

# Merger Influence on the Thermal SZ Effect

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1. Model and characteristics: - integrated pressure  
- spectral function  
(transonic merger)
2. An application: maps for subsonic mergers

# Why look at mergers?

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- increasing observational evidence from X-rays:
  - dimension:  $r \sim 10\text{-}600$  kpc
  - Mach number: 0.4 – 2.5
  - (early stage/late stage, subsonic/transonic)
- source of non-thermal physics (spectral fct.)
- reveal the cluster substructure
- information on structure formation

# Why look at mergers with SZ?

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- compare with X-rays, provide an (independent) tool (in particular for high  $z$ )
- observe mergers which are not seen in X-rays (position and direction of motion), possibly extract parameters from a simple model
- investigate (high  $z$ ) substructure
- source of error for parameters based on SZ flux, e.g.  $H_0$

# MODEL: framework

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- focus on (common) minor mergers
  - ☆ DM profile not changed  
(major mergers excluded)
- $r_{\text{sub}} \leq 0.6 r_1$ ,  $M_{\text{sub}} \leq 10\text{-}20\% M_{\text{cl}}$
- simple gas dynamics: gas spread around subcluster, redistribution maintaining  $\beta$ -profile
  
- ☆ goal: build a model with characteristic merger features

# Model and characteristics: subsonic

$$\Delta I(x) \propto g(x) \int_{cl} \left( \frac{k_B T_g}{m_e c^2} \right) \sigma_T n_e dl_{cl}$$

**Subsonic:**

- $\sim$  incompressible, but  $P_{ex}$
- Moving body through gas
- No shock waves  $\nabla g(x)$  unchanged

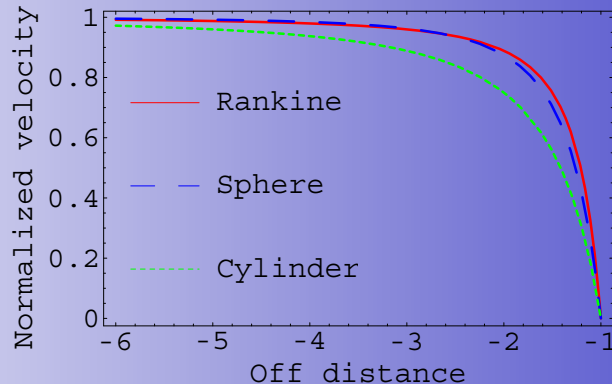
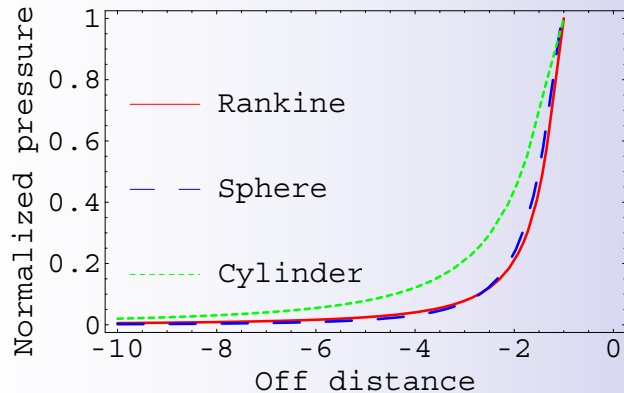
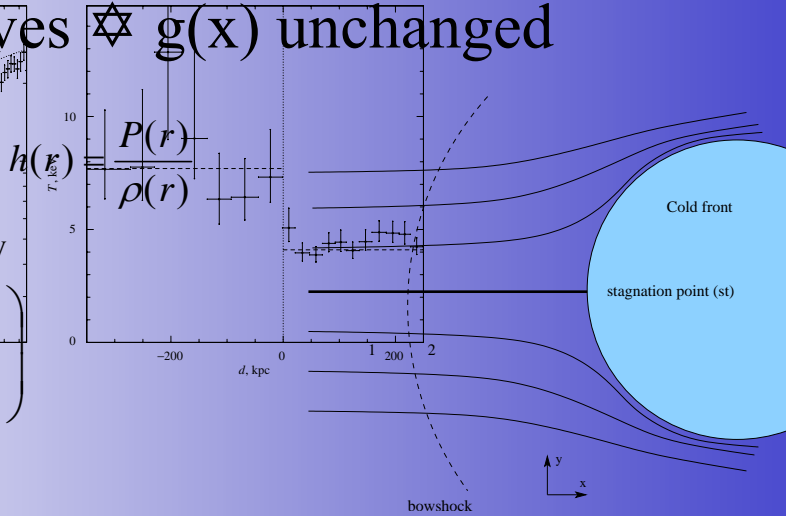
Bernoulli eq.  $h(r) + \frac{1}{2} v^2(r) + \phi(r) = const.$

$S_v, \text{ erg s}^{-1} \text{ cm}^{-2} \text{ km}^{-2}$

Potential flow theory

(Stagnation point l.o.s)

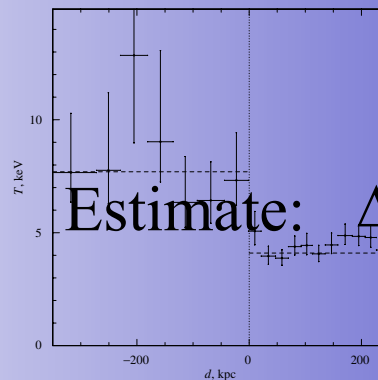
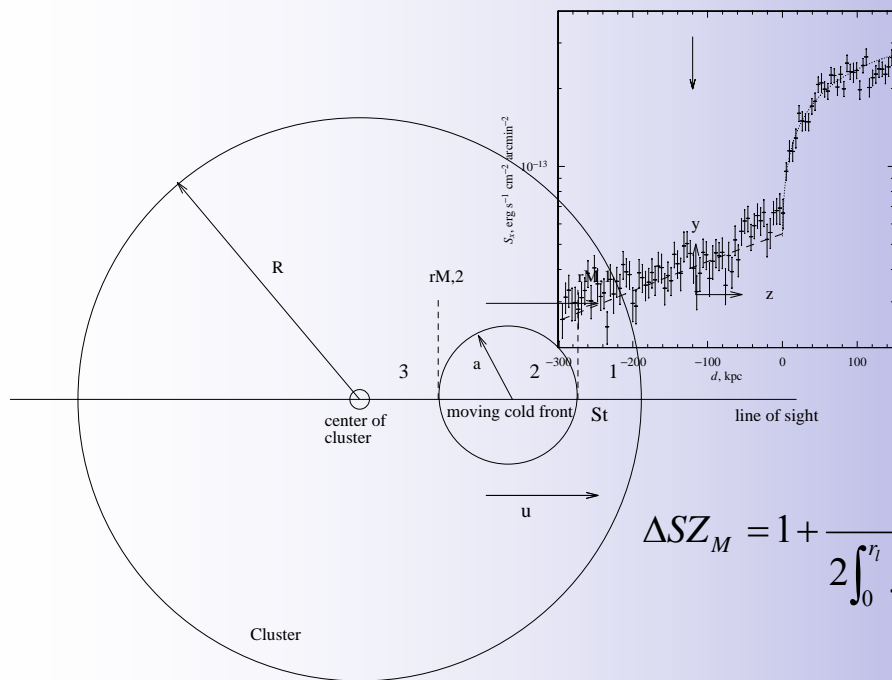
$$P_{ex}(r) \propto \rho_{gas} \frac{1}{2} \left( 1 + \left( \frac{a^3}{z^3} \right)^2 \right)$$



# Modified SZ signal (1)

$$\Delta I(x) \propto g(x) \int_{cl} \left( \frac{k_B T_g}{m_e c^2} \right) \sigma_T n_e dl_{cl}$$

- no change in  $g(x)$
- 3 regions along l.o.s:  $P_{ex}$ , subcluster, turbulent region behind



Estimate:  $\Delta SZ_M = \frac{\Delta I_M(x)}{\Delta I(x)}$

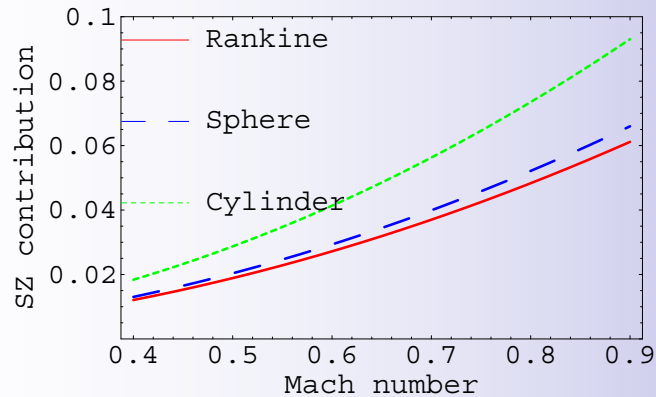
$$\Delta SZ_M = 1 + \frac{1}{2 \int_0^{r_1} f(r) dr} \left[ \int_{r_1}^{r_{M,1}} f(r) \frac{1}{2} M^2 \left( 1 - \frac{v(z)^2}{u_\infty^2} \right) dr - \int_{r_{M,1}}^{r_{M,2}} f(r) dr + a \frac{n_{e,M} T_M}{n_{e,0} T} \right]$$

✧ Many parameters:  $r_c$ ,  $M$ , subcluster

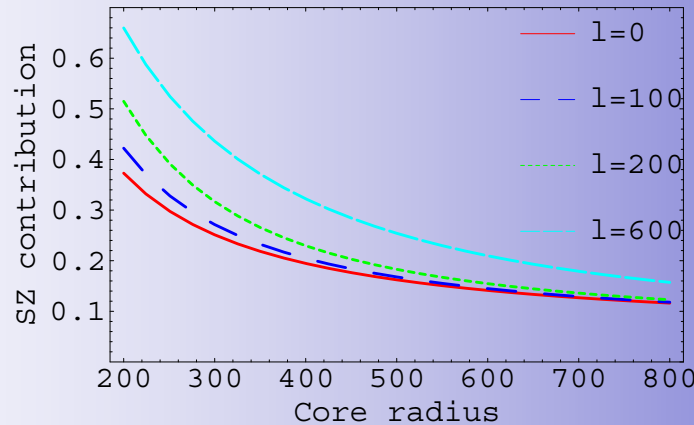
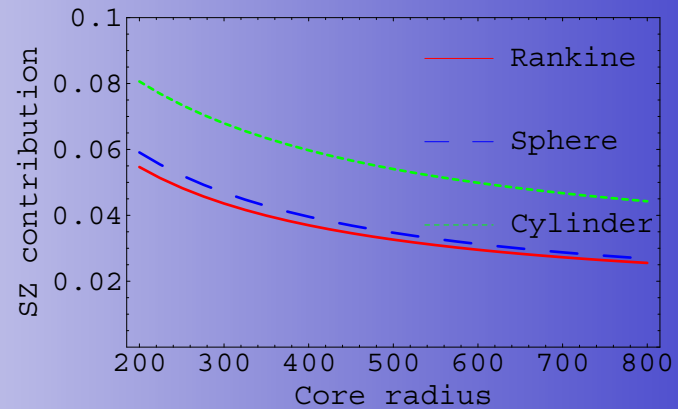
# Modified SZ signal (2)

$$\Delta SZ_M = \frac{\Delta I_M(x)}{\Delta I(x)} \quad \Delta SZ_M = 1 + \frac{1}{2 \int_0^{r_l} f(r) dr} \left[ \int_{r_l}^{r_{M,1}} f(r) \frac{1}{2} M^2 \left( 1 - \frac{v(z)^2}{u_\infty^2} \right) dr - \int_{r_{M,1}}^{r_{M,2}} f(r) dr + a \frac{n_{e,M} T_M}{n_{e,0} T} \right]$$

Excess pressure contribution



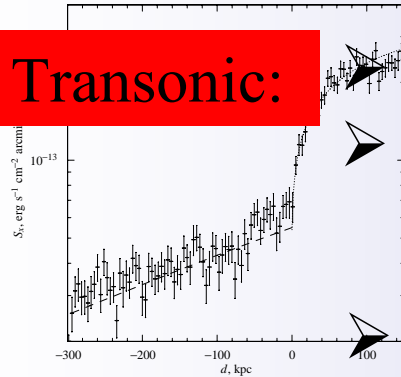
Excess pressure contribution



subcluster contribution  
depending on location l

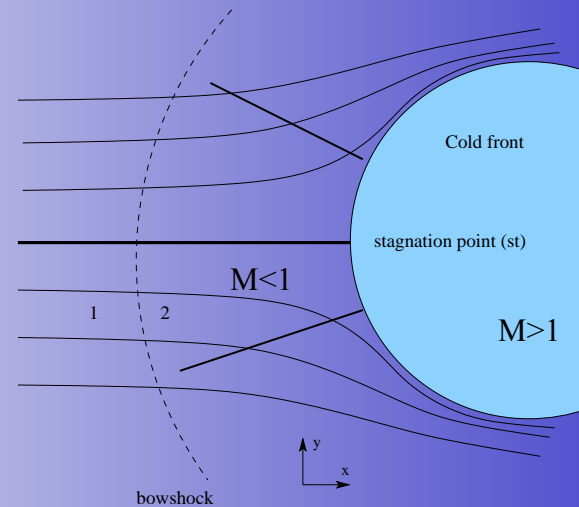
# Model and characteristics: transonic

**Transonic:**



- bow shock  $\star$  change microphysics,  $g(x)$
- Rankine-Hugoniot jump conditions at shock front
- $\star$  test with observations:  $C$
- compressible flow within shock region

$$\left. \begin{aligned} \rho_1 v_1 &= \rho_2 v_2 \\ P_1 + \rho_1 v_1^2 &= P_2 + \rho_2 v_2^2 \\ h_1 + \frac{1}{2} v_1^2 &= h_2 + \frac{1}{2} v_2^2 \end{aligned} \right\} \begin{aligned} \frac{\rho_1}{\rho_2} &= \frac{2\gamma}{\gamma+1} M^2 + \frac{\gamma-1}{\gamma+1} = \frac{1}{C} \\ \frac{P_2}{P_1} &= \frac{2\gamma}{\gamma+1} M^2 - \frac{\gamma-1}{\gamma+1} \end{aligned}$$



$\star$  Result: additional contribution due to pressure jump



# Modified SZ signal (1)

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What changes? ☆ **g(x)**

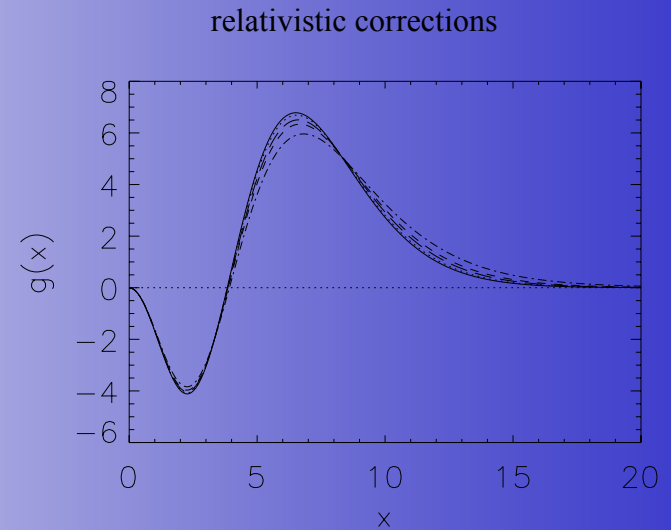
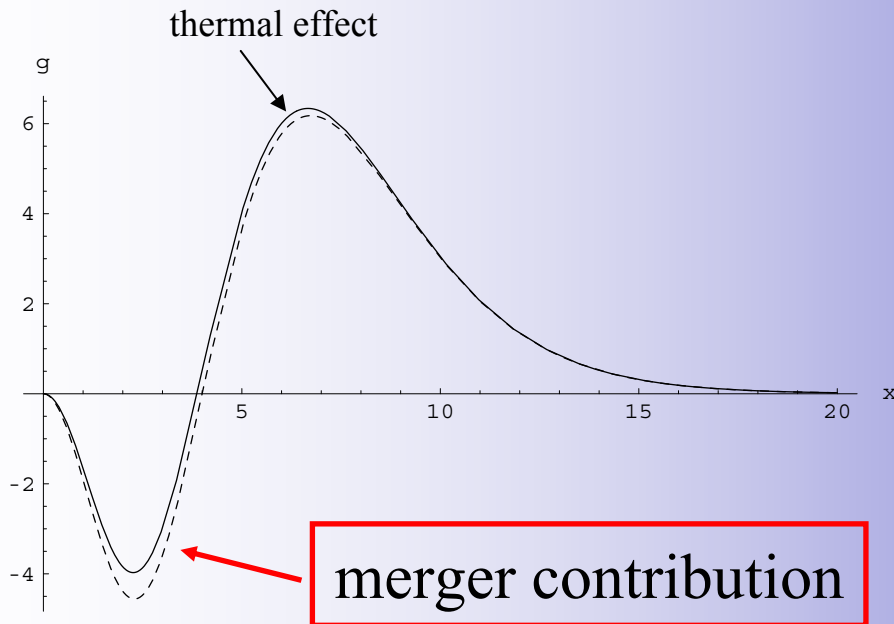
- shock particle re-acceleration mechanism depending on  $C$   
(1st order Fermi acc., stochastic acc. ... Not well known!)
- new emerging electron population
- hybrid electron distribution with high energy power law tail


$$\alpha = \frac{C+2}{C-1} \quad \star \text{ Problem: lower limit } p_l \text{ for power law!}$$

combination of 2 (independent) electron populations:  
☆ cross scattering, requires new calculation technique

# Modified SZ signal (2)

$$g(x)$$

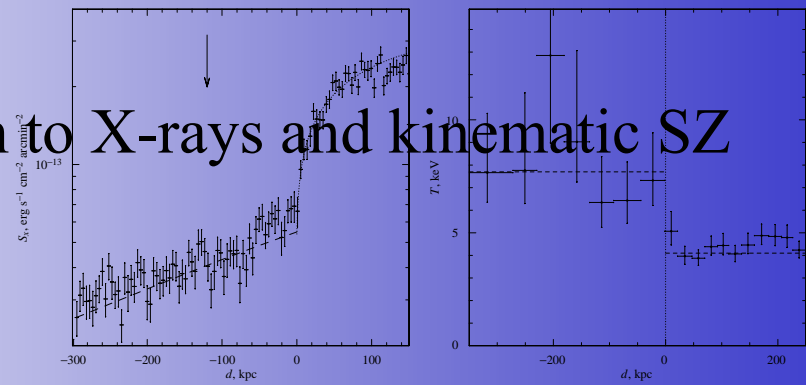
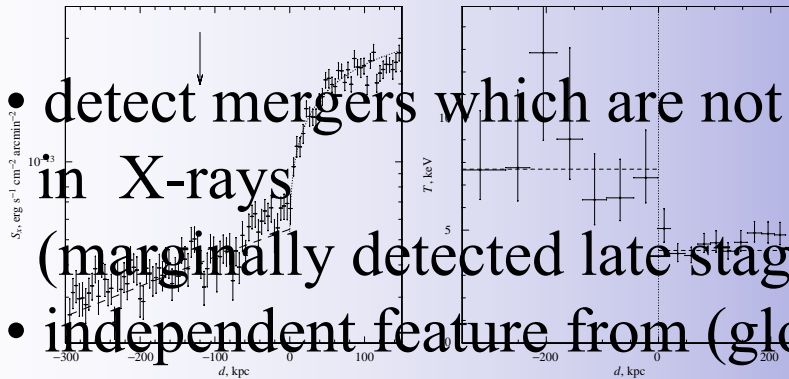


- ☆ Results:
- change in crossover  $\sim 10\%$
  - limited to certain regions?

# MAPS FOR SUBSONIC MERGERS

## Interest:

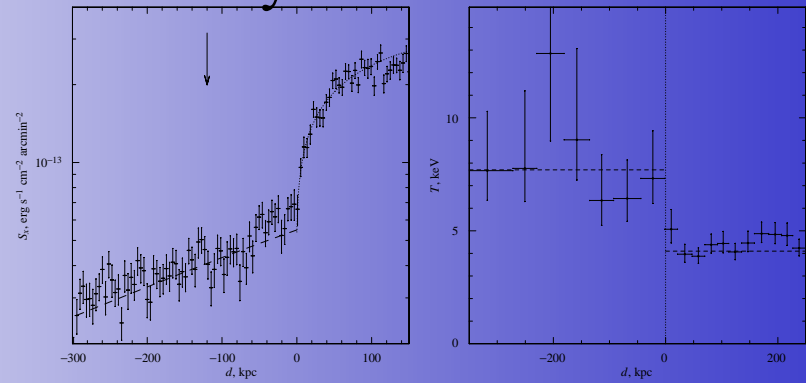
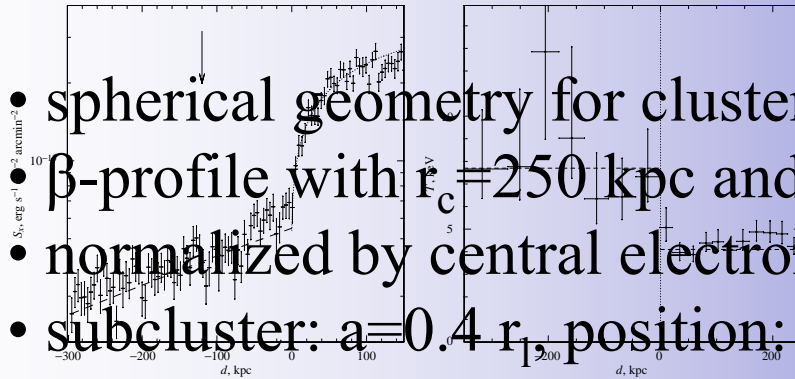
- detect mergers which are not identified by bow shocks in X-rays (marginally detected late stage, cold fronts)
- independent feature from (global) compressibility and heating effects
- look for merger dynamics
- complementary information to X-rays and kinematic SZ



# Maps for subsonic mergers

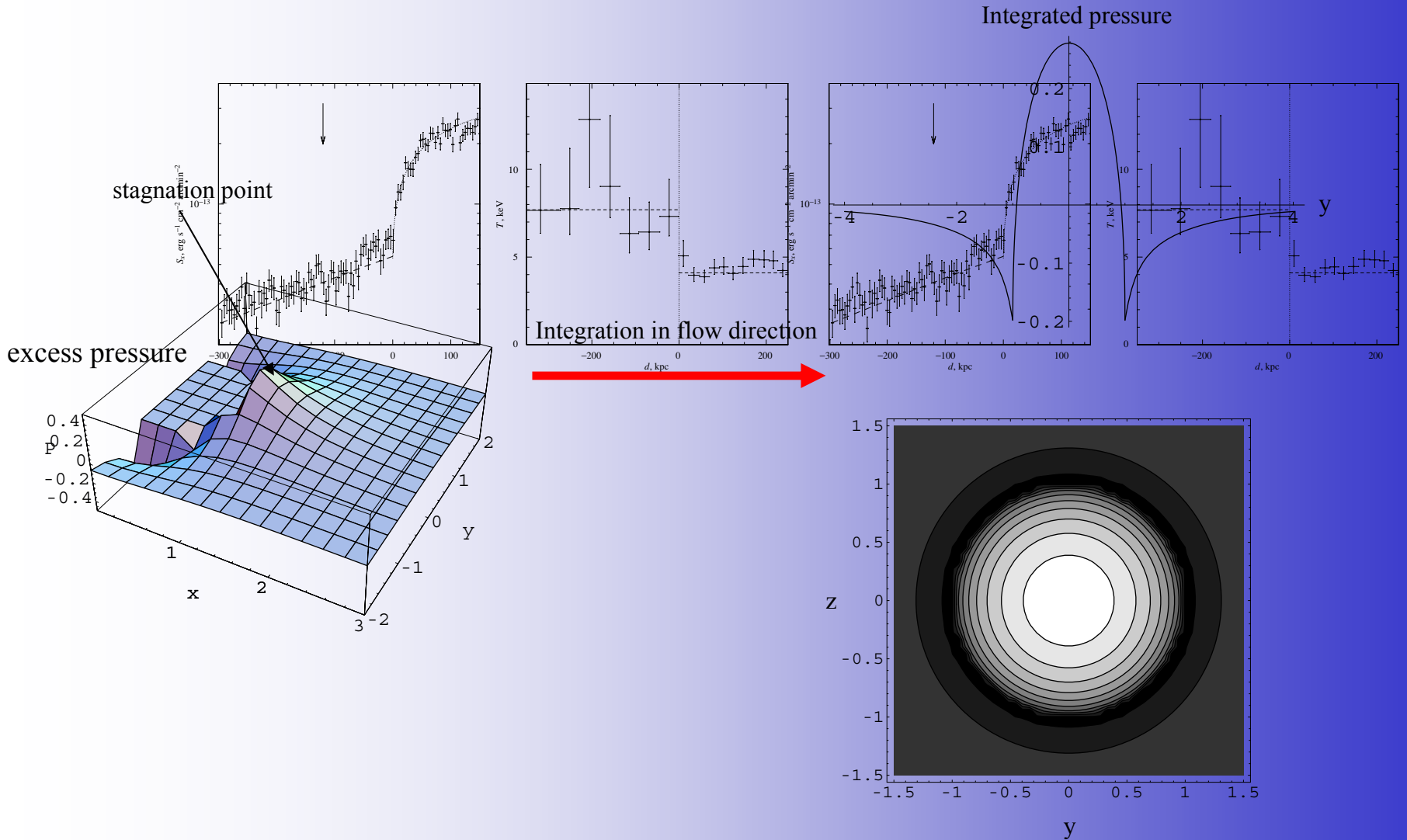
## Parameters:

- spherical geometry for cluster and subcluster
- $\beta$ -profile with  $r_c = 250$  kpc and  $\beta = 2/3$ ,  $r_1 = 1$  Mpc
- normalized by central electron density and temperature
- subcluster:  $a = 0.4 r_1$ , position:  $x = 0.5 r_1$ ,  $y = z = 0$ ,  $M = 0.6$
- subcluster density = background density
- DM structure not changed



# Maps for subsonic mergers

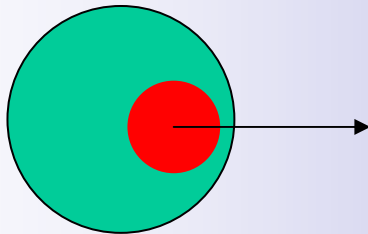
excess pressure feature:



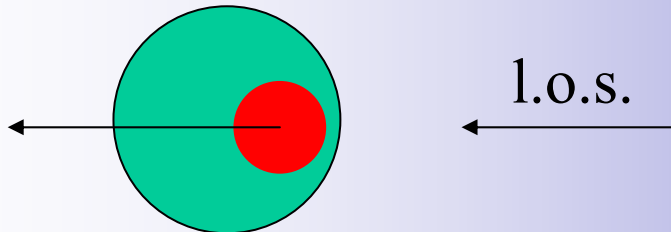
# Maps for subsonic mergers

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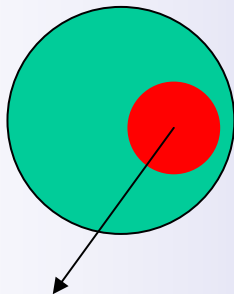
location  $\star$  direction of movement



late stage merger, cold front  
(slowed down)



infalling substructure

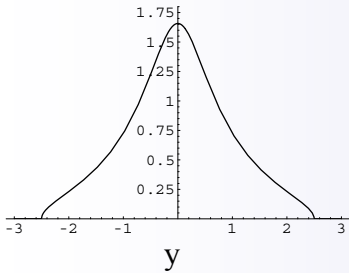


transversally moving  
substructure

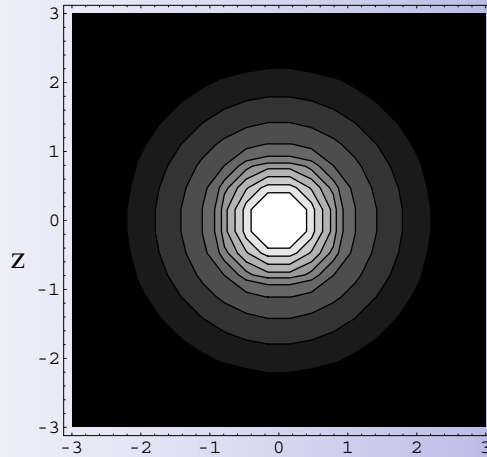
# Maps for subsonic mergers

results: excess pressure contribution

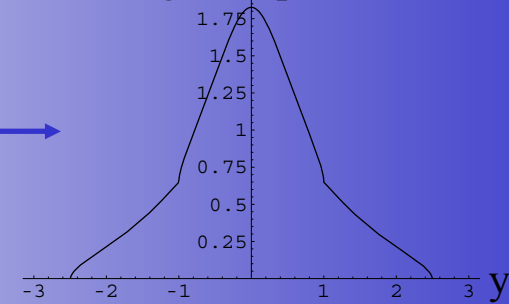
integrated pressure



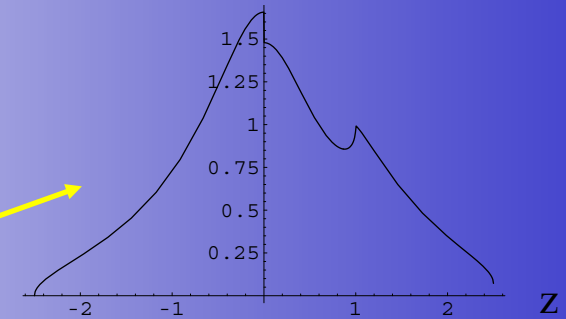
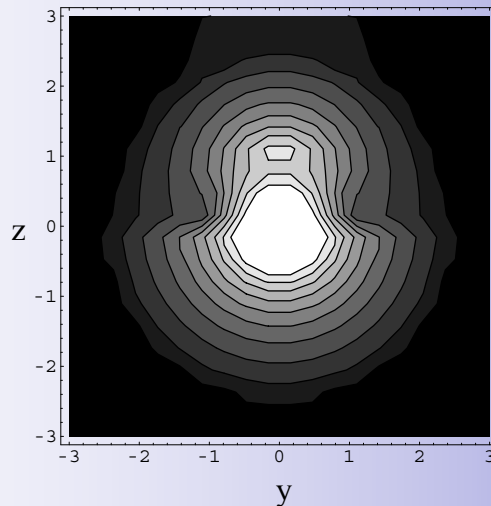
parallel



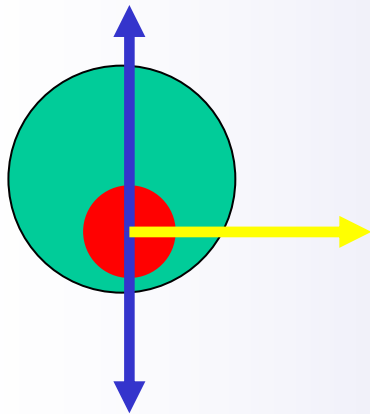
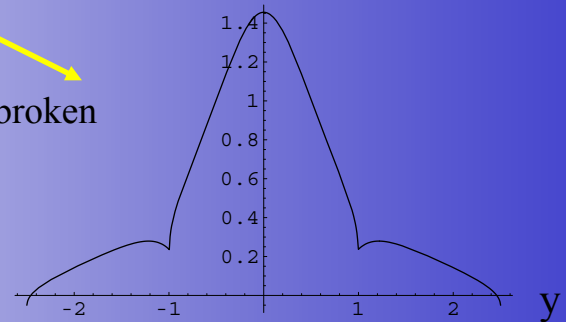
integrated pressure



perpendicular



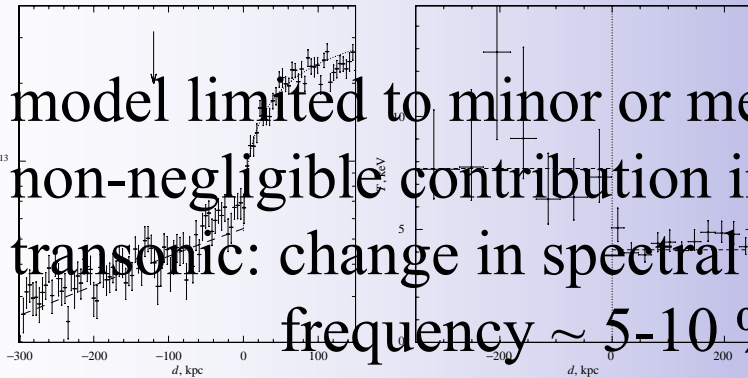
Symmetry broken



l.o.s.  
↑

# CONCLUSION AND SUMMARY

- model limited to minor or medium-scale merger
- non-negligible contribution in intensity:  $\sim 10-15\%$
- transonic: change in spectral function  $g(x)$  at crossover frequency  $\sim 5-10\%$



(Problem: disentangle from relativistic corrections)

- complementary/additional information due to excess pressure compared to X-rays (“invisible merger”)
- different features depending on direction of moving substructure (subsonic mergers), change:  $\sim 5-10\%$
- complementary to kinematic SZ
- detect substructures with high resolution SZ mapping (high  $z$ )
- SZ-survey: constrain merger rate and structure formation

