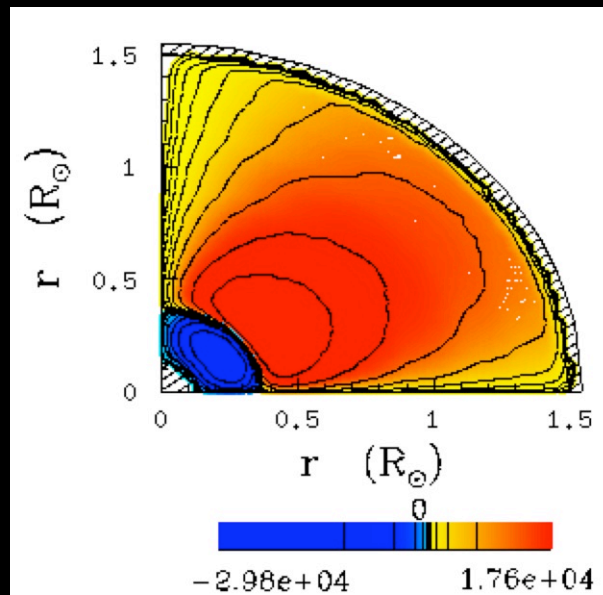
Angular velocity profile



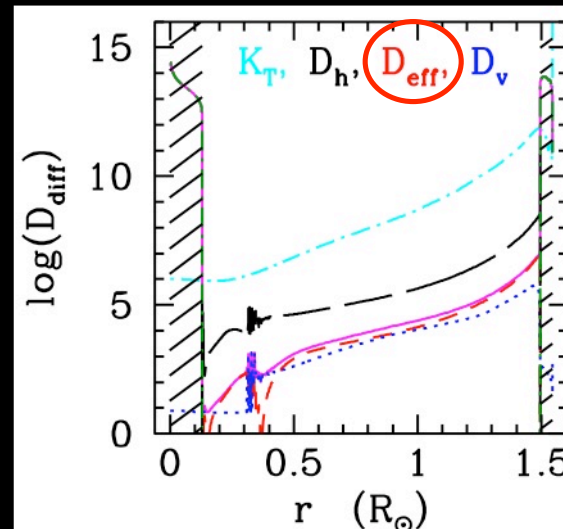
T-excesses

STAREVOL
Mathis et al. (06)
Decressin et al. (08)

$1.5 M_{\odot}, Z_{\odot}$
 $V_{ini} = 100 \text{ km s}^{-1}$



Meridional circulation currents

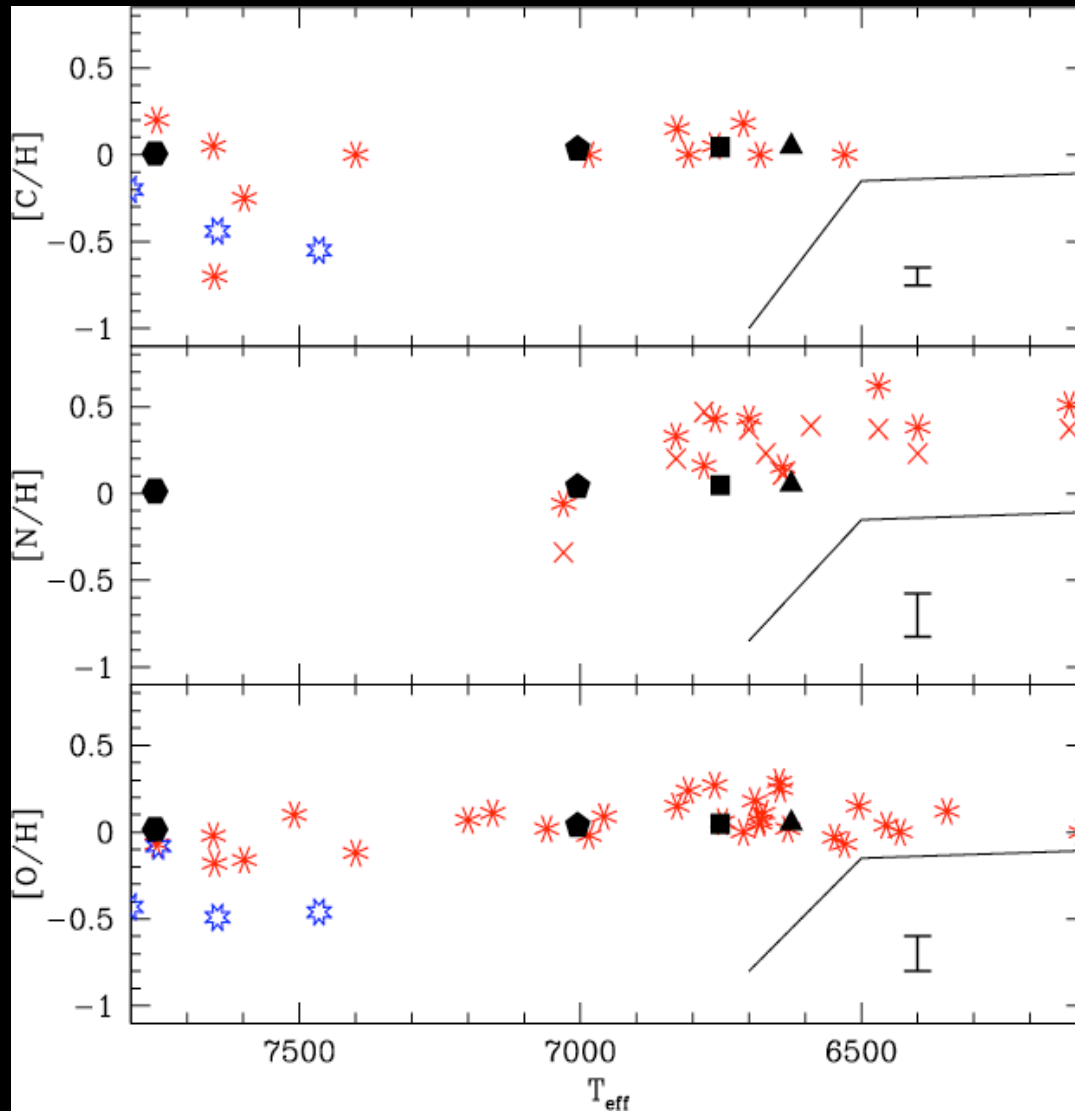


Transport of chemicals

Thermal diffusivity,
 horizontal and
 vertical
 eddy-diffusivities,
 effective (MC)
 and total diffusivities

$D_h \gg D_v$

Rotation-induced mixing : The hot side of the lithium dip (MS)



CNO at the age of the Hyades

Observations in the Hyades

Varenne & Monier (98)

Takeda et al. (98)

Solid lines : atomic diffusion alone

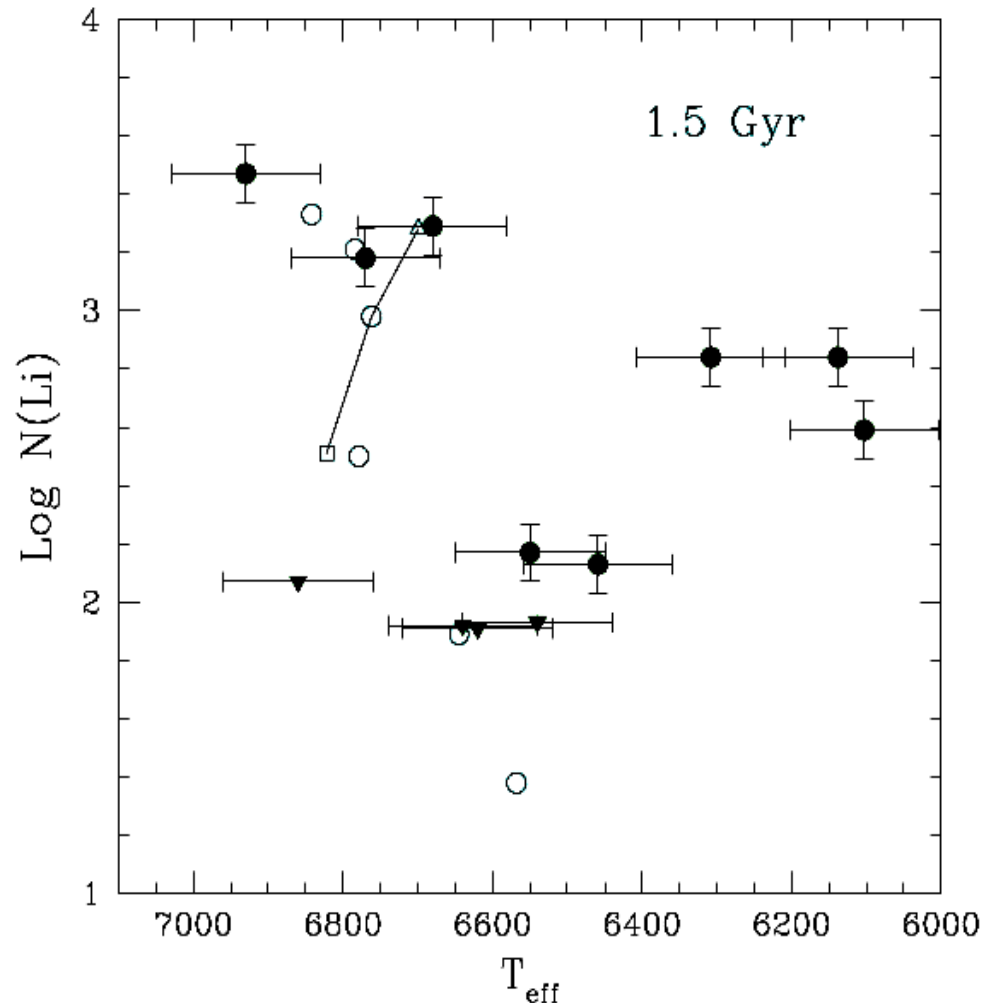
Turcotte et al. (98)

Rotating models : black points

Palacios et al. (03)

Palacios et al. (03)

Rotation-induced mixing : The hot side of the lithium dip (MS)



Li in IC 4651

Intermediate age, $M_{\text{turnoff}} \sim 1.8 M_{\odot}$

Observations in IC 4651 : black points

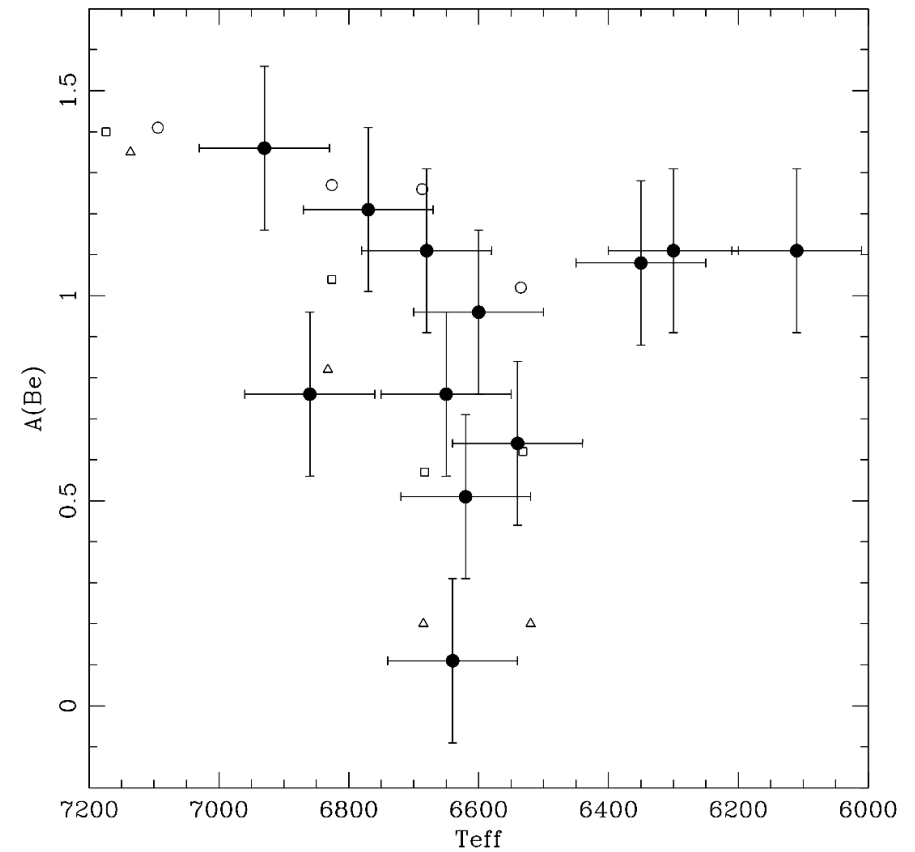
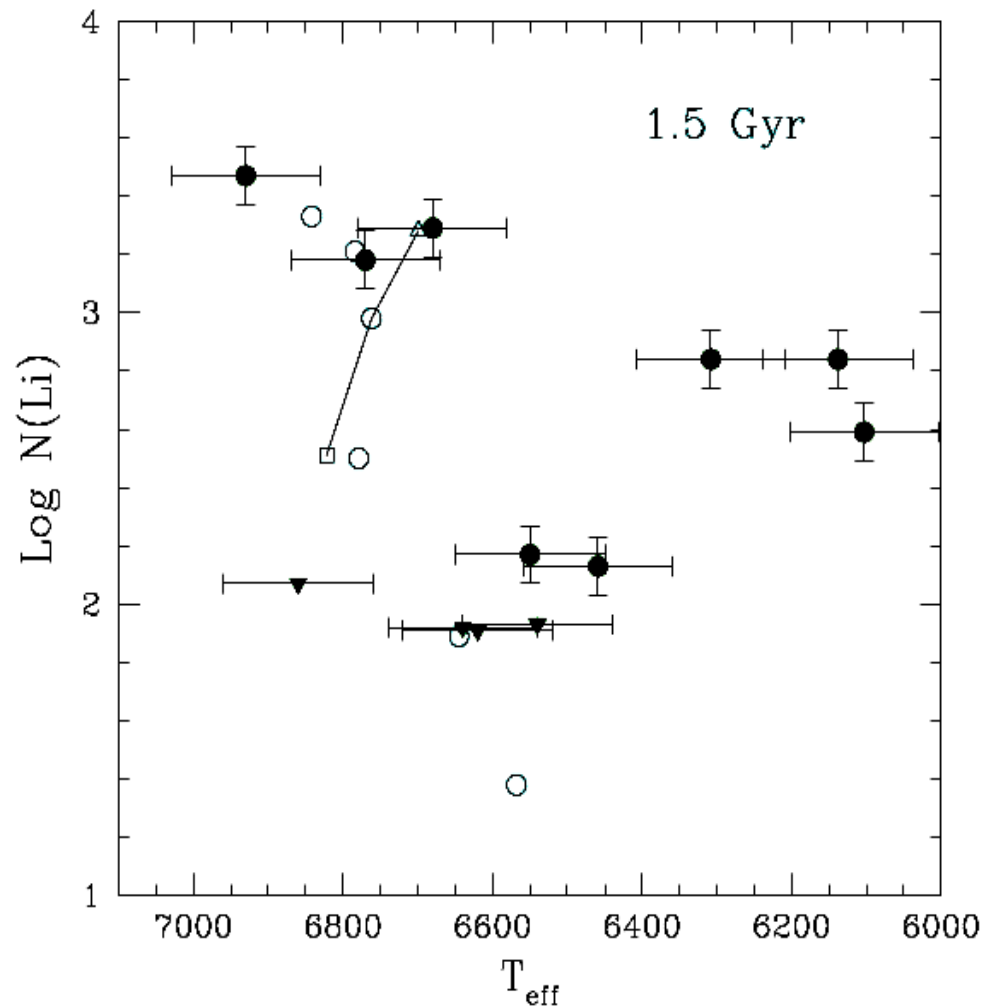
Rotating models at 1.5 Gyr : open symbols

$V_i = 110 \text{ km} \cdot \text{sec}^{-1}$ (+50 and 150 for the $1.5 M_{\text{sun}}$)
(Charbonnel & Talon 99, Palacios et al. 03)

Observations :
 ● = exact values
 ▼ = higher values

Models :
 ○ = $V_{\text{ZAMS}}=110 \text{ km/s}$
 □ = $V_{\text{ZAMS}}=80 \text{ km/s}$
 △ = $V_{\text{ZAMS}}=50 \text{ km/s}$

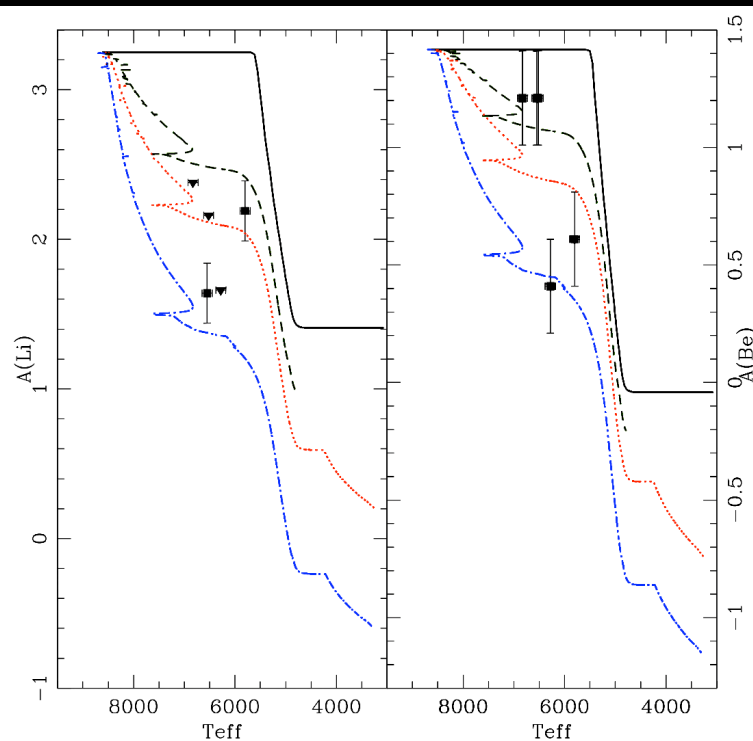
Rotation-induced mixing : The hot side of the lithium dip (MS)



Smiljanic, Pasquini, Charbonnel, Lagarde (09)

Pasquini, Randich, Zoccali, Hill, Charbonnel & Nordström (05)

Rotation-induced mixing in low-mass main subgiant stars



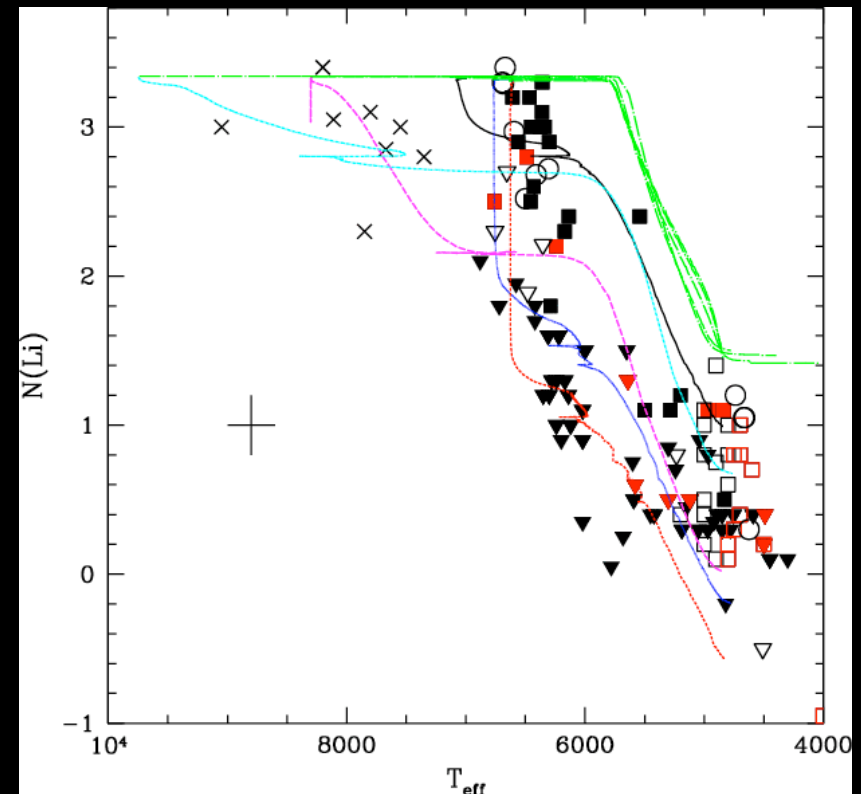
— Classical models

Models with thermohaline and rotation :

----- $V_{\text{ZAMS}}=80 \text{ km/s}$
 ----- $V_{\text{ZAMS}}=110 \text{ km/s}$
 ----- $V_{\text{ZAMS}}=180 \text{ km/s}$

Observations : IC 4651

Smiljanic, Pasquini, Charbonnel & Lagarde (09)



Standard models : **green lines**

Rotating models of various M_* : other colored lines

Observations : Field and

open cluster evolved stars

Lèbre et al. (99), Wallerstein et al. (94), Gilroy (89)

Pasquini et al. (01), Burkhardt & Coupry (98, 00)

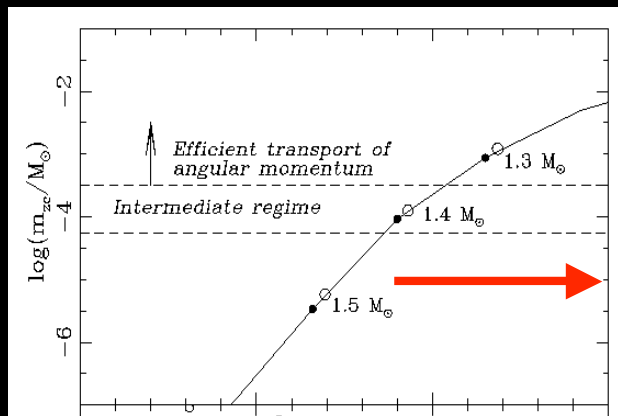
Palacios et al. (03), Pasquini et al. (04)

The rotating models
are successful
in explaining the data
for the stars lying on
or originating from
the hot side of the Li dip
(on a very large mass range!)

What about the less massive stars?

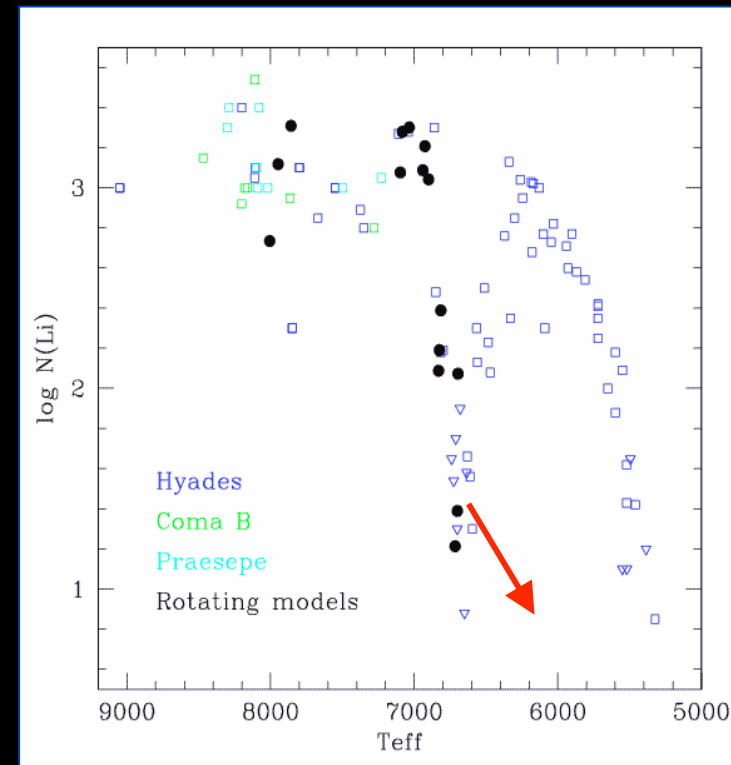
The cool side of the lithium dip

$T_{\text{eff}} \leq 6600 \text{ K}$: Deep convective envelope sustaining strong dynamo
Strong magnetic torque
Very efficient magnetic braking of the outer layers



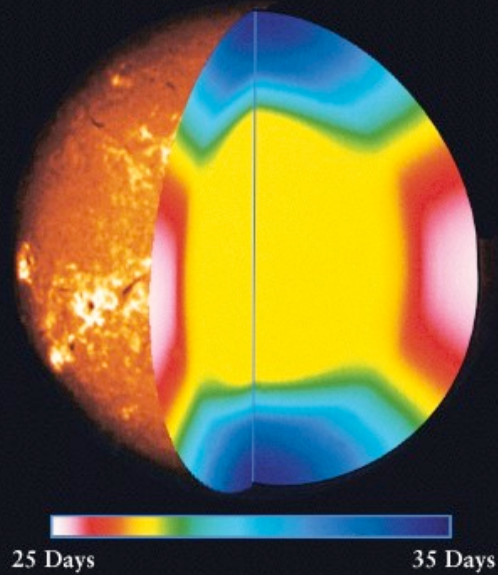
**Another mechanism is very efficient
in transporting
angular momentum in cooler stars
(Talon & Charbonnel 98)**

Meridional circulation and shear increase
 \Rightarrow Too much Li destruction



Clues from the solar case

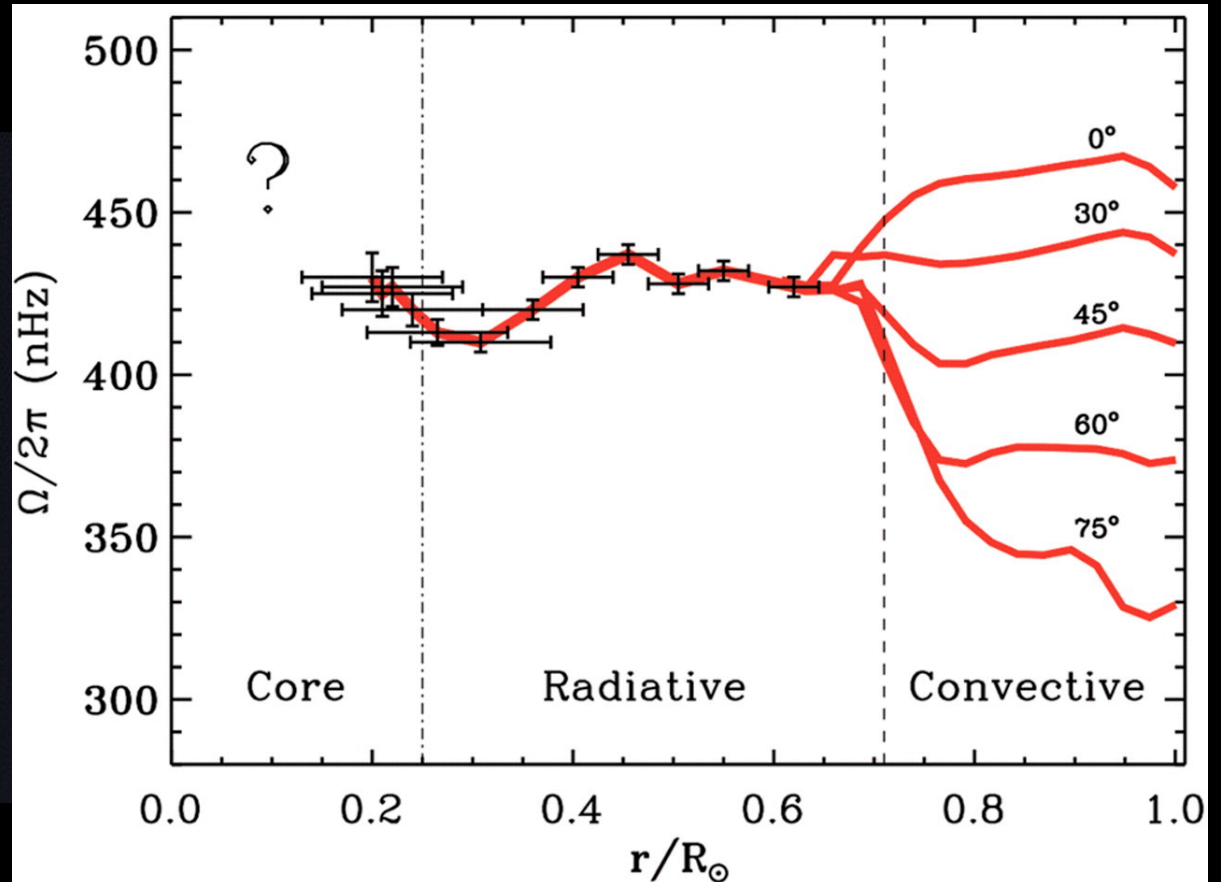
Latitudinal differential rotation



Brown et al. (89)
Kosovichev et al. (97)
Couvidat et al. (03)

...

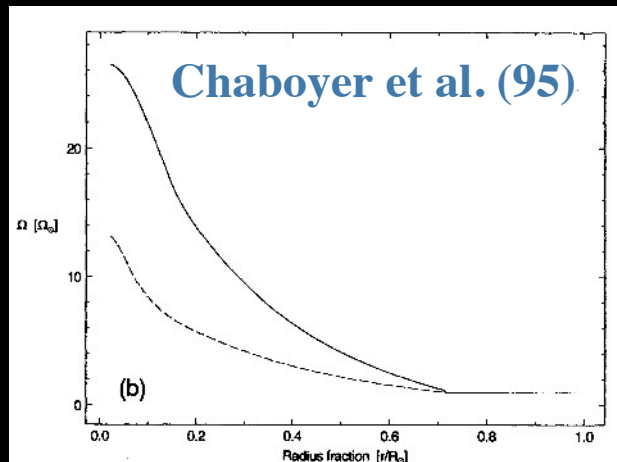
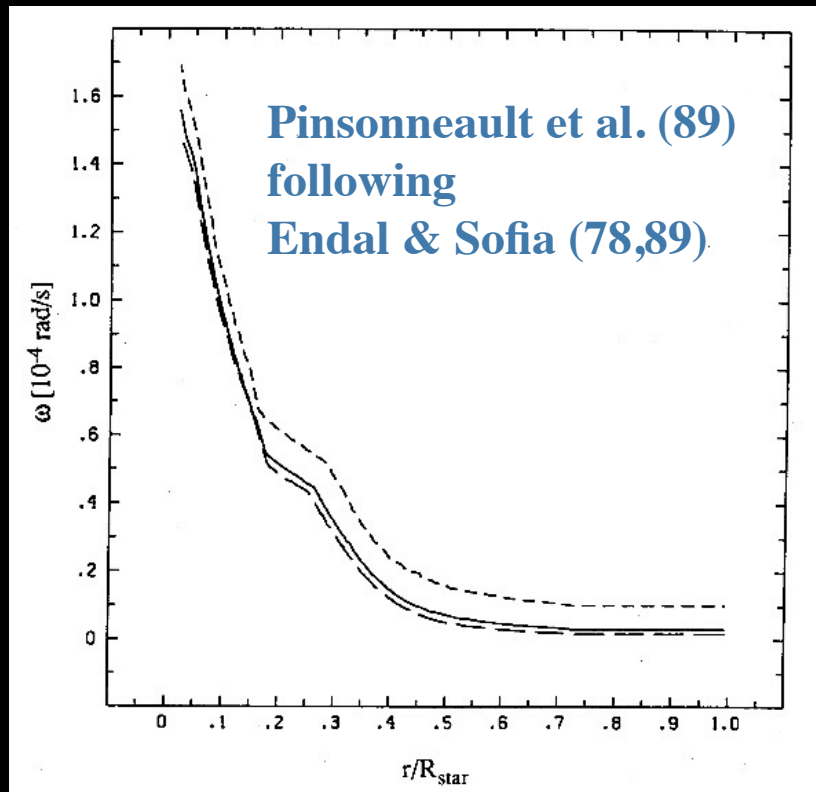
Radial rotation profile



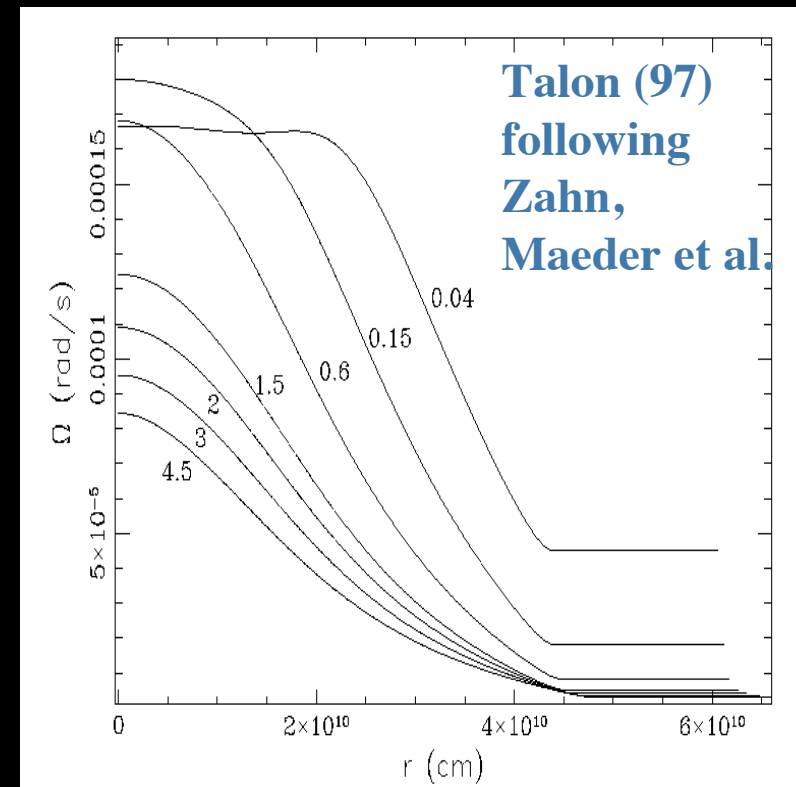
GOLF + MDI data

García et al. (07)

Clues from the solar case



Meridional circulation and shear turbulence
(Pinsonneault et al. 89, Chaboyer et al. 95, Zahn et al. 97)
fail to extract sufficient angular momentum from the
radiative interior to explain the \sim flat rotation profile
in the Sun (Brown et al. 1989)



Clues from the solar case

Meridional circulation and shear turbulence

(Pinsonneault et al. 89, Chaboyer et al. 95, Zahn et al. 97)

fail to extract sufficient angular momentum from the radiative interior to explain the \sim flat rotation profile in the Sun (Brown et al. 1989)

Sun and cool side of the Li dip \rightarrow Angular momentum transported by

Magnetic fields ?

Charbonneau & Mc Gregor 93, Barnes et al. 97, Eggenberger et al. 05

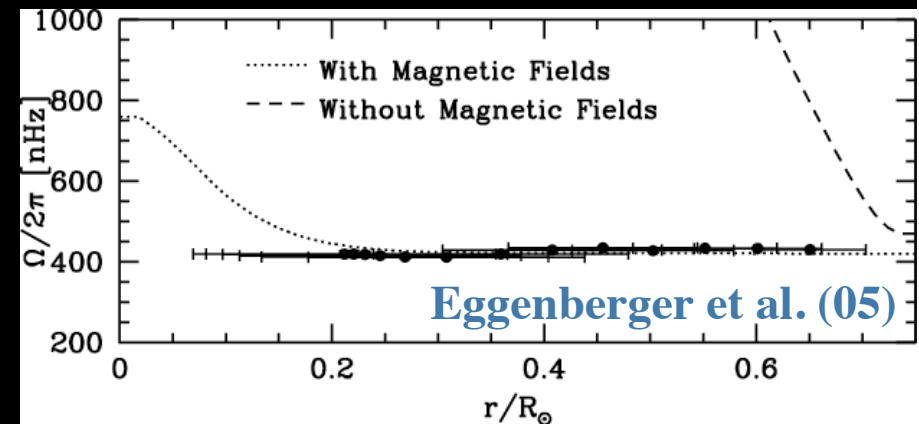
\rightarrow No correlation is expected with T_{eff}

Internal gravity waves ?

Schatzman 1993, Zahn et al. 97, Kumar & Quataert 97,

Kumar et al. 99, Talon et al. 02, Talon & Charbonnel 03,04

\rightarrow Efficiency dependent on the convection envelope characteristics,
as required by the Li data



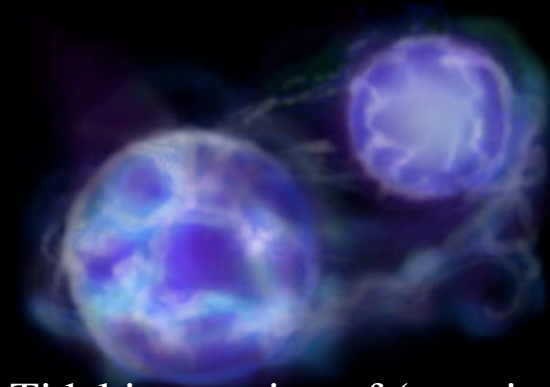
Internal Gravity Waves



Earth's atmosphere

Wind compression by topography

→ Cloud patterns formed in the regions of low-P of a topography wave



Tidal interaction of (massive) **binary systems**

Zahn (70, 75, 76), Goldreich & Nicholson (89)

Excitation of internal Gravity Waves

- In single stars, IGWs are produced by the injection of kinetic energy from a turbulent (convection) region to a stable adjacent region. Two sources of excitation:

- **Convective overshooting in the adjacent radiative zone**

García-López & Spruit 91; Frits et al. 98; Kiraga et al. 03; Rogers & Glatzmaier 05

- **Reynolds stresses in the convection zone itself**

Goldreich & Keeley 77; Goldreich & Kumar 90; Goldreich et al. 94 (GMK)

→ First applied to solar p-modes; reproduces the solar spectral energy input rate distribution; driving is dominated by entropy fluctuations

Balmforth 92

Looking for realistic wave fluxes from numerical simulations !

Wave Excitation in 2-3D numerical simulations of penetrative convection

See also

Hurlburt et al. (86, 94)

Andersen (94)

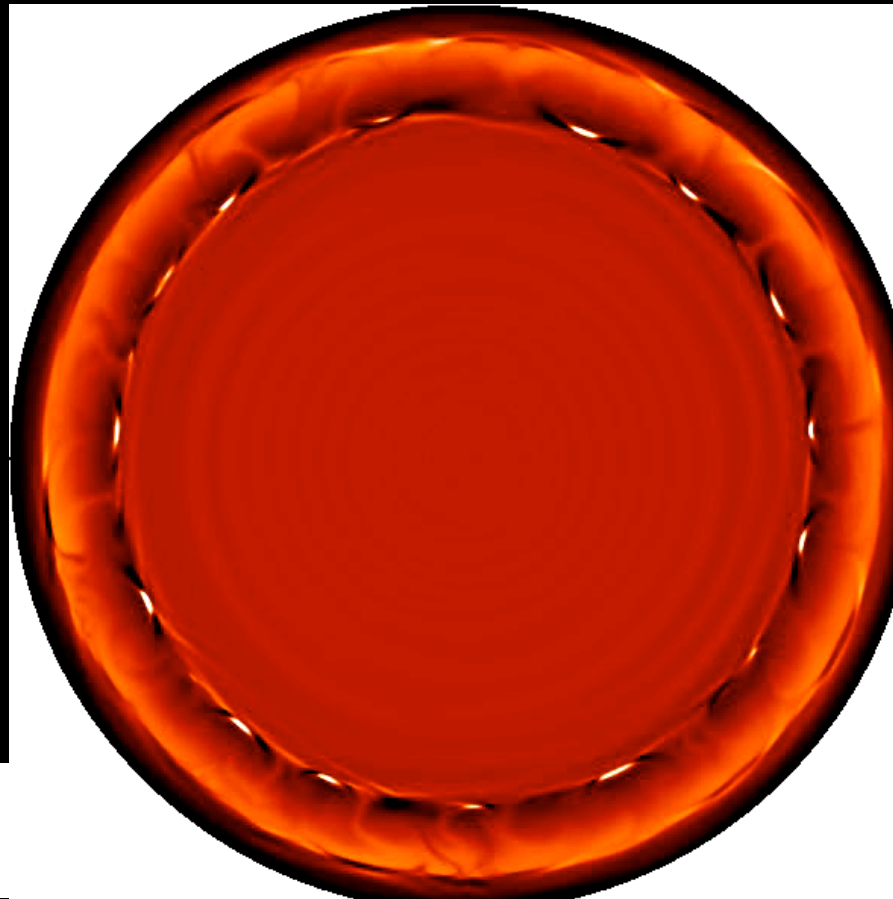
Nordlund et al. (96)

Kiraga et al. (00, 03)

Dintrans et al. (05)

Rogers & Glatzmaier (05)

Temperature
fluctuation



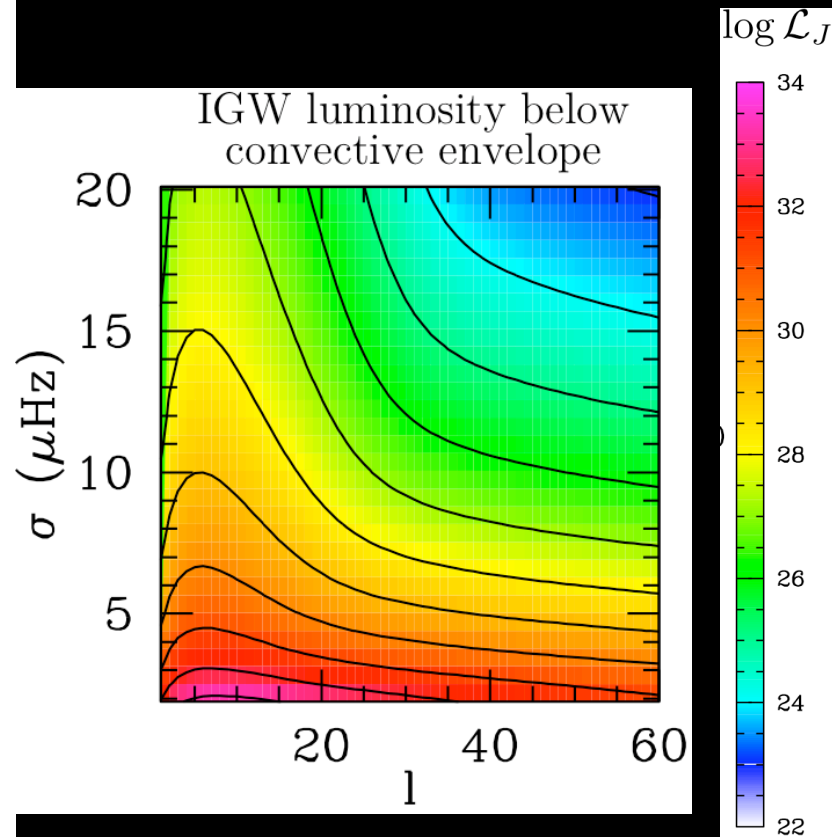
Rogers & Glatzmaier (06)

Wave Excitation in a
cylindrical (2D) model
with stratification similar
to that of the Sun

? Is the level of turbulence
reached in the simulation
realistic ?

? Analysis of the wave
spectrum as a function of
convective properties
(i.e., vs T_{eff}) ?

**For the moment, we still have to rely on theoretical estimates
for wave generation**



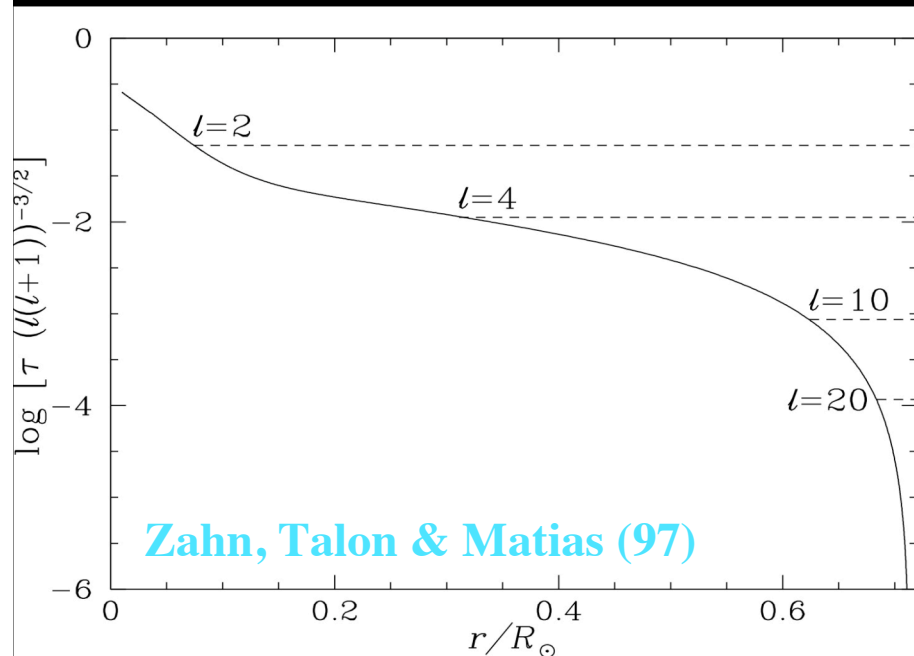
*Spectrum of IGW luminosity
below the CE
generated by Reynolds stresses
 $1.1M_{\odot}$, Z_{\odot} at 180 Myrs*

Volume excitation model of Goldreich et al. (94) is used for the kinetic energy flux \mathcal{F}_J (driving is dominated by entropy fluctuations)



Wave spectrum of angular momentum luminosity ($4\pi r^2 \mathcal{F}_J$) just below the convective envelope

Frequency $\sigma \leq$ Brunt-Väisälä frequency
(natural oscillation frequency of a displaced element in a stratified region)
Order $l \leq l_c$, spherical order characterizing convection
(corresponds to the pressure scale-height)



Evaluation of the **damping factor** τ for a frequency of $1\mu\text{Hz}$ in a solar model.

The depth corresponding to an attenuation by a factor $1/e$ is shown for various degrees ℓ

Local momentum luminosity integrated over the whole spectrum :

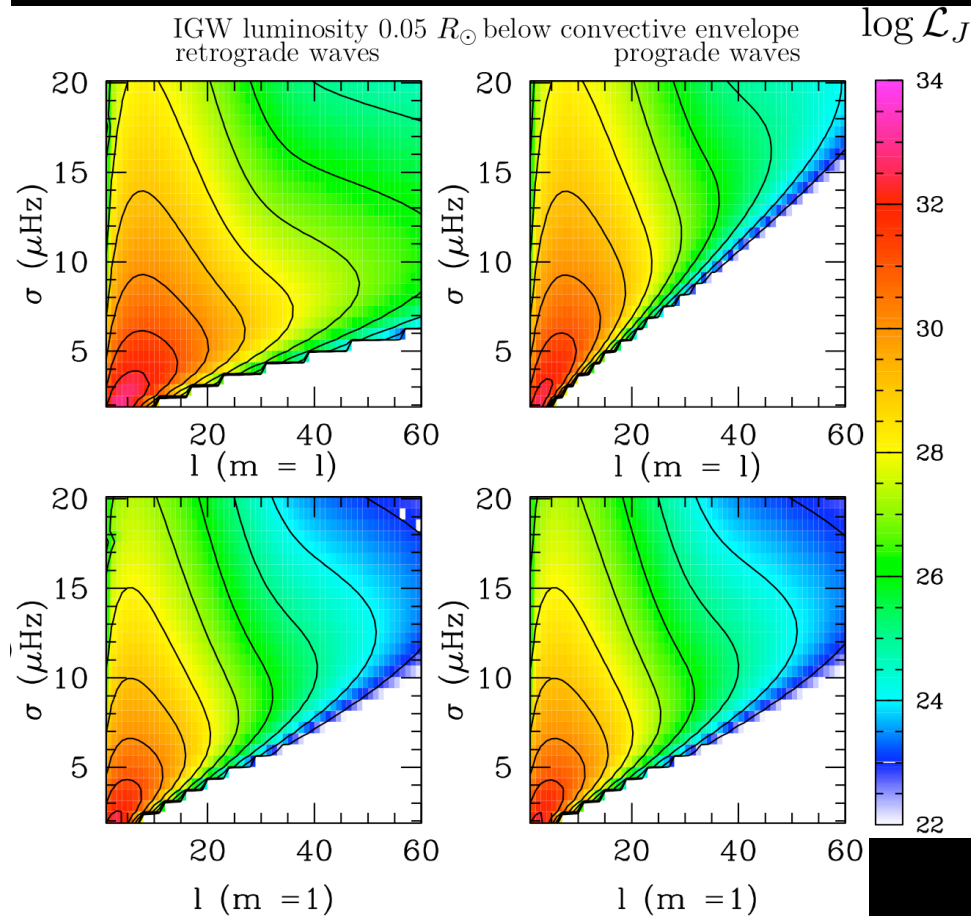
$$\mathcal{L}_J(r) = \sum_{\sigma, \ell, m} \underbrace{\mathcal{L}_{J\ell, m}(r_{cz})}_{\propto F_{\text{conv}}} \exp[-\tau(r, \sigma, \ell)]$$

$$\tau(r, \sigma, \ell) = [\ell(\ell+1)]^{\frac{3}{2}} \underbrace{\int_r^{r_c} (K_T + \nu_v)}_{\text{Integrated damping due to thermal diffusion } K_T \text{ and turbulent viscosity } \nu_t} \frac{NN_T^2}{\sigma^4} \left(\frac{N^2}{N^2 - \sigma^2} \right)^{\frac{1}{2}} \frac{dr}{r^3}$$

Integrated damping due to thermal diffusion K_T and turbulent viscosity ν_t

σ : local frequency

$N^2 = N_T^2 + N^2$: Brunt-Väisälä frequency



Local momentum luminosity integrated
over the whole spectrum :

$$\mathcal{L}_J(r) = \sum_{\sigma, \ell, m} \underbrace{\mathcal{L}_{J\ell, m}(r_{cz})}_{\propto F_{\text{conv}}} \exp[-\tau(r, \sigma, \ell)]$$

$$\tau(r, \sigma, \ell) = [\ell(\ell + 1)]^{\frac{3}{2}} \underbrace{\int_r^{r_c} (K_T + \nu_v)}_{\text{Integrated damping due to thermal diffusion } K_T \text{ and turbulent viscosity } \nu_t} \frac{NN_T^2}{\sigma^4} \left(\frac{N^2}{N^2 - \sigma^2} \right)^{\frac{1}{2}} \frac{dr}{r^3}$$

Integrated damping due to thermal diffusion K_T and turbulent viscosity ν_t

σ : local frequency

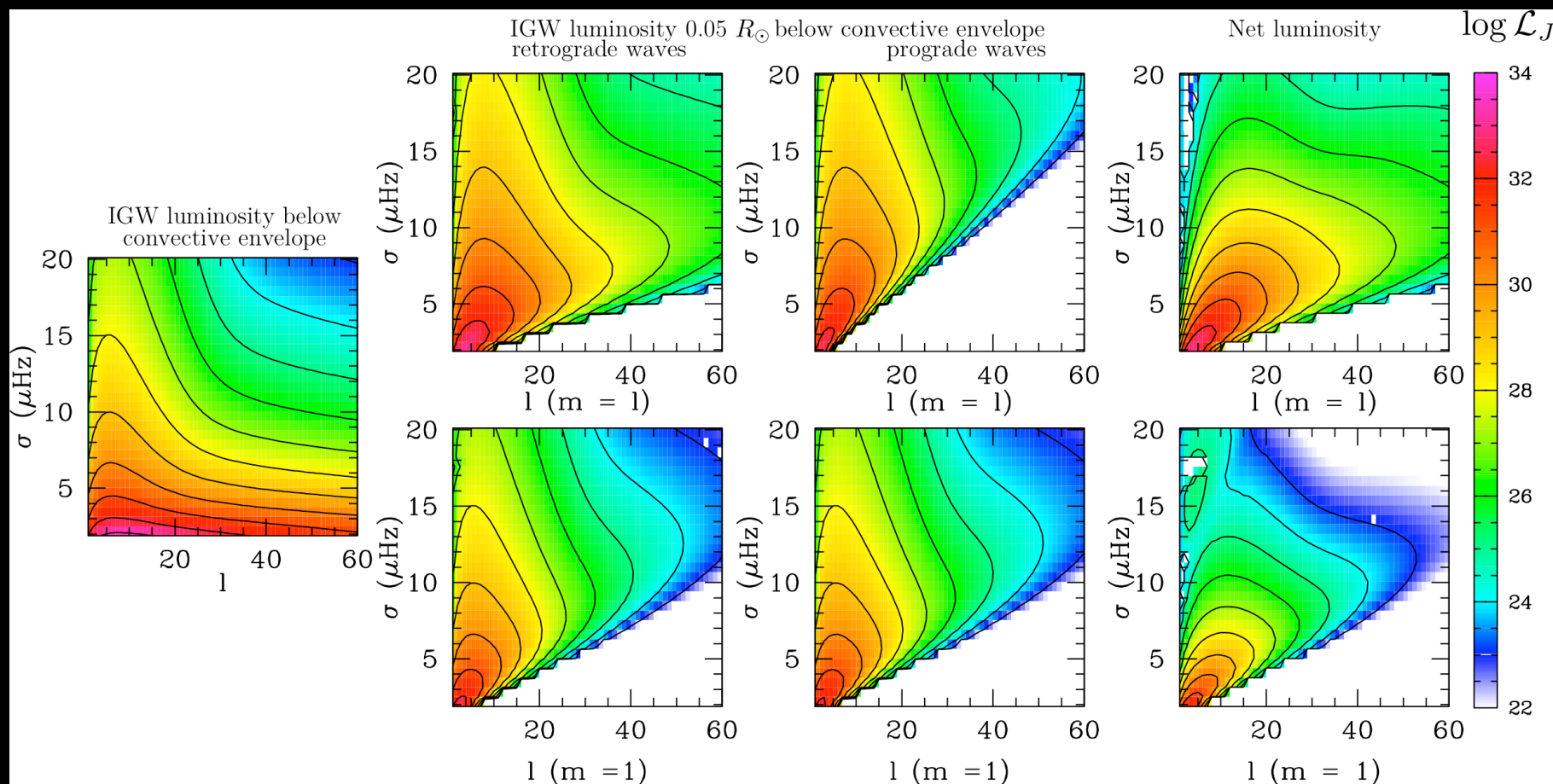
$N^2 = N_T^2 + N^2$: Brunt-Väisälä frequency

**Wave spectrum of angular momentum
luminosity at $0.05 R$ below the convective
envelope - $1.1M_\odot$, Z_\odot at 180 Myrs**

Mathis, Decressin, Eggenberger & Charbonnel (in prep.)

following Talon, Kumar & Zahn (02), Kumar & Quataert (97), Talon & Charbonnel (03, 04, 05)

Spectrum of IGW luminosity generated by Reynolds stress - $1.1M_{\odot}$ at 180 Myrs



- ✓ Most of the momentum is carried by low-frequency waves
- ✓ Significant momentum luminosity in low-order waves that penetrate deep into the interior

Mathis, Decressin, Eggenberger & Charbonnel (in prep.)

following Talon, Kumar & Zahn (02), Kumar & Quataert (97), Talon & Charbonnel (03, 04, 05)

$\mathbf{L_J}$: Net momentum luminosity
 at $0.03R_*$ below the surface convection zone
 as a function of T_{eff} (zams) for Pop I stars
 \Leftrightarrow Momentum extraction in the stellar interior

Local momentum luminosity integrated
 over the whole spectrum :

$$\mathcal{L}_J(r) = \sum_{\sigma, \ell, m} \mathcal{L}_{J\ell, m}(r_{\text{cz}}) \exp[-\tau(r, \sigma, \ell)]$$

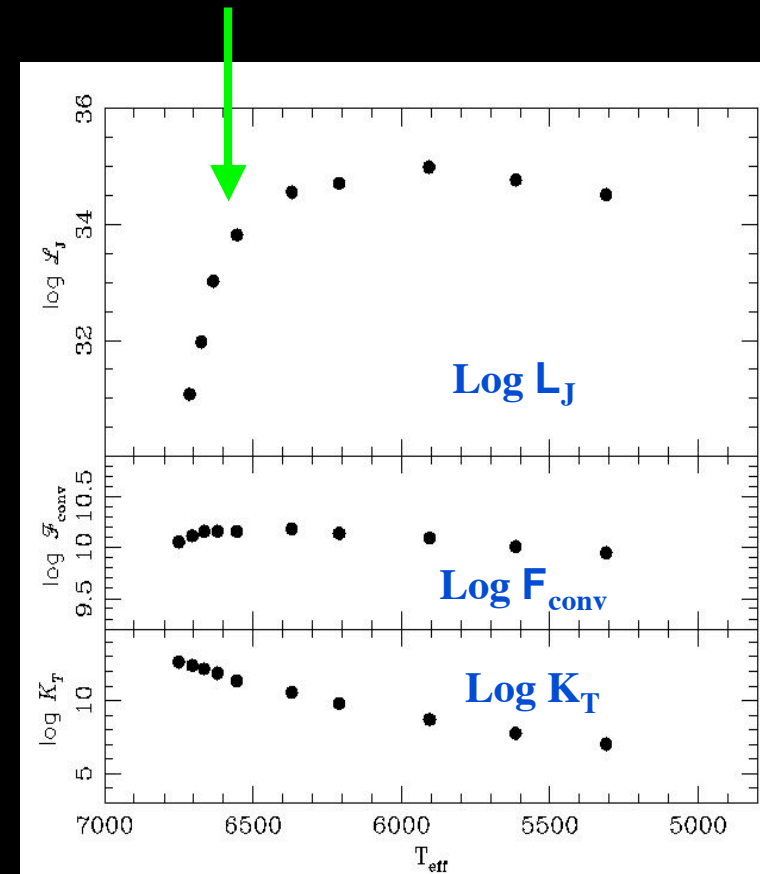
Momentum transport by IGW
 has the proper mass dependence
 Local amplitude :
 to be the required process

$$\tau(r, \sigma, \ell) = [\ell(\ell+1)]^{\frac{3}{2}} \int_r^{r_c} (K_T + \nu_v) \frac{NN_T^2}{\sigma^4} \left(\frac{N^2}{N^2 - \sigma^2} \right)^{\frac{1}{2}} \frac{dr}{r^3}$$

Integrated damping due to thermal diffusion K_T and turbulent viscosity ν_t

σ : local frequency

$N^2 = N_T^2 + N^2$: Brunt-Väisälä frequency



Talon & Charbonnel (03, 04)

Complete evolution models including rotation, gravity waves and atomic diffusion

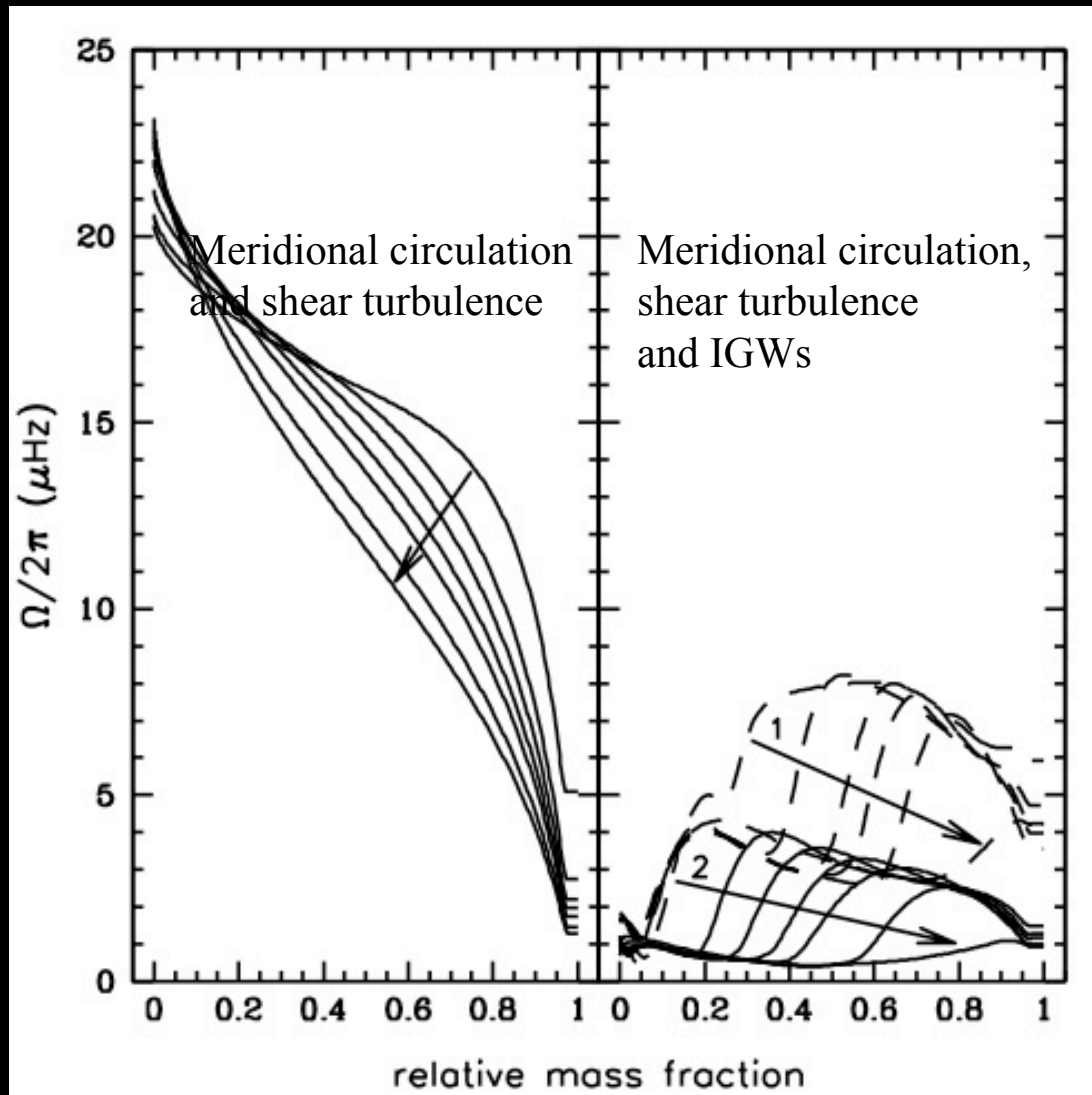
Transport of angular momentum :

$$\underbrace{\frac{d}{dt}}_{\text{Contraction or expansion}} [r^2 \Omega] = \underbrace{\frac{1}{5r^2} \frac{\partial}{\partial r} [r^4 \Omega U_2]}_{\text{Advection (MC)}} + \underbrace{\frac{1}{r^2} \frac{\partial}{\partial r} v r^4 \frac{\partial \Omega}{\partial r}}_{\text{Diffusion (shear)}} - \underbrace{\frac{3}{8\pi} \frac{1}{r^2} \frac{\partial \mathcal{L}_j(r)}{\partial r}}_{\text{IGW}}$$

Local momentum luminosity
is obtained by calculating the damping integral for each individual waves
and then summing over all waves

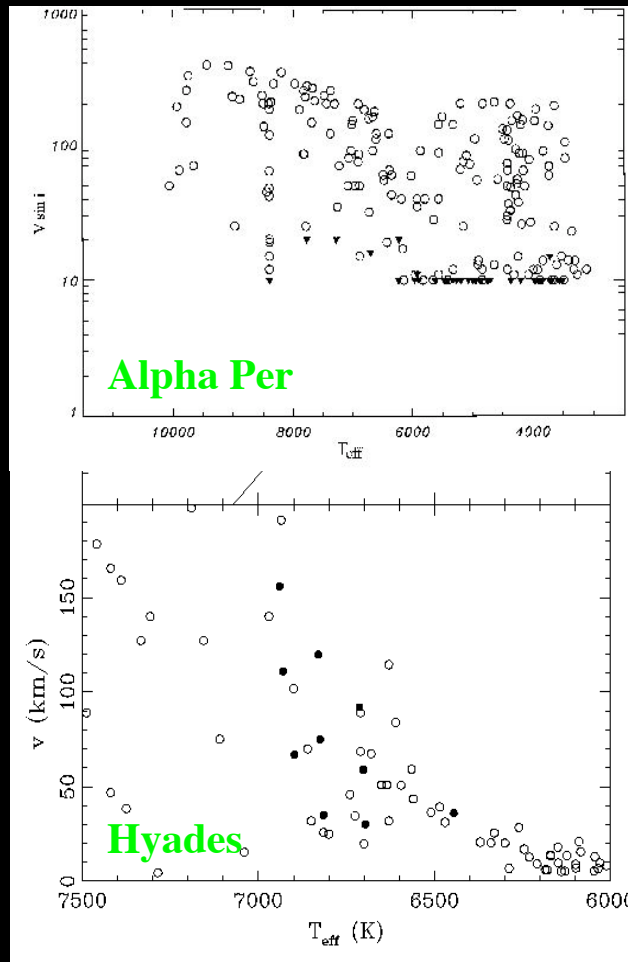


Rotation profile inside a $1.0 M_{\odot}$, $Z=0.02$ star

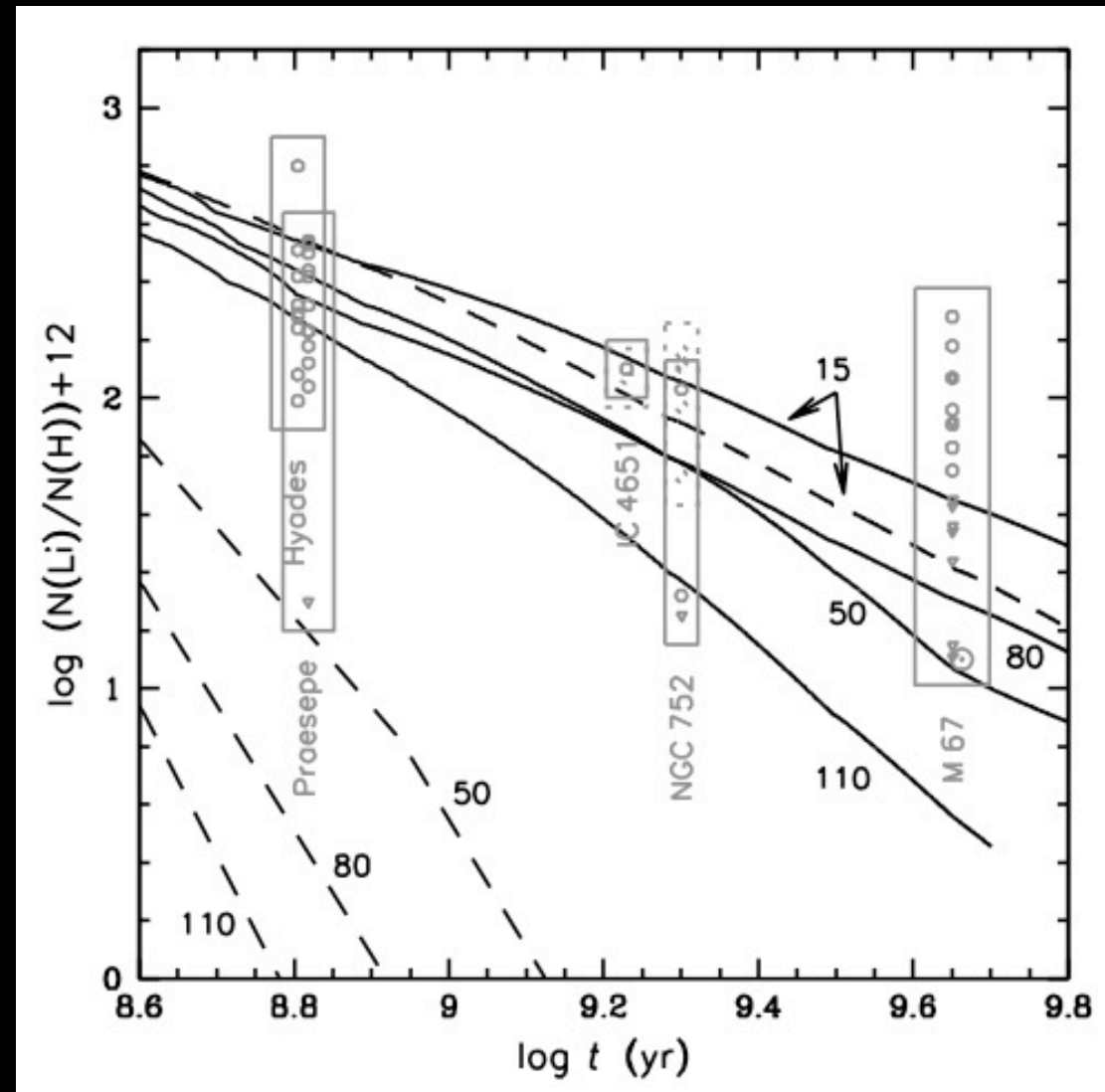


Identical magnetic braking applied
 $V_i = 50 \text{ km s}^{-1}$

$1M_{\odot}, Z=0.02$



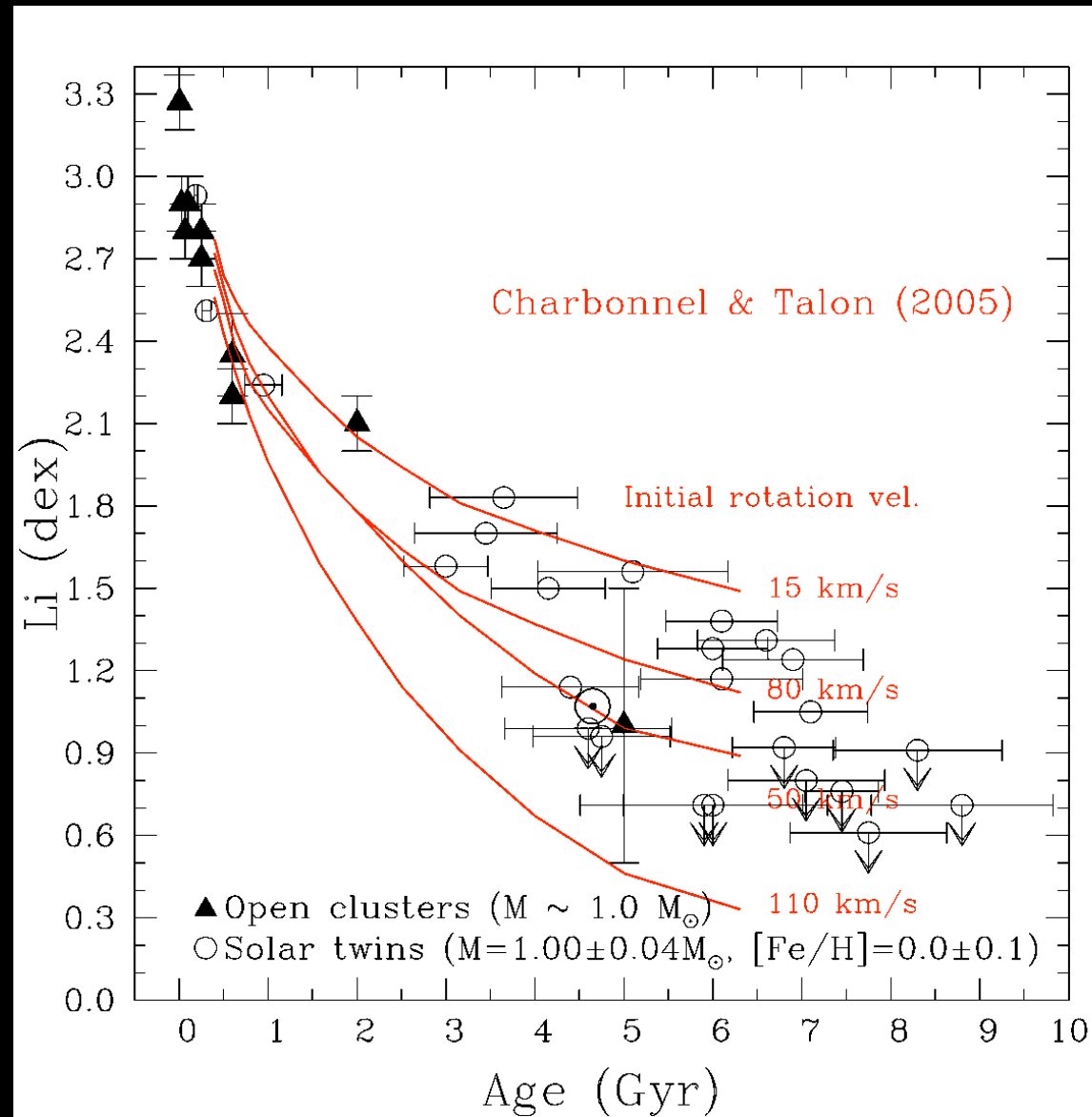
Magnetic braking applied
with Kawaler (1988) formulation



--- MC and shear turbulence
— MC, shear and IGWs

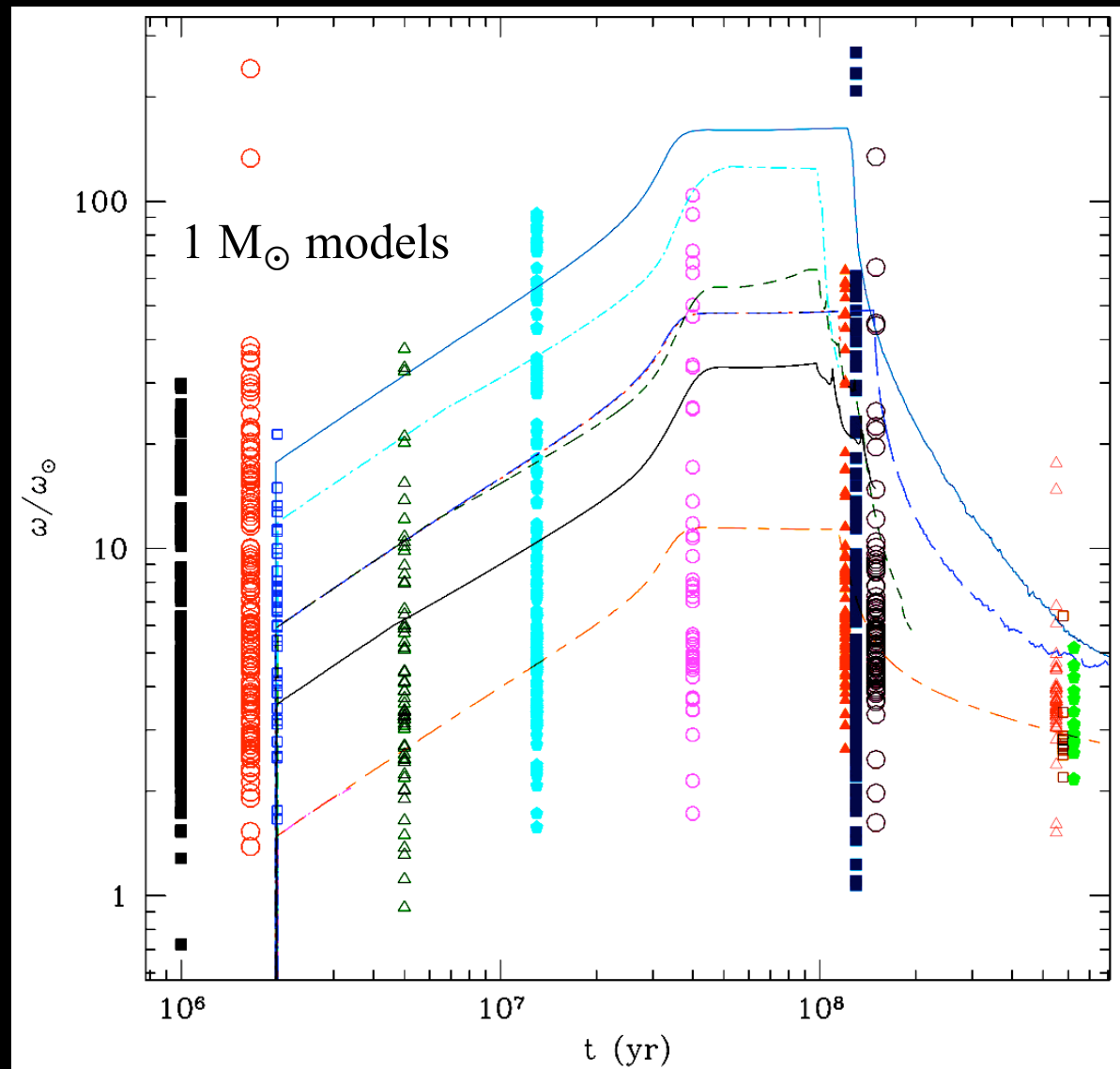
Charbonnel & Talon (05)

$1M_{\odot}, Z=0.02$



Melendez et al. (09)

Pre-main sequence

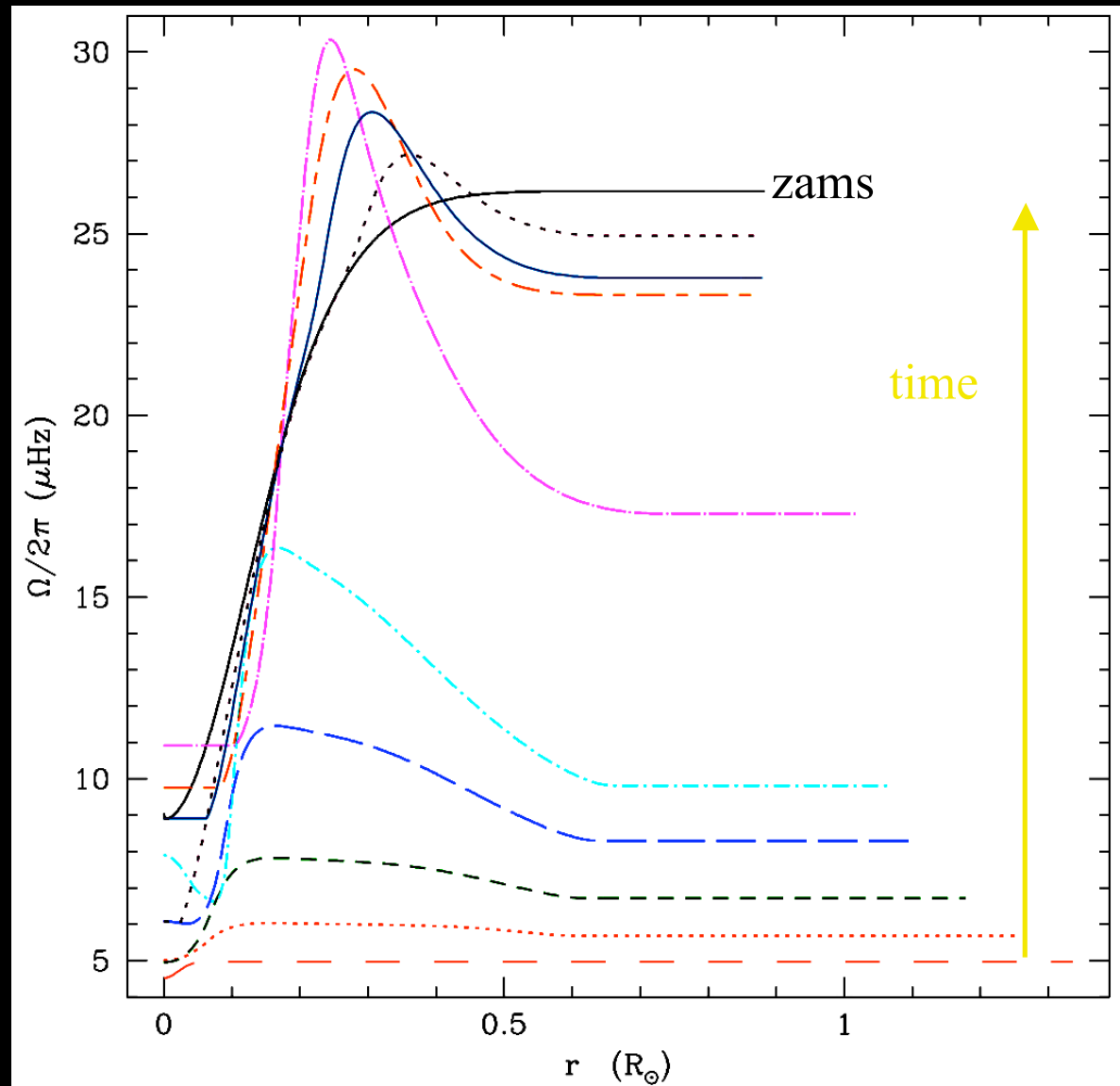


Data: Rotational periods in young open clusters ($0.9 - 1.1 M_{\odot}$)
Gallet & Bouvier (in prep)

Charbonnel, Decressin & Talon (in prep.)

Pre-main sequence

$1M_{\odot}$
 $V_i = 20 \text{ km/sec}$
 $\text{Prot}_i = 5 \text{ d}$
 $V_{\text{zams}} = 102 \text{ km/sec}$

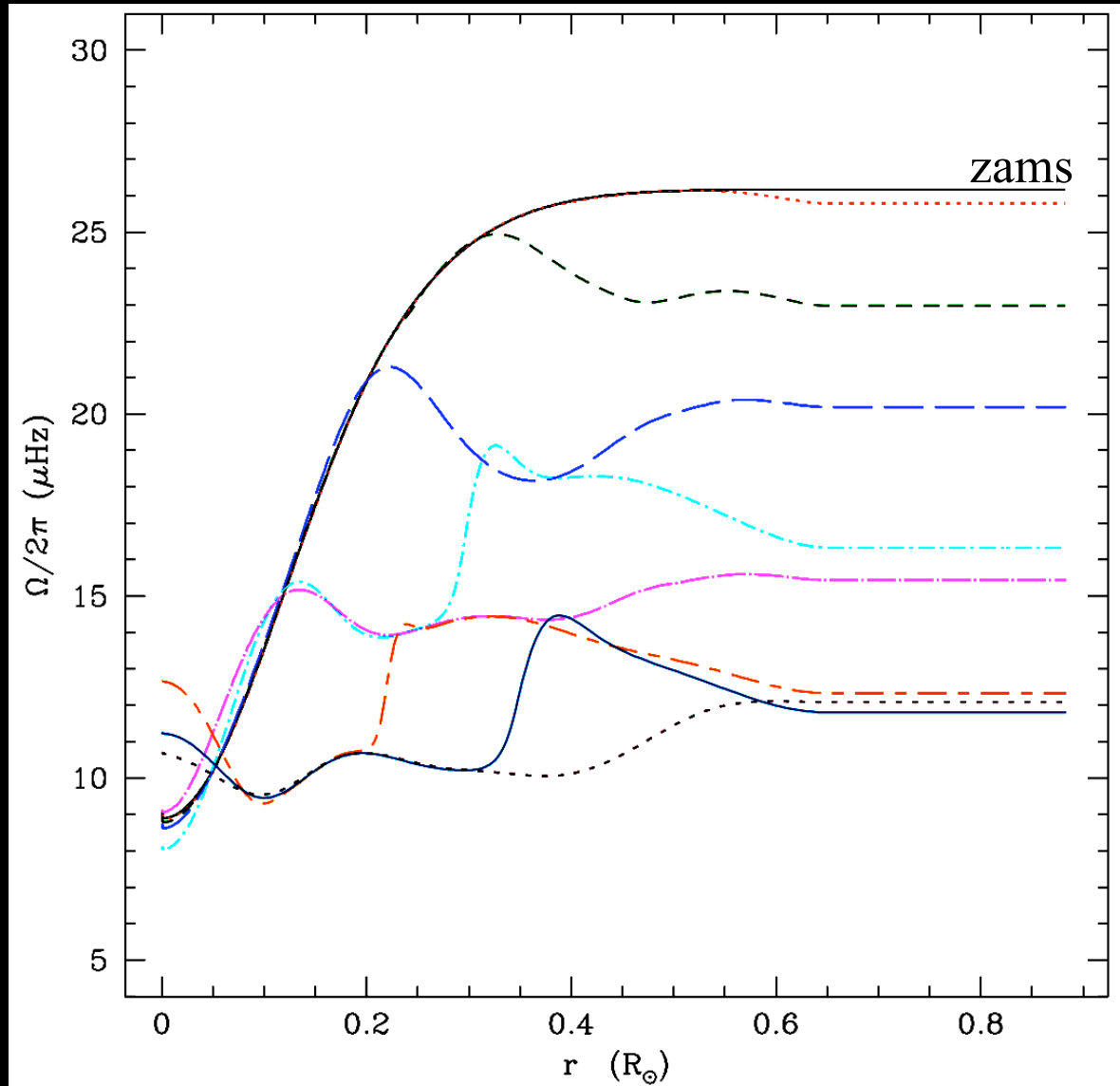


6.2, 8, 11, 16, 22, 36, 51, 65, 80, 98 Myr

Charbonnel, Decressin & Talon (in prep.)

Main sequence

$1M_{\odot}$
 $V_i = 20$ km/sec
 $\text{Prot}_i = 5$ d
 $V_{\text{zams}} = 102$ km/sec

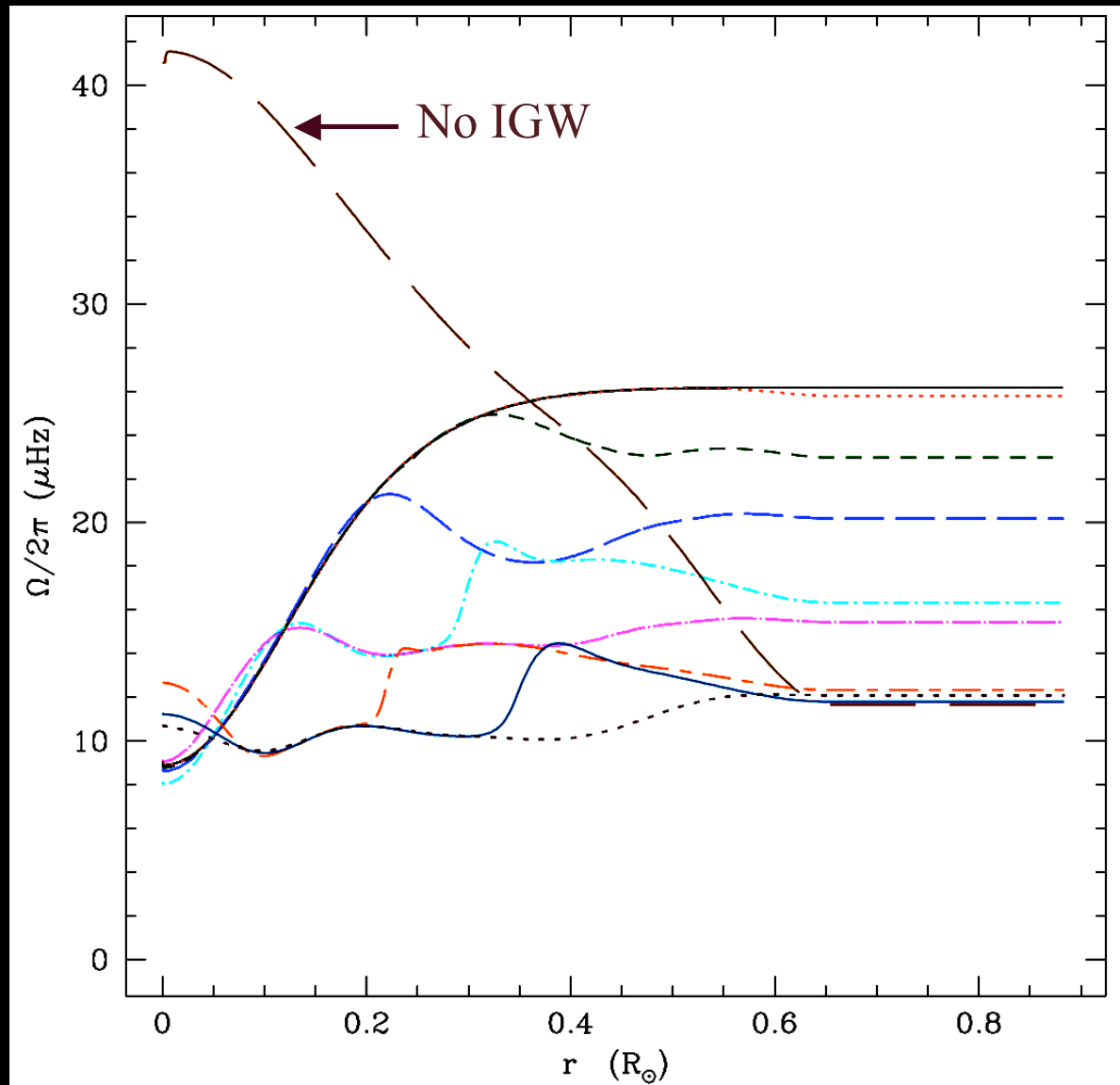


98, 100, 105, 110, 115, 120, 125, 130 Myr

Charbonnel, Decressin & Talon (in prep.)

Main sequence

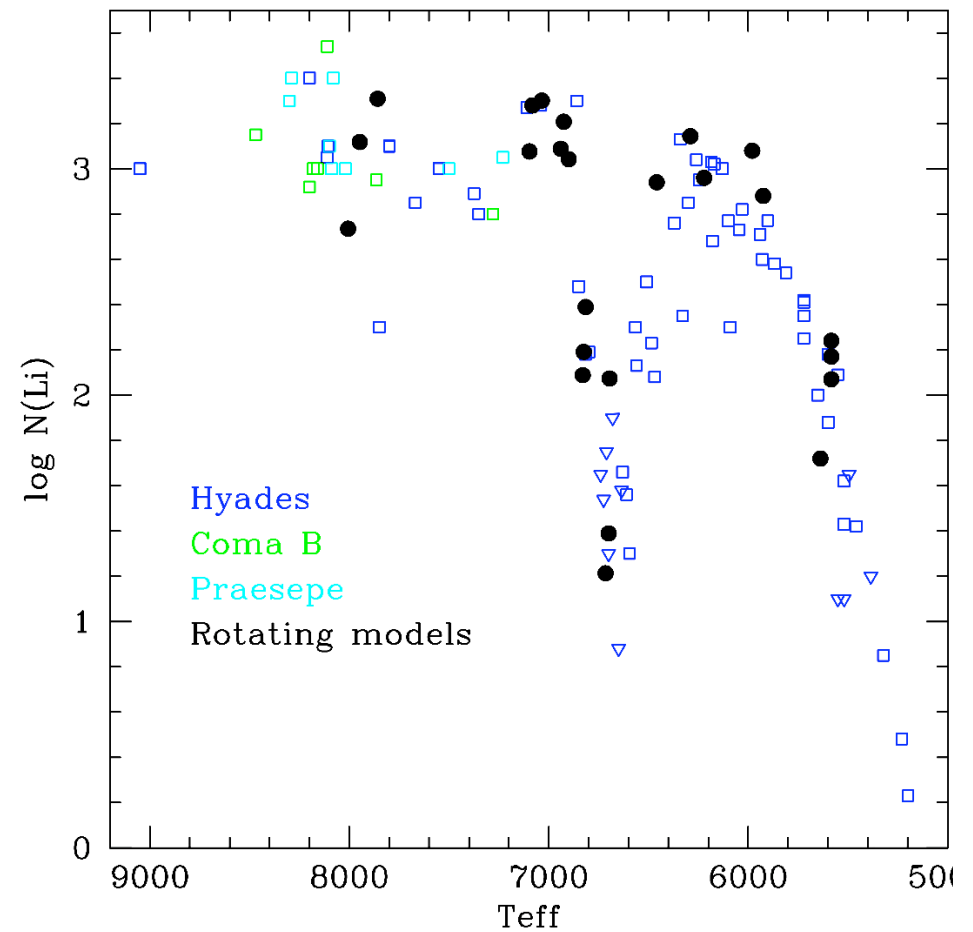
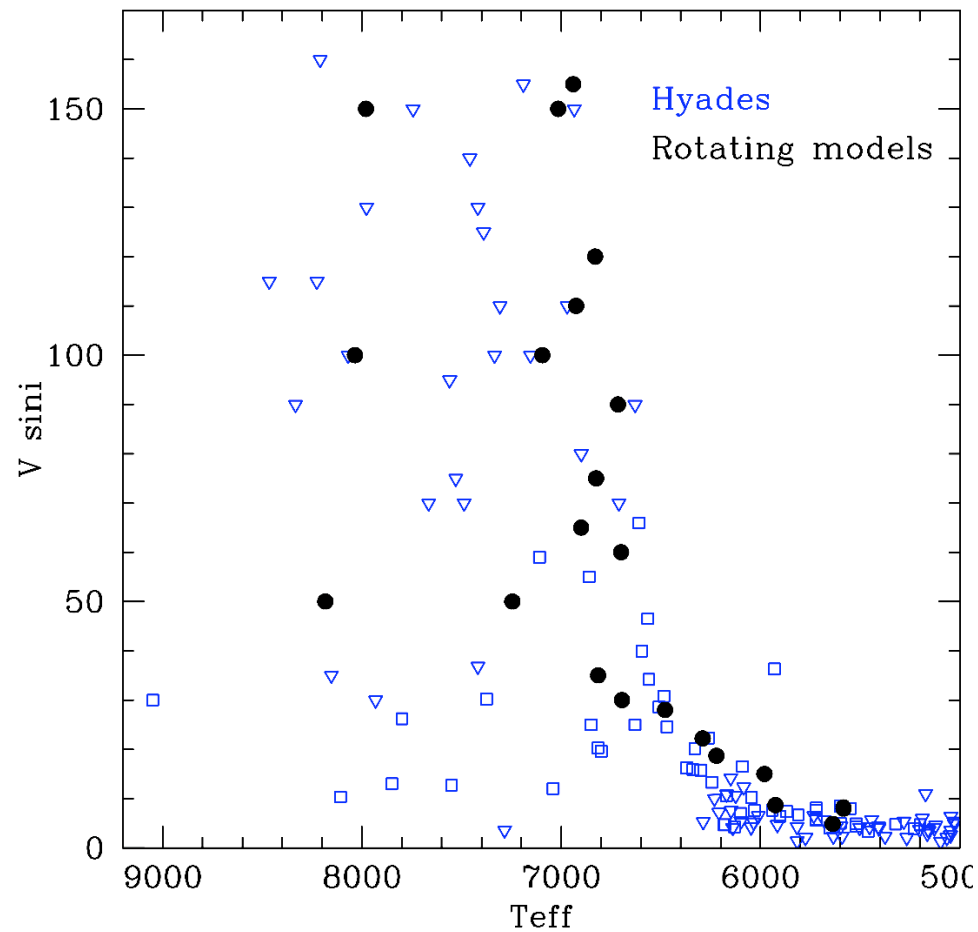
$1M_{\odot}$
 $V_i = 20 \text{ km/sec}$
 $\text{Prot}_i = 5 \text{ d}$
 $V_{\text{zams}} = 102 \text{ km/sec}$



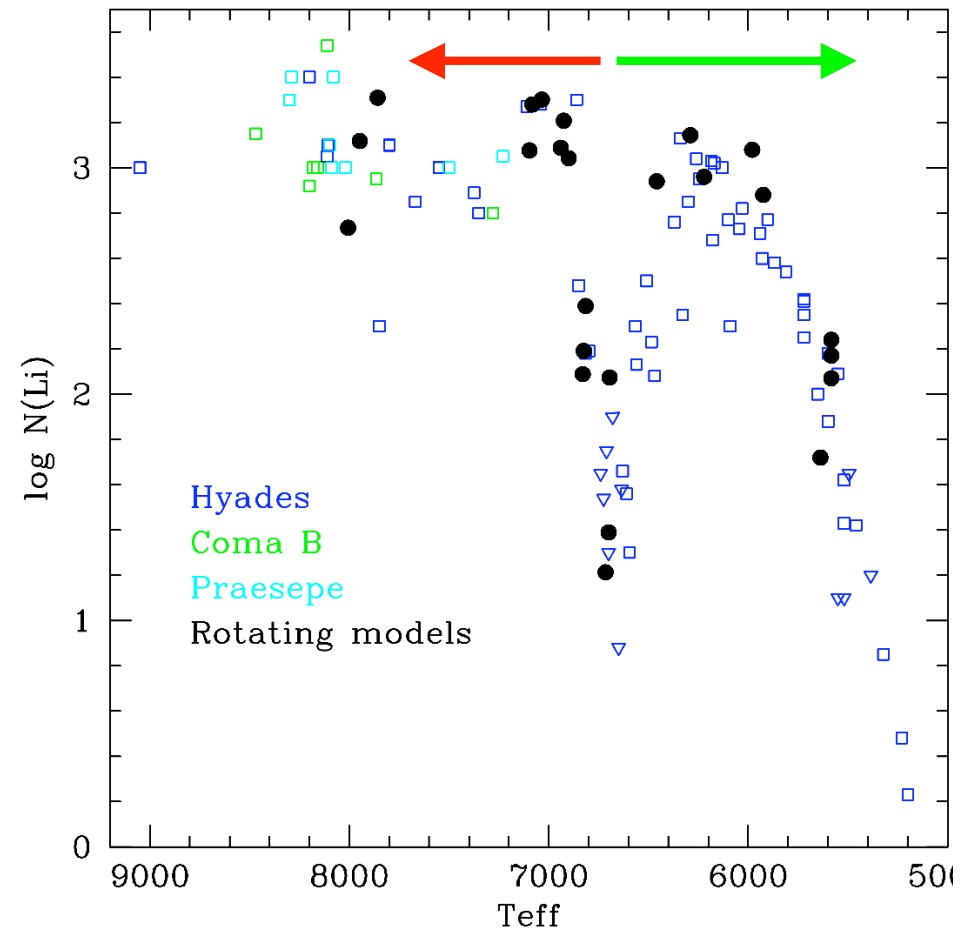
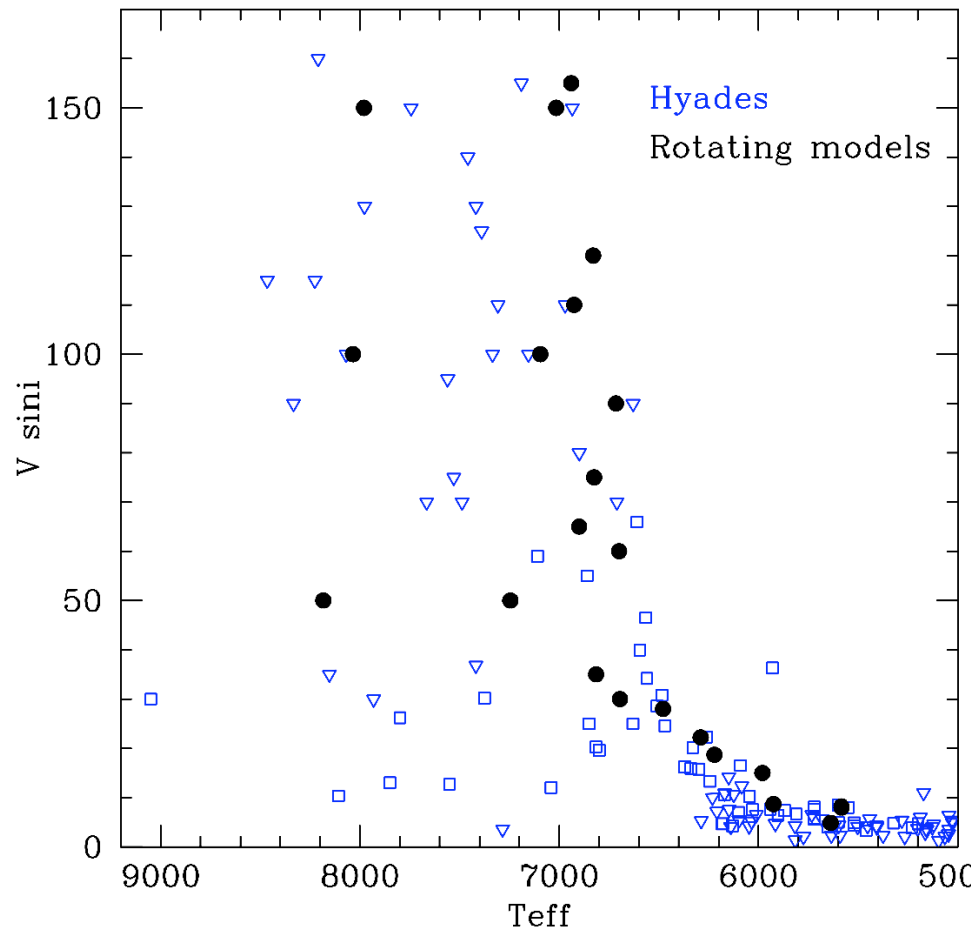
9.8e7, 1e8, 1.05e8, 1.1e8, 1.15e8, 1.2e8, 1.25e8, 1.3e8

Charbonnel, Decressin & Talon (in prep.)

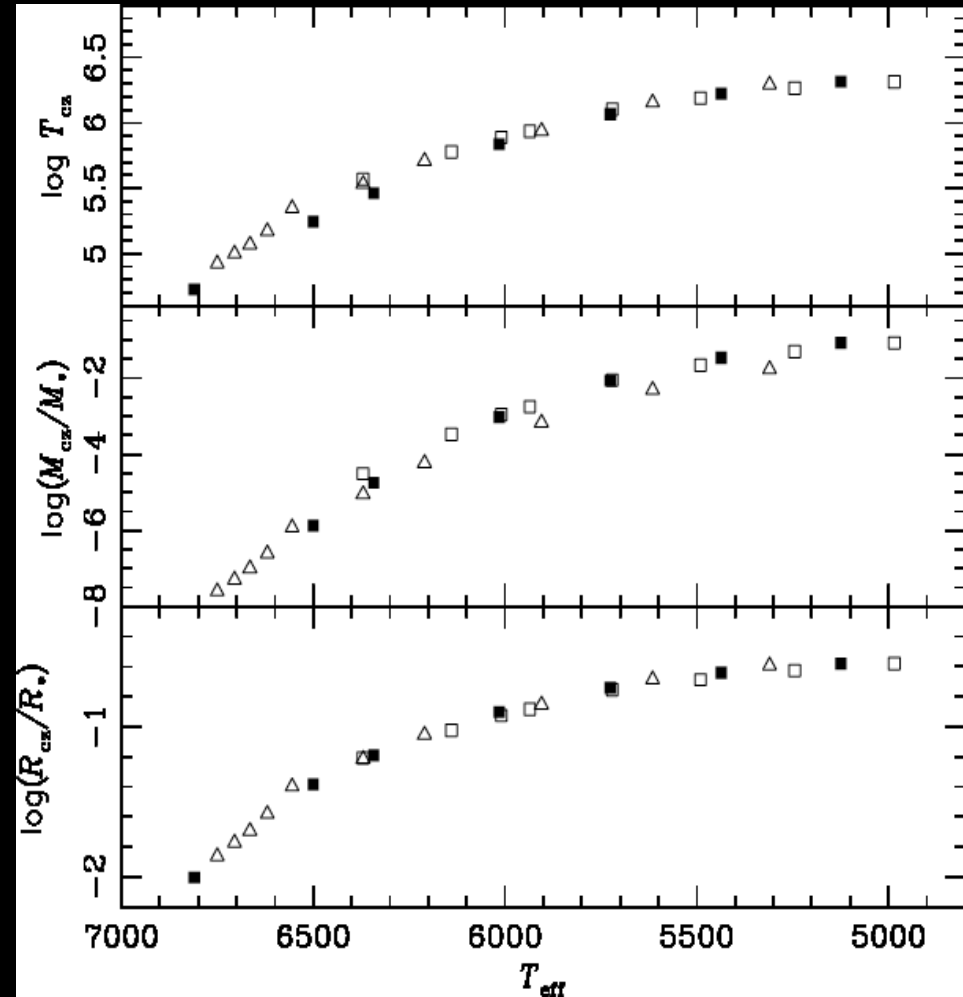
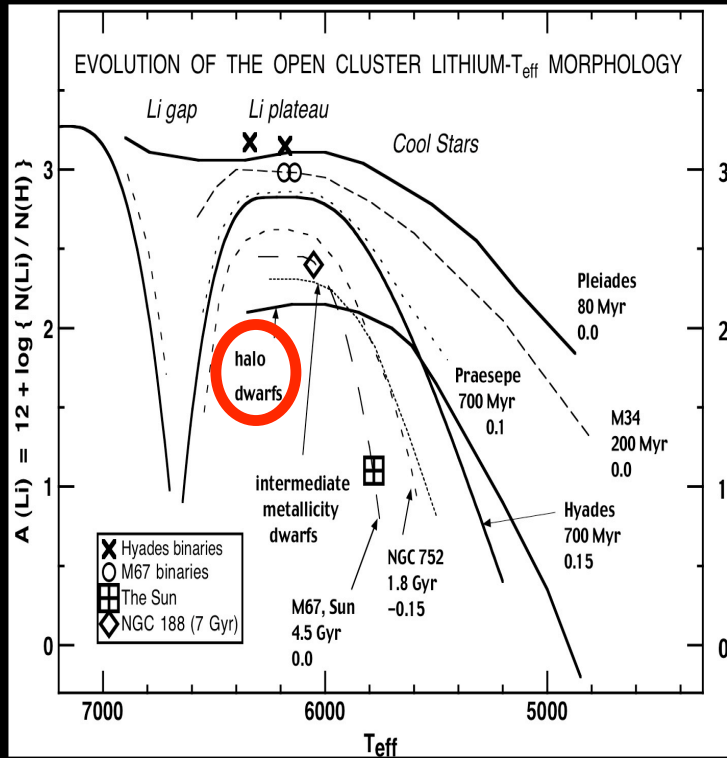
Bridging the gap



Transport of angular momentum dominated by
Circulation and turbulence in massive stars down to the Li dip
Internal gravity waves in low mass stars with deeper convective envelopes

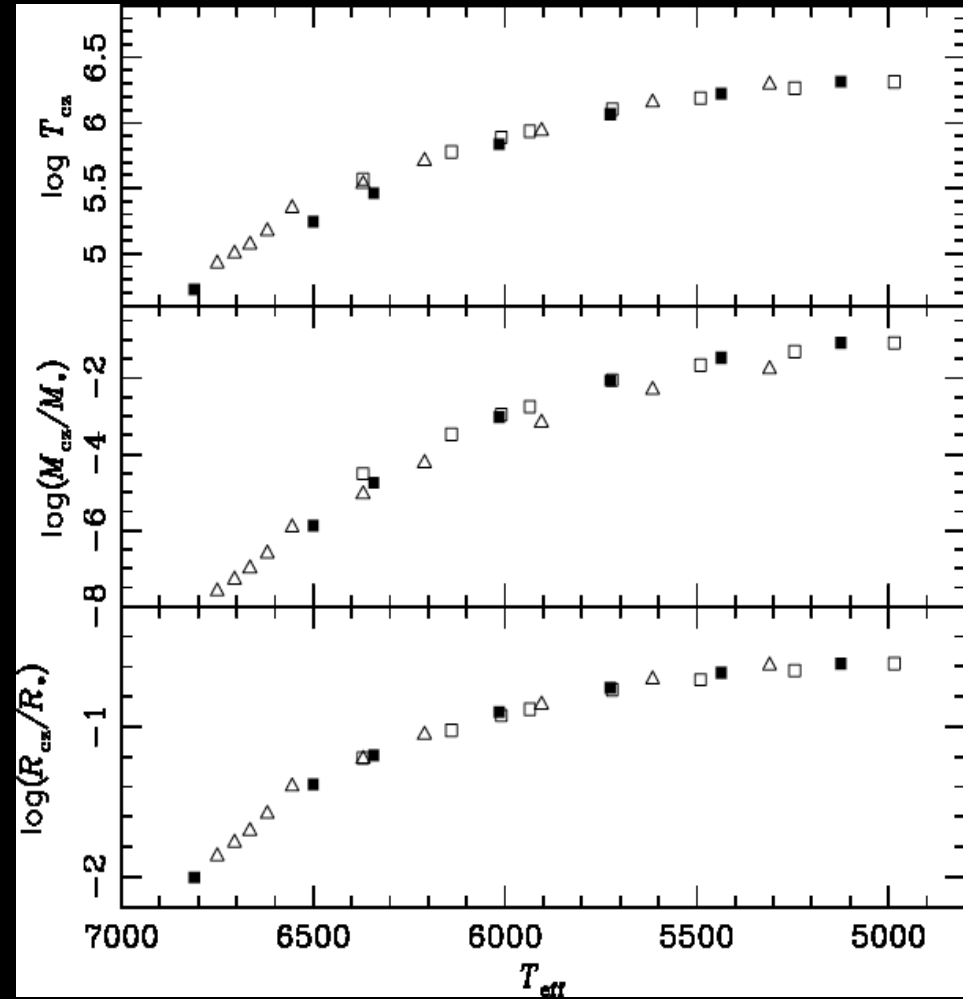
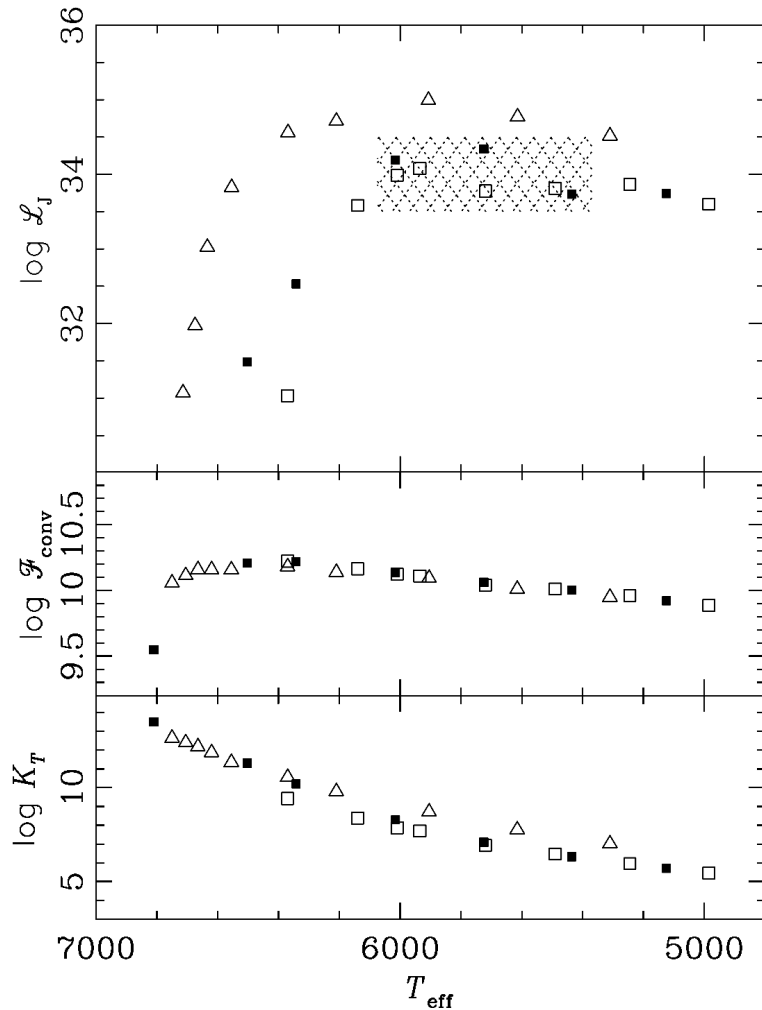


Pop II stars



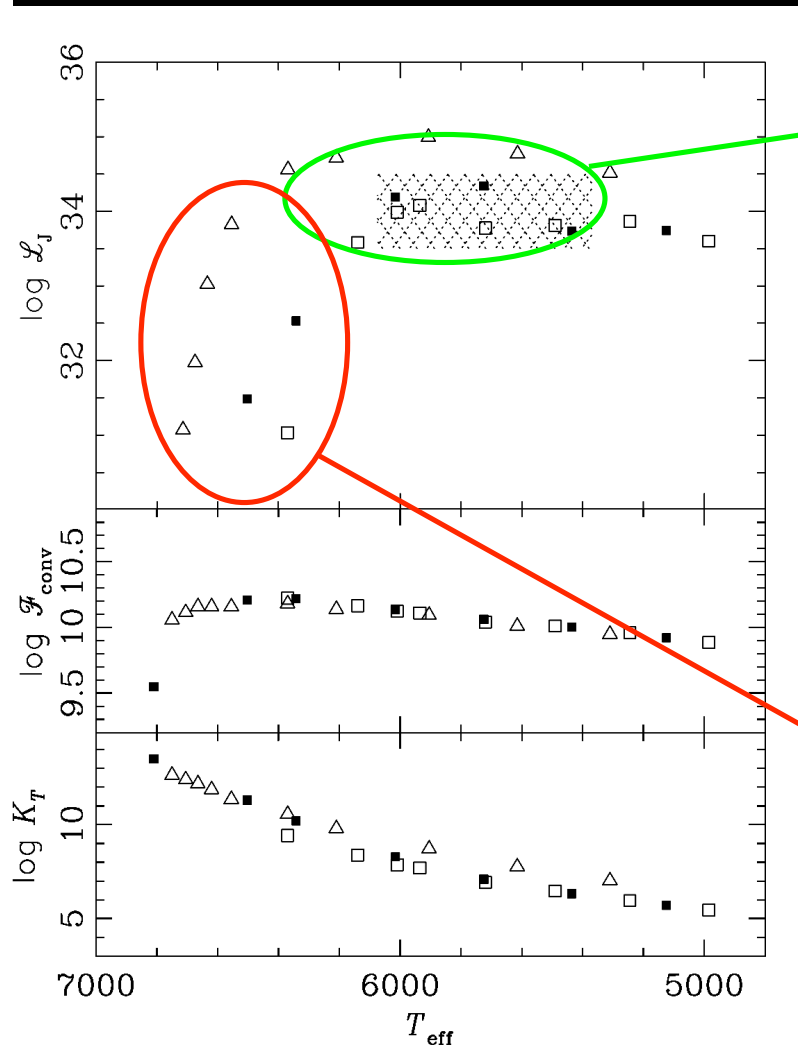
Open squares : Pop II stars ($[\text{Fe}/\text{H}]=-2$) on the zams
 Black squares : Pop II stars ($[\text{Fe}/\text{H}]=-2$) at 10 Gyr
 Open triangles : Pop I stars on the zams

Pop II stars



Open squares : Pop II stars ($[\text{Fe}/\text{H}]=-2$) on the zams
 Black squares : Pop II stars ($[\text{Fe}/\text{H}]=-2$) at 10 Gyr
 Open triangles : Pop I stars on the zams

Pop II stars



Dwarf stars lying on the Spite plateau
 \Leftrightarrow IGWs dominate the transport of
angular momentum

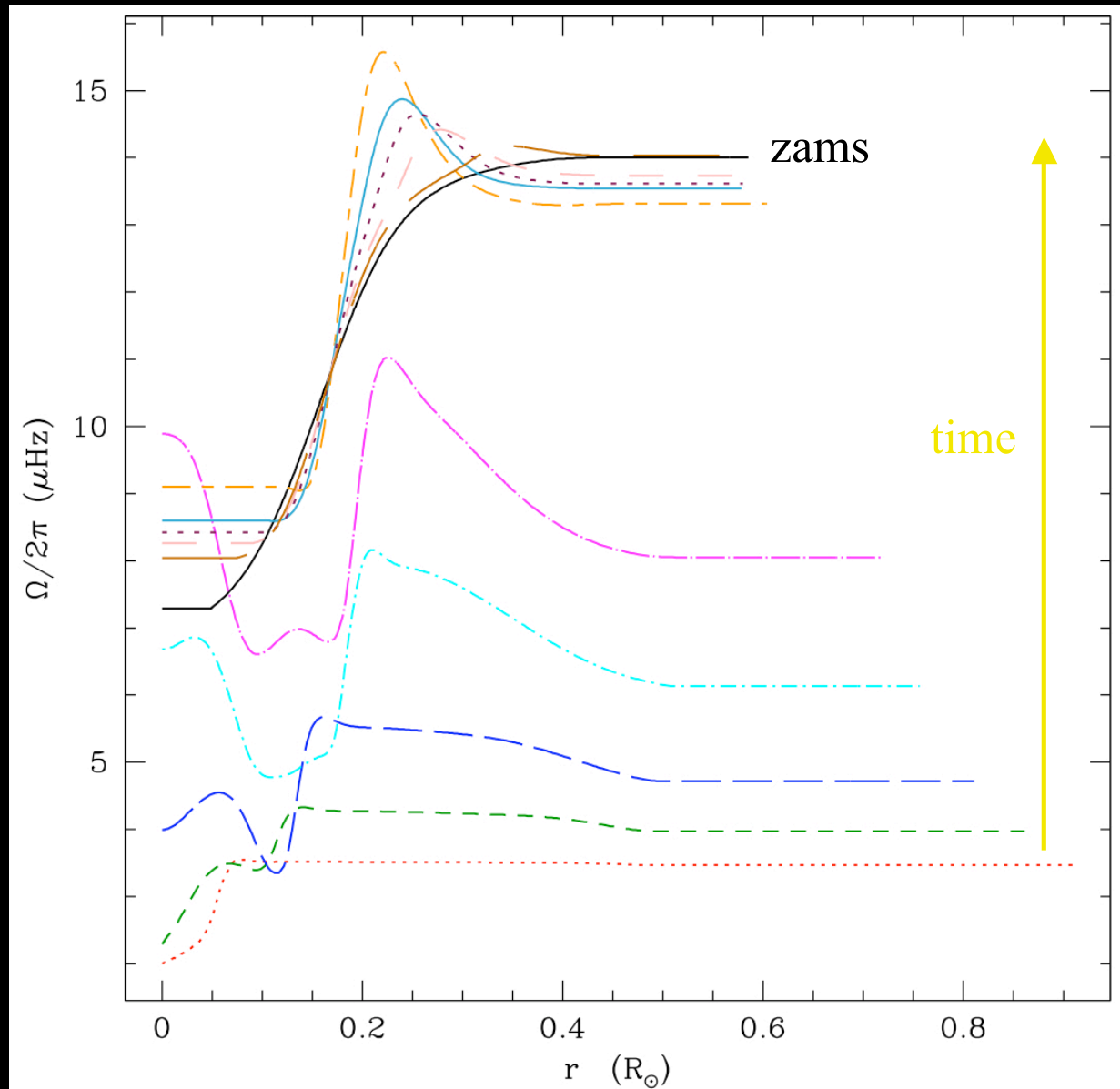
- Solid body rotators
- Decrease of the surface Li abundance
but very little Li dispersion

Slightly more massive stars

- Large internal differential rotation
- More Li dispersion (Charbonnel & Primas 05)
- High $V \sin i$ observed on the horizontal branch

Pre-main sequence

$0.7 M_{\odot}$, $[\text{Fe}/\text{H}] = -2$
 $V_i = 10 \text{ km/sec}$
 $V_{\text{zams}} = 30 \text{ km/sec}$

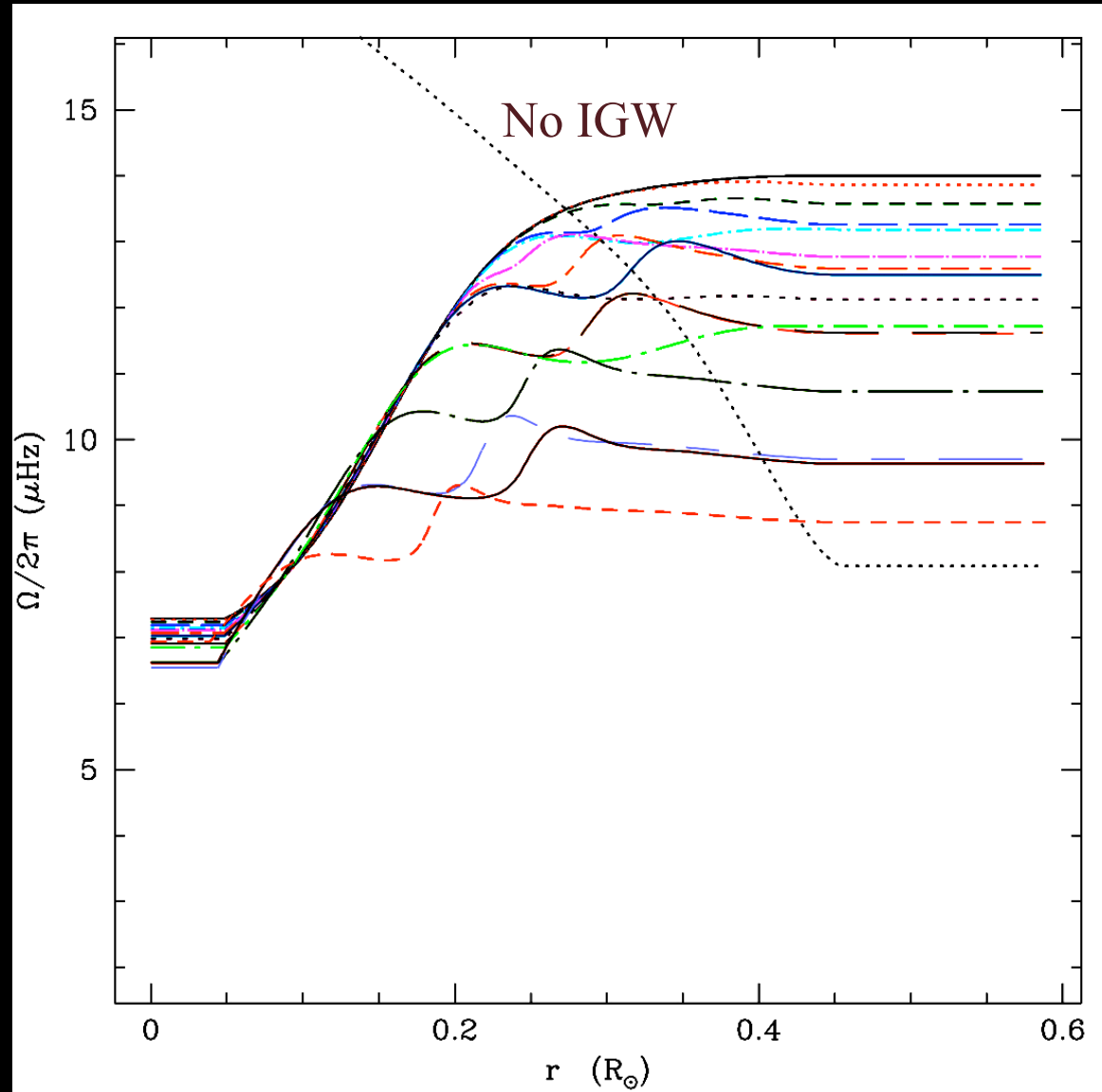


6.2, 8, 11, 16.5, 22, 36, 51, 654, 80, 98, 125, 159 Myrs

Charbonnel, Decressin & Talon (in prep.)

Main sequence

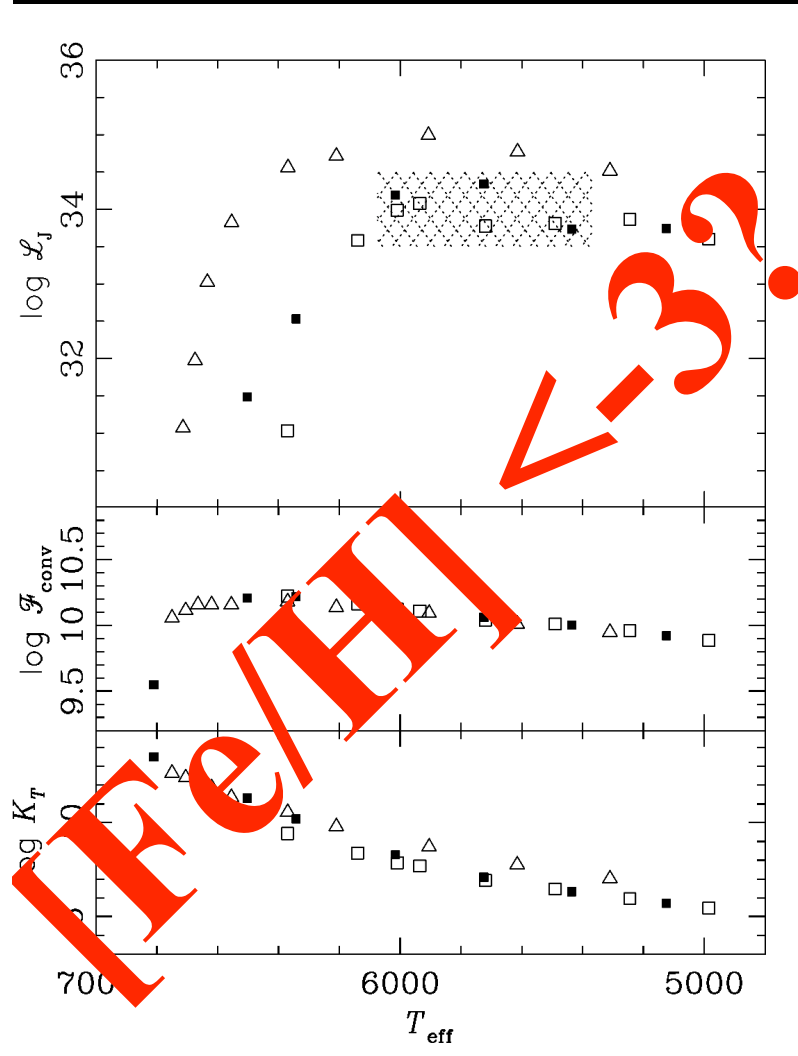
$0.7 M_{\odot}$, $[\text{Fe}/\text{H}] = -2$
 $V_i = 10 \text{ km/sec}$
 $V_{\text{zams}} = 30 \text{ km/sec}$



159, 161, 165, 170, 175, 180, 185, 190, 200, 216, 225, 250, 300, 308, 360 Myrs

Charbonnel, Decressin & Talon (in prep.)

Pop II stars at very low metallicity



Dwarf stars lying on the Spite plateau at low Z ($[\text{Fe}/\text{H}] < -3$)

\Leftrightarrow Do IGWs still dominate the transport of angular momentum ?

- \rightarrow If not, then they would behave like Pop I stars of the left side of the Li dip
i.e., Li depletion depends on angular momentum extraction
- \rightarrow Li dispersion should then reflect dispersion in initial rotation velocity

Stay tuned!

Open squares : Pop II stars ($[\text{Fe}/\text{H}] = -2$) on the zams

Black squares : Pop II stars ($[\text{Fe}/\text{H}] = -2$) at 10 Gyr

Open triangles : Pop I stars on the zams