

# Adventures in the CMB Damping Tail

La Fièvre Neutrino et Comment Je Me Suis Soigné

Lloyd Knox (UC Davis)

Zhen Hou & Marius Millea (UCD)

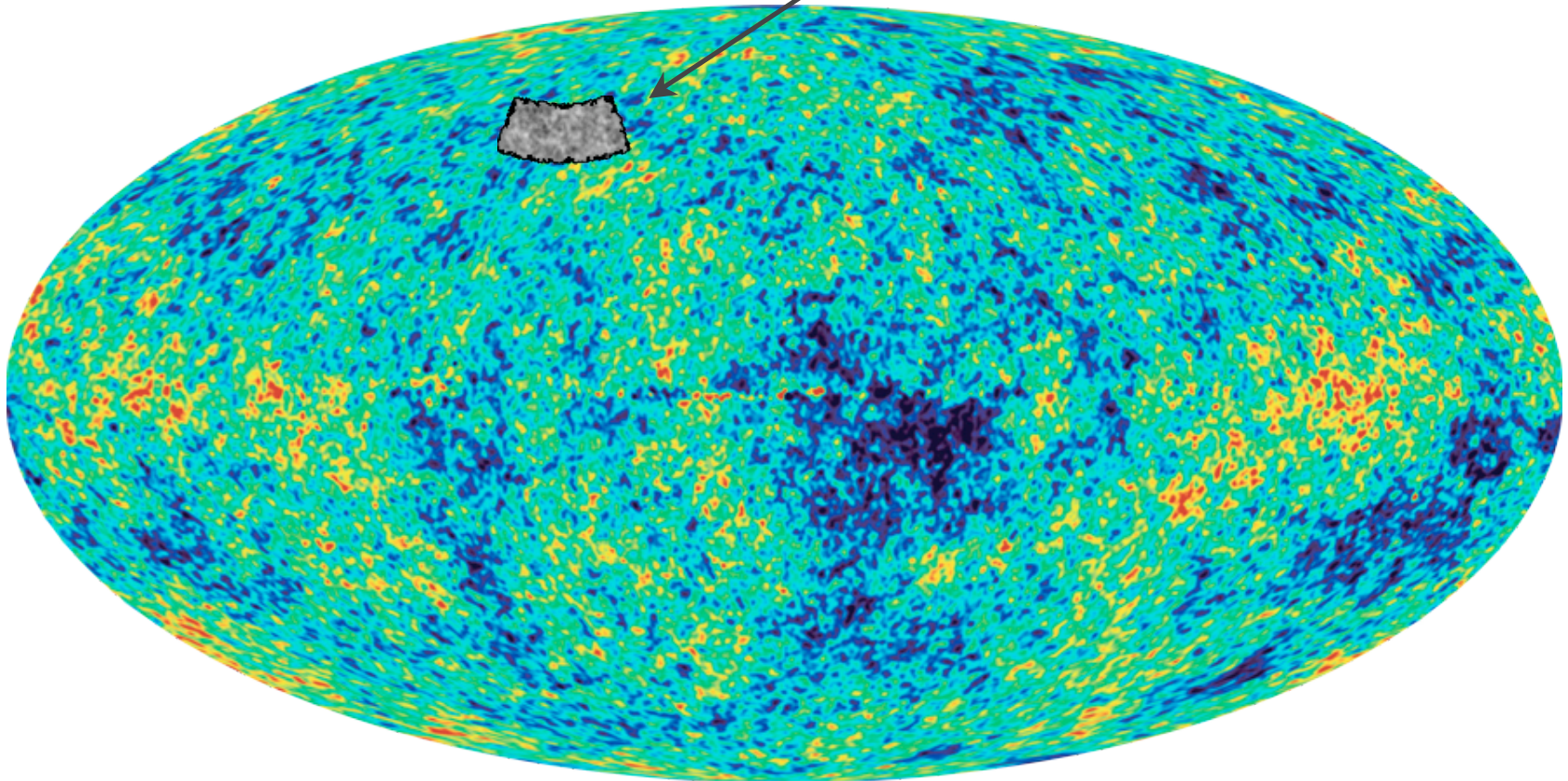
Ryan Keisler\* (UC), Christian  
Reichardt (UCB)

SPT collaboration

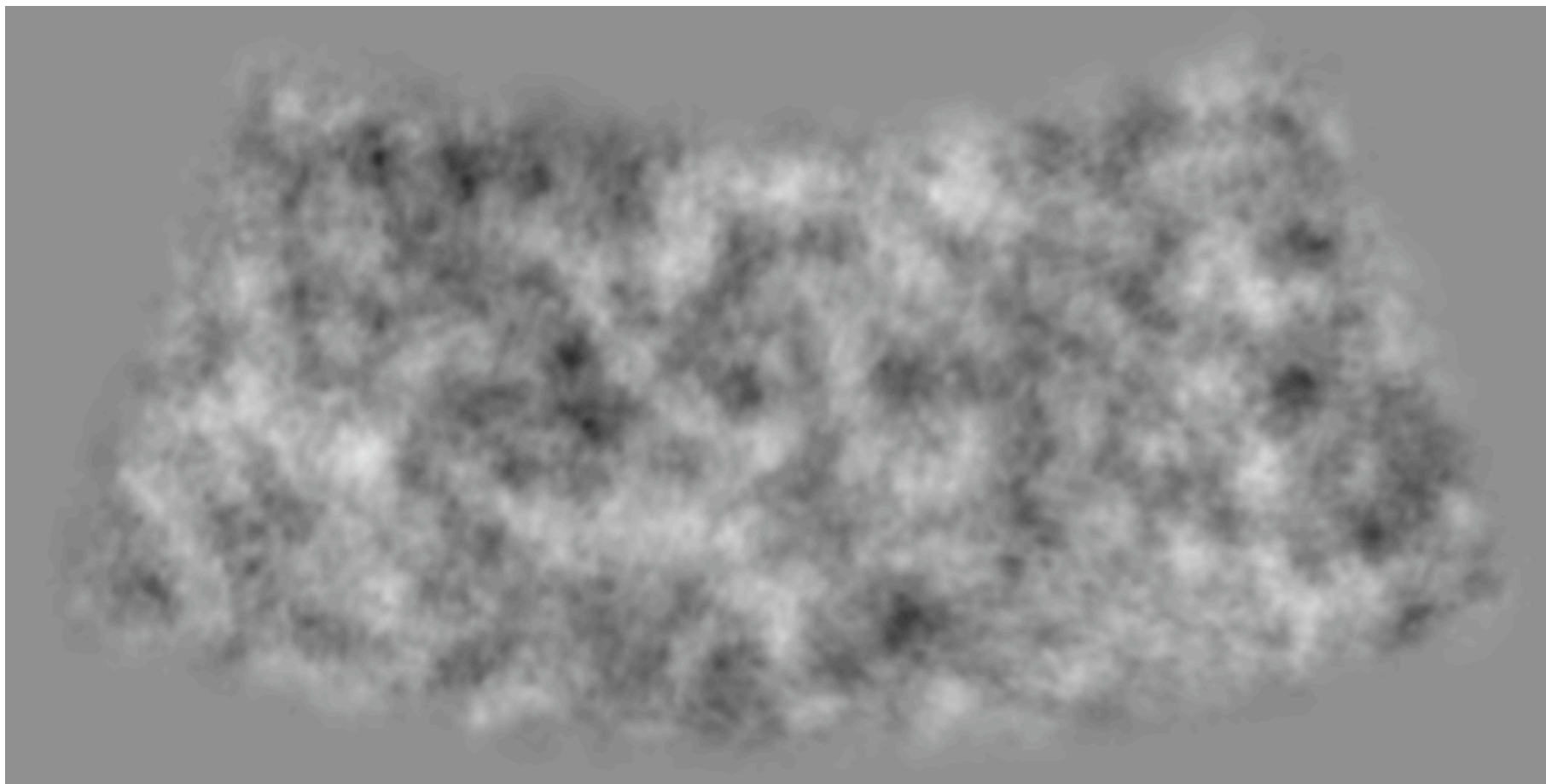
Hou et al. (2011), Keisler + SPT Collaboration (2011)

# WMAP

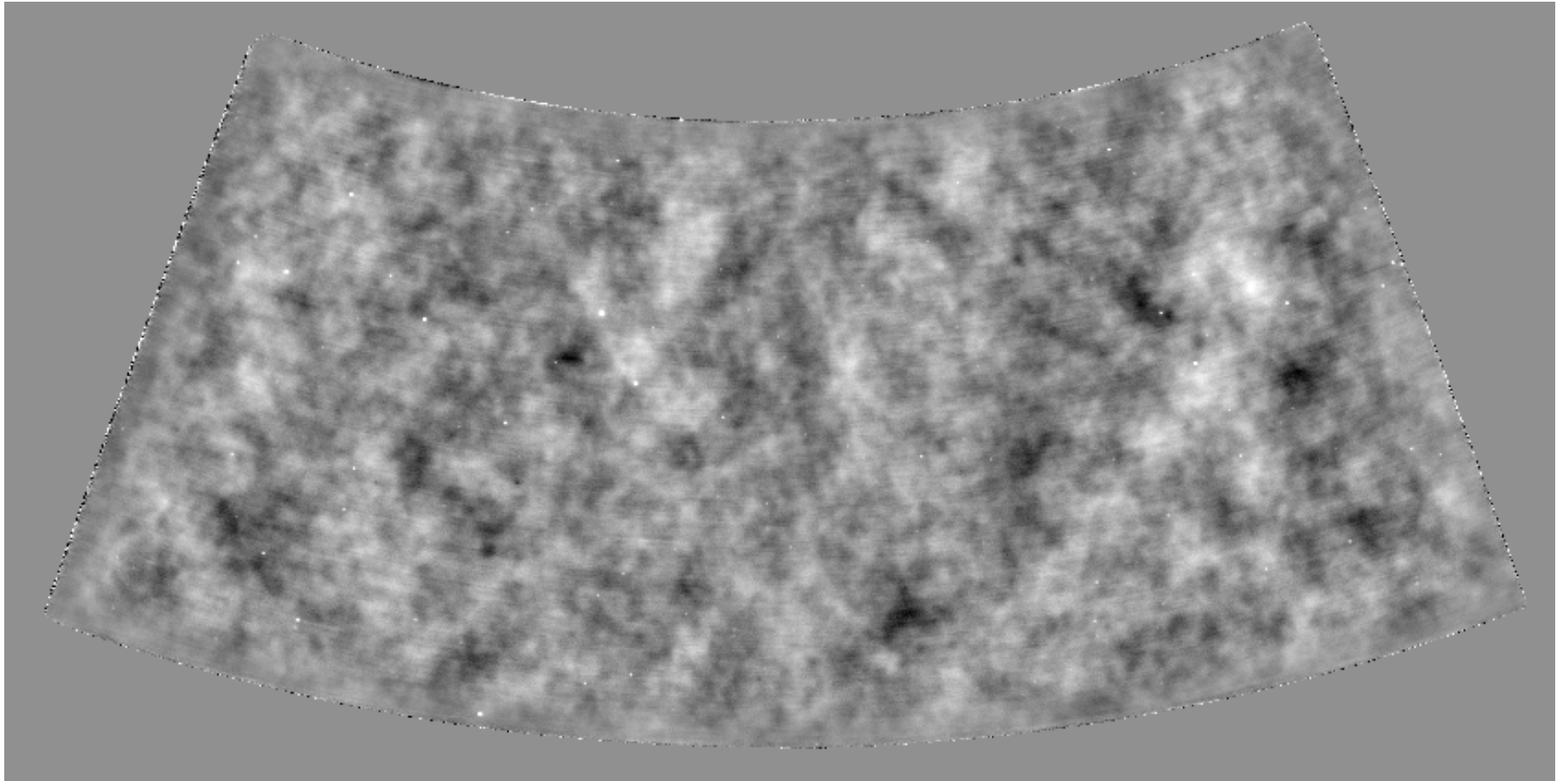
230 sq. degrees



# WMAP



# SPT



One of five fields observed in 2009, totaling 800 sq. deg.

# The South Pole Telescope

- 10 meter primary mirror
- 1000 pixel camera
- 3 bands (95, 150, 220 GHz)
- 1 arcminute resolution
- Deployed February 2007, will complete **2500 deg<sup>2</sup>** survey by end of 2011.

Chicago  
Berkeley  
Case Western  
McGill  
Boulder  
Harvard  
Davis  
Caltech  
Munich  
Michigan  
Arizona

...

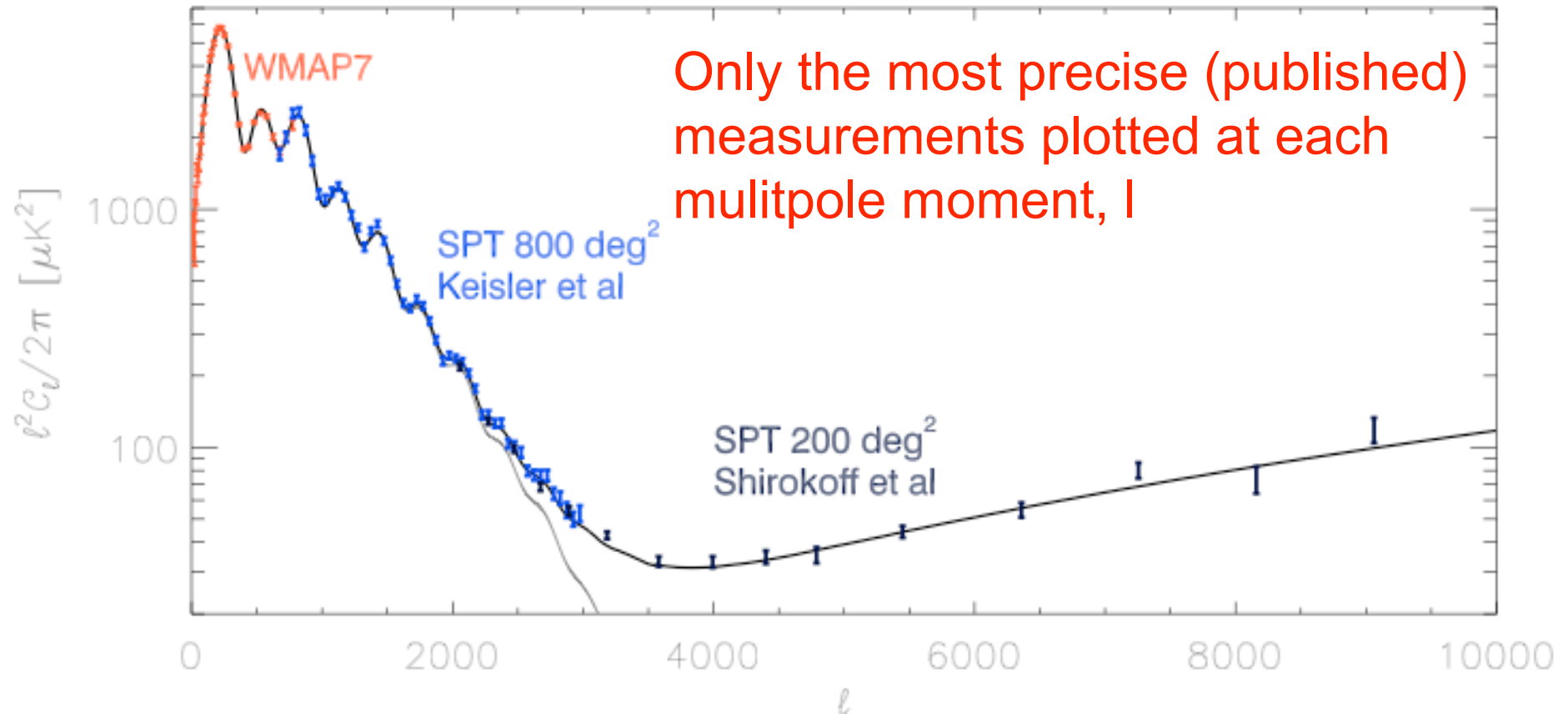
photo by Dana Hrubes

# The Angular Power Spectrum at 150 GHz

WMAP7

Extrapolated from

94 GHz

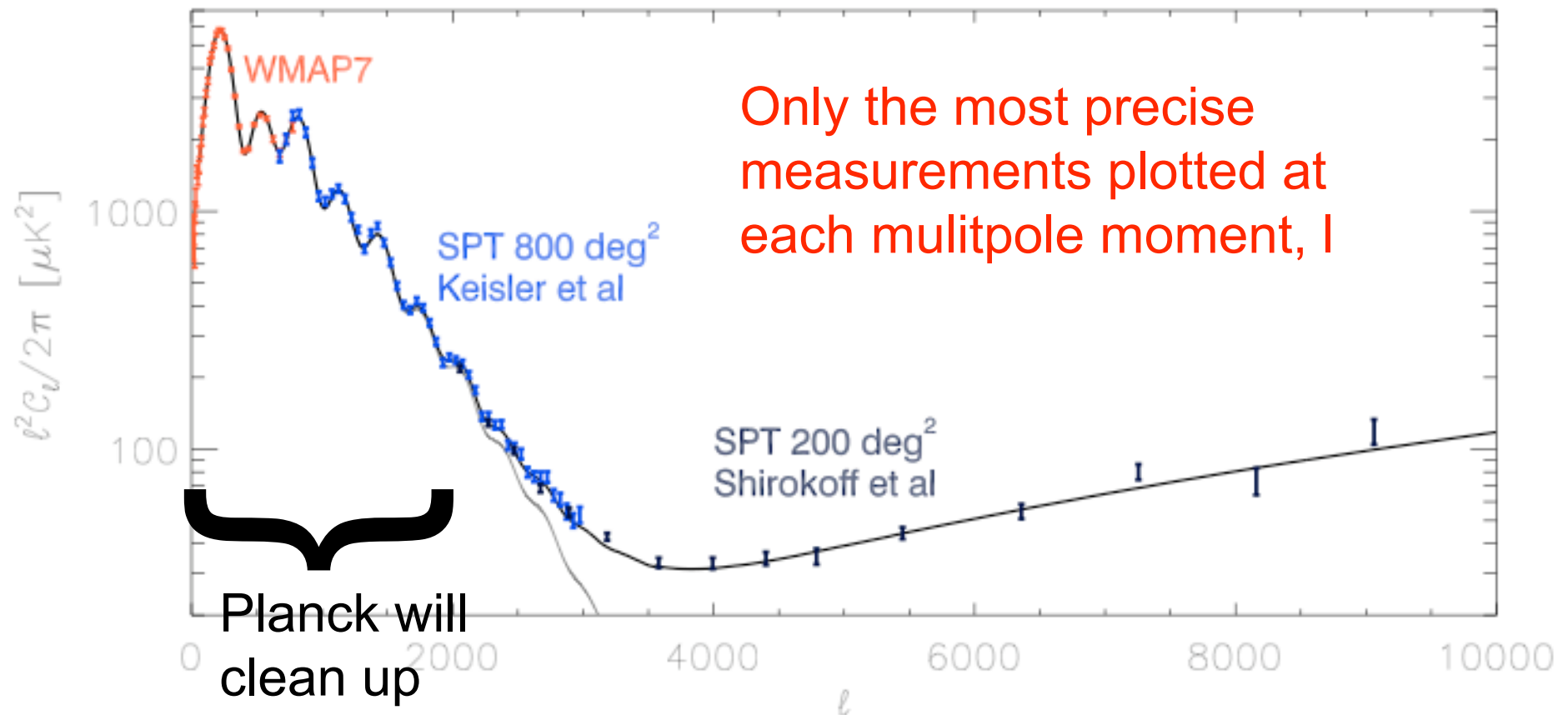


# The Angular Power Spectrum at 150 GHz

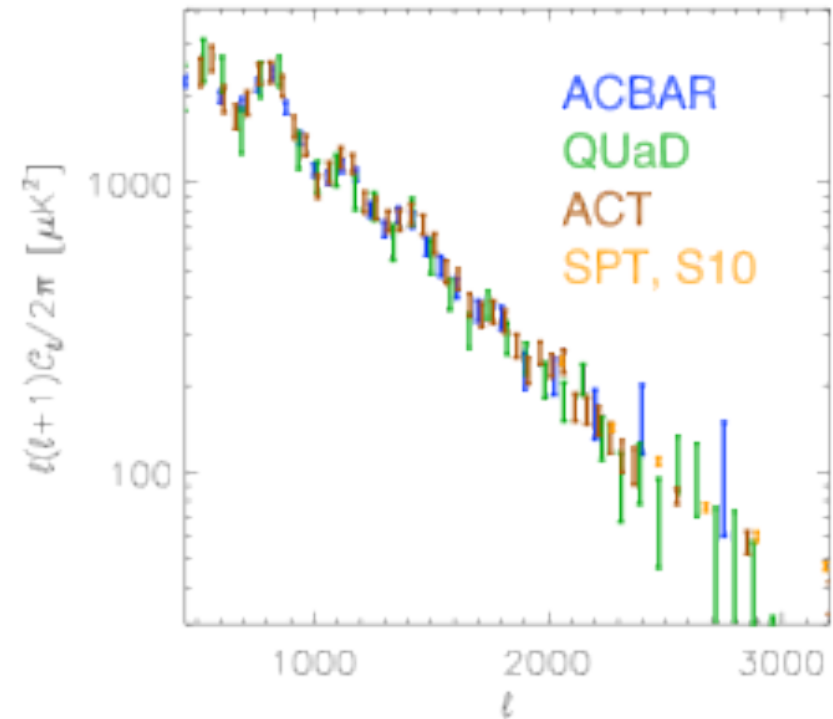
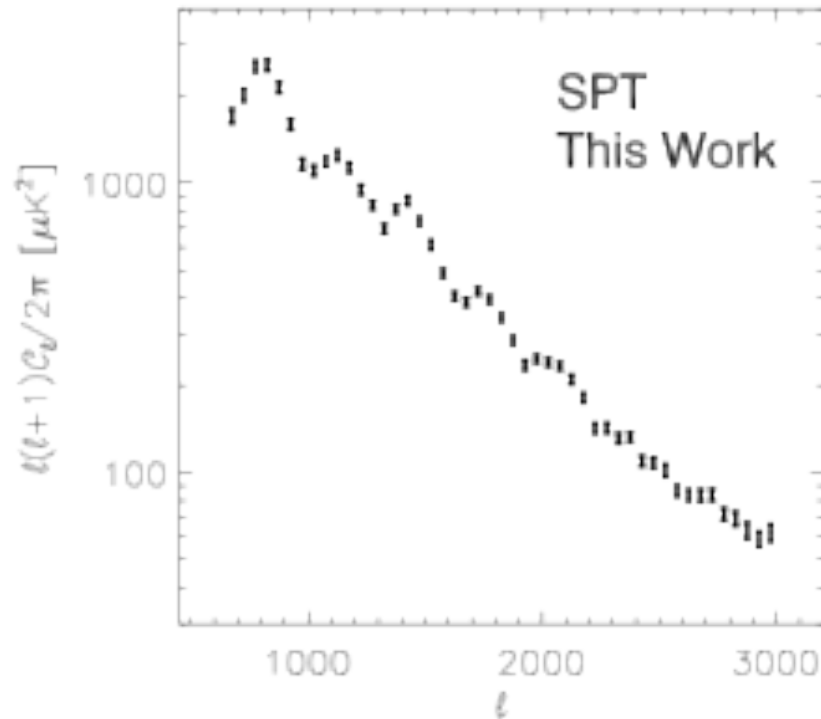
WMAP7

Extrapolated from

94 GHz



Keisler et al. (2011) provides a significant improvement in our knowledge of the damping tail



Prior state of the art

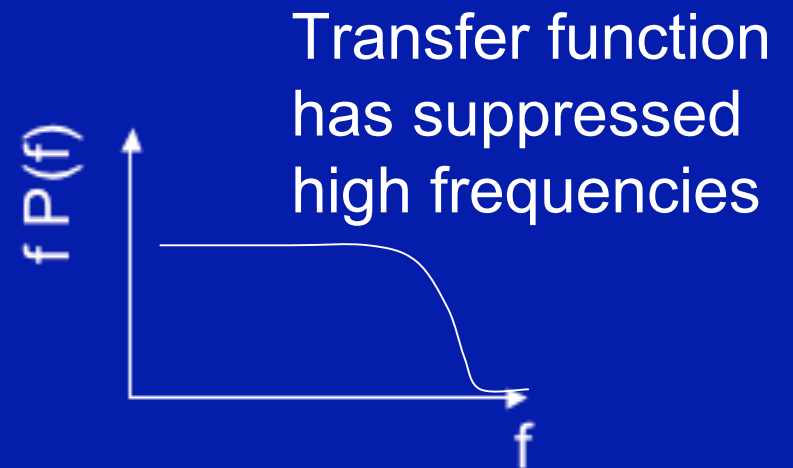
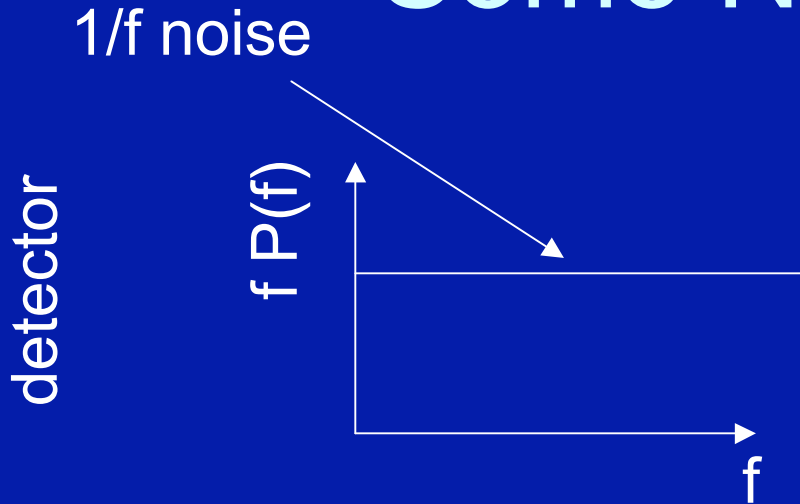
With this advance, and with much more to come soon from Planck, it's perhaps timely to review the physical interpretation.



# Outline

- CMB Theory for CMB Experimentalists
  - A Transfer Function Controlled by Three Angular Scales
- What can we learn from the damping tail
- Non-CMB evidence for extra neutrinos
- Conclusions

# The CMB is Like a Detector of Some Noise Source



CMB

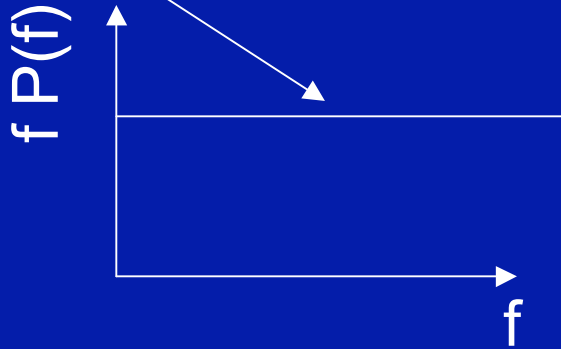
Noise source (input)

Detector output

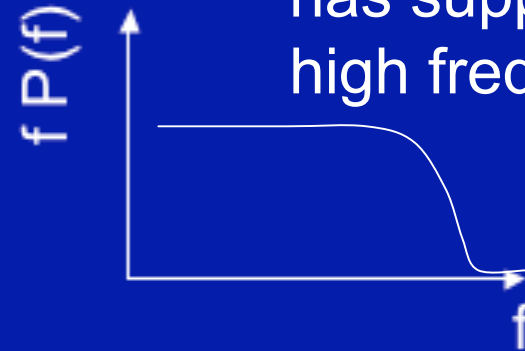
# The CMB is Like a Detector of Some Noise Source

detector

1/f noise



Transfer function has suppressed high frequencies



CMB



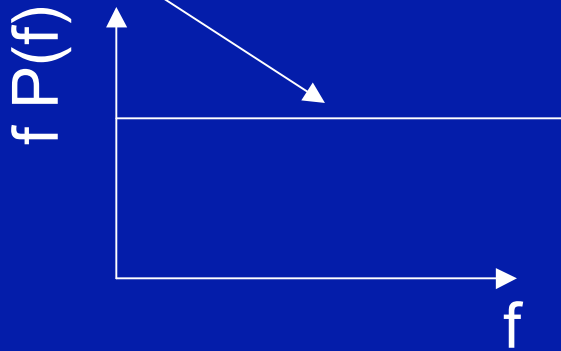
Noise source (input)

Detector output

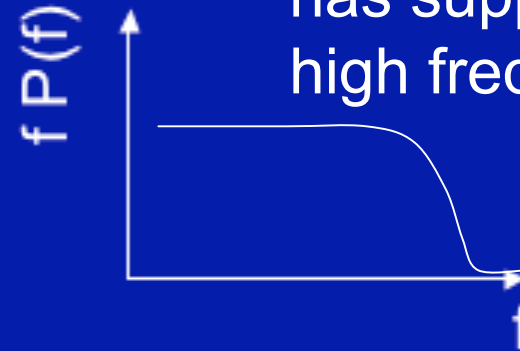
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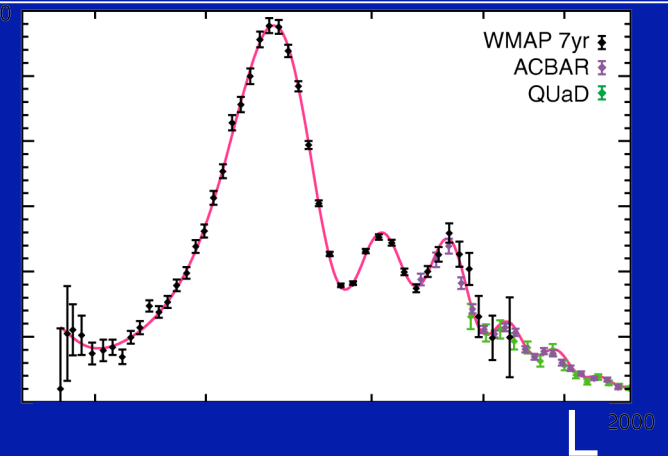


CMB



Noise source (input)

$L^2 C_L$



Detector output

# CMB as a Detector

Noise Source

Primordial fluctuation  
generator (inflation  
works well)

Transfer Function

Depends on matter content

# CMB as a Detector

Noise Source

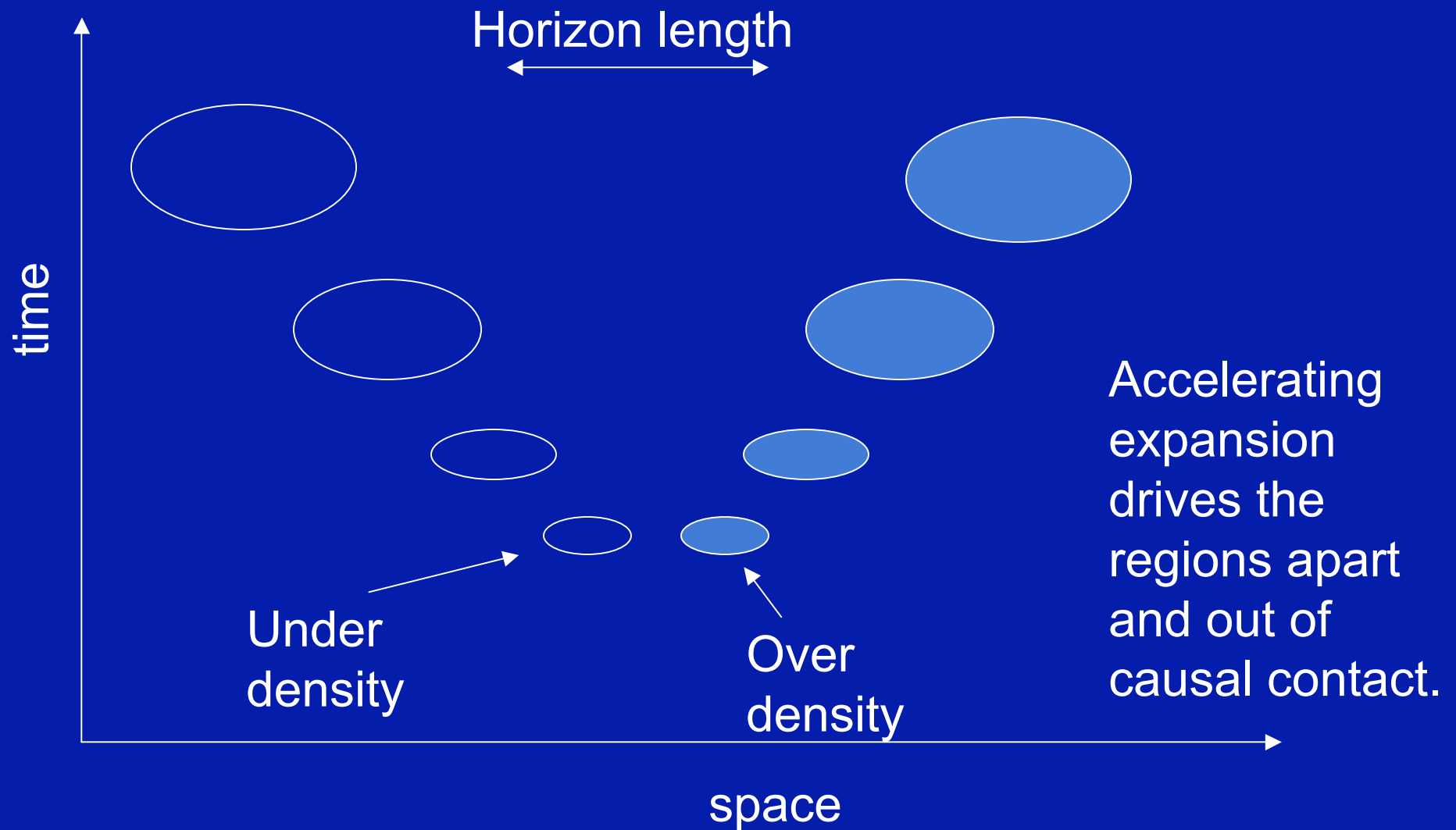
Primordial fluctuation  
generator (inflation  
works well)

Transfer Function

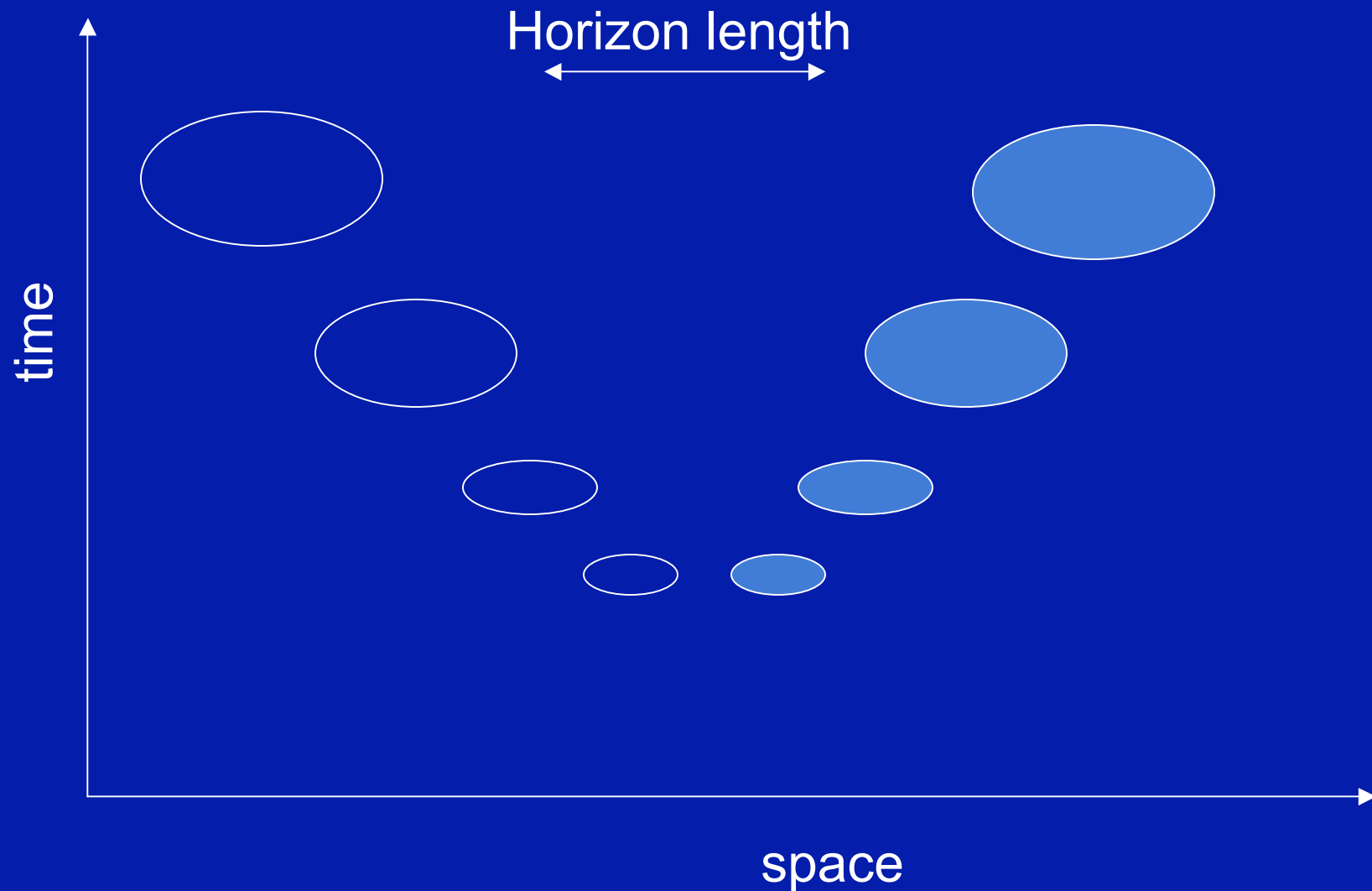
Depends on matter content

Inflation is a period of  
accelerating expansion rate

# Accelerating Expansion prevents quantum fluctuation from becoming undone

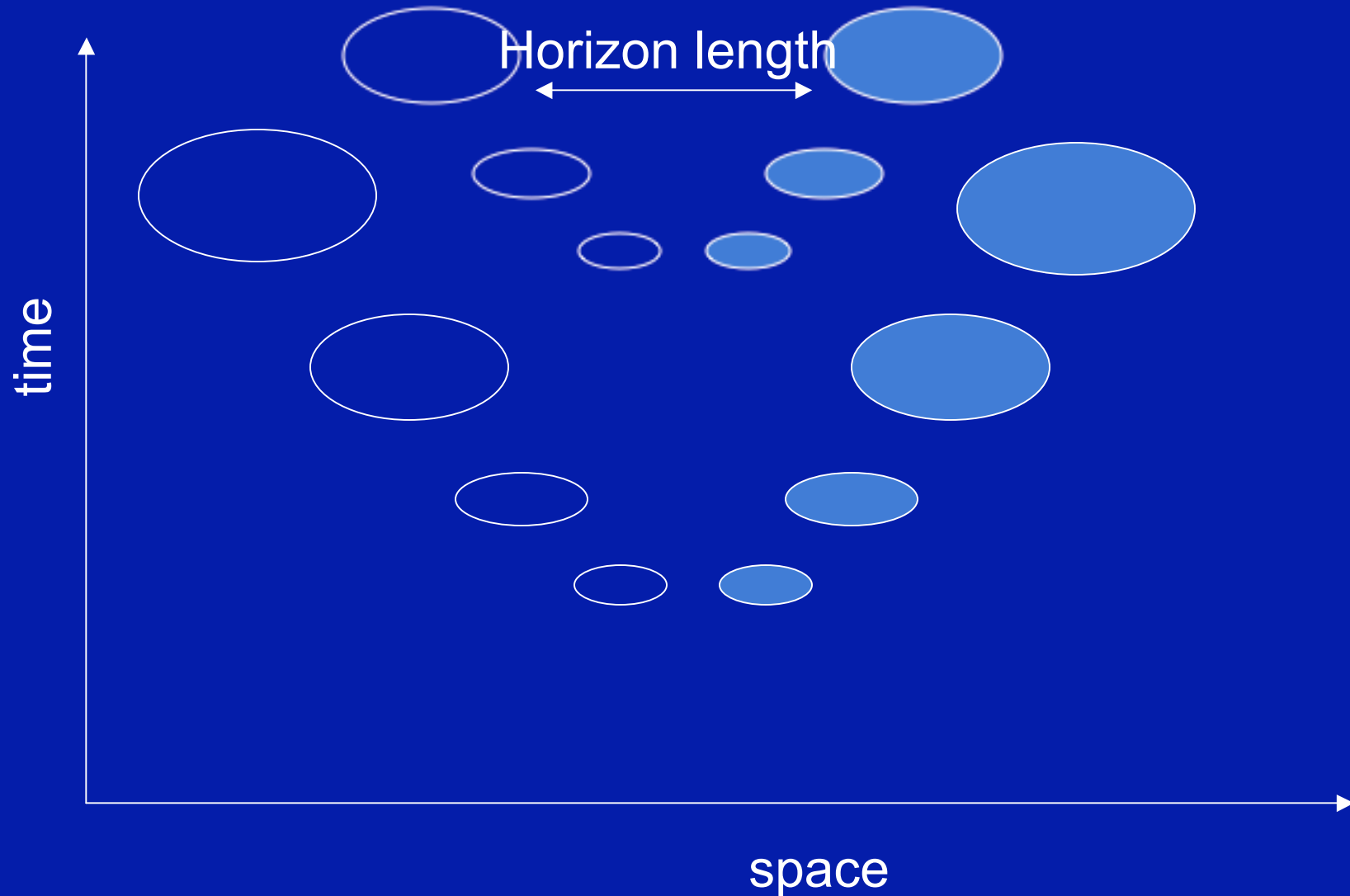


# Smaller-scale perturbations are made later





# Smaller-scale perturbations are made later



# CMB as a Detector

Noise Source

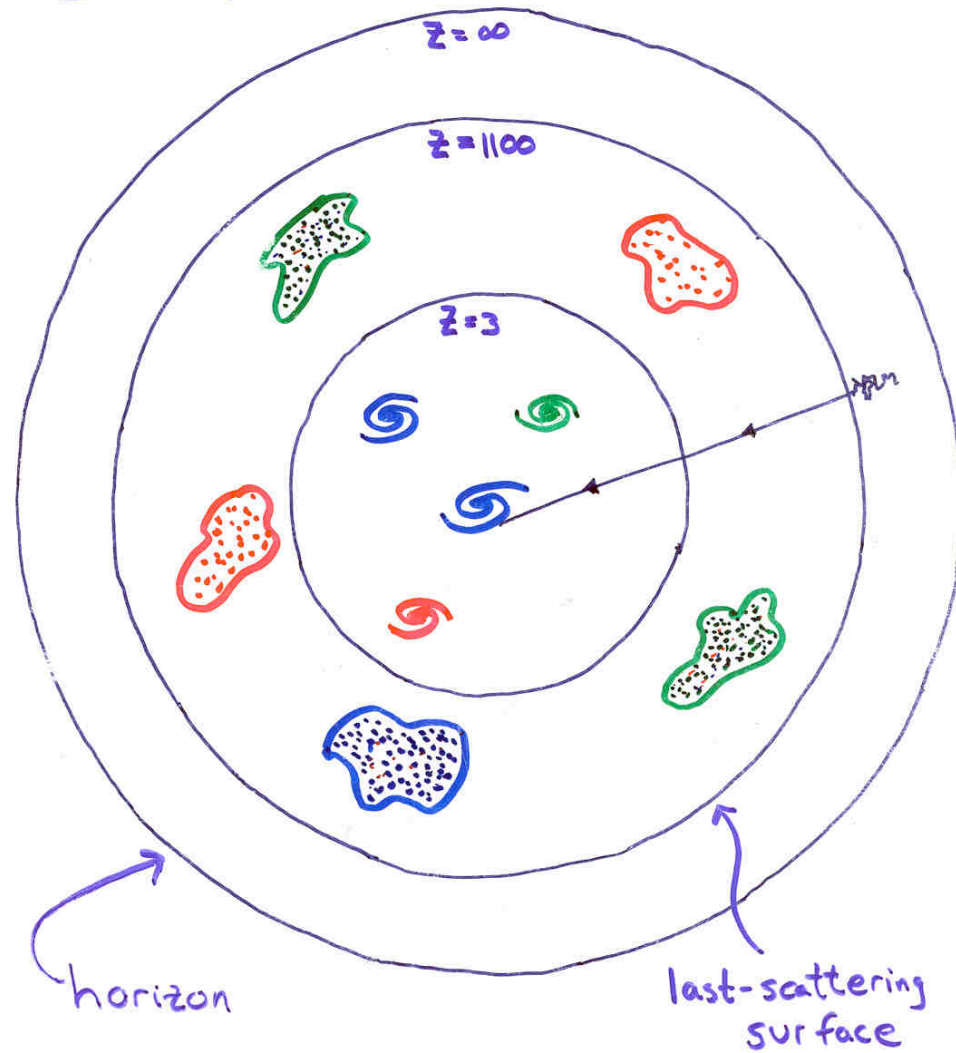
Primordial fluctuation  
generator (inflation  
works well)

Transfer Function

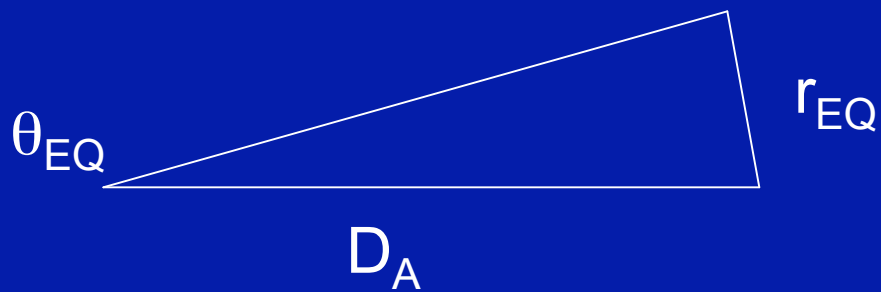
Depends on matter content

# THE HISTORY OF A SINGLE PHOTON

(12)



# Three Scales in the CMB Transfer Function

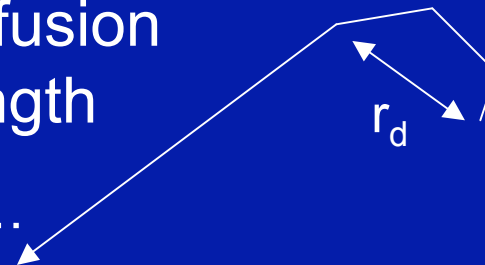


$r_{EQ}$  is the comoving size of the Hubble radius at Equality.

sound horizon: distance sound could travel by the time of last scattering.  $\theta_s$  controls peak locations.



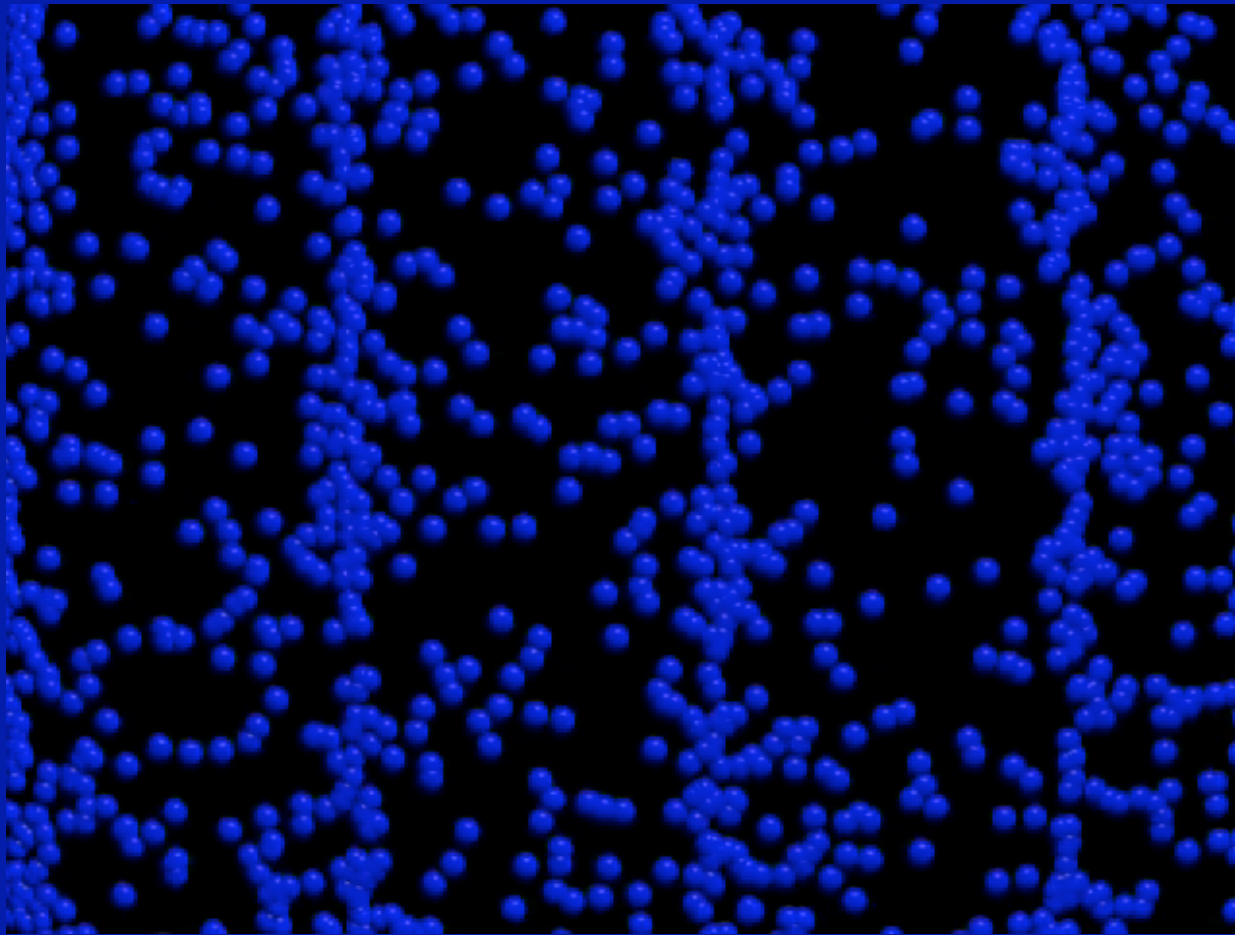
diffusion length



Silk, Kaiser, Hu, White, Bashinsky, Seljak, ...

Animation credit: Damien Martin (UCD)

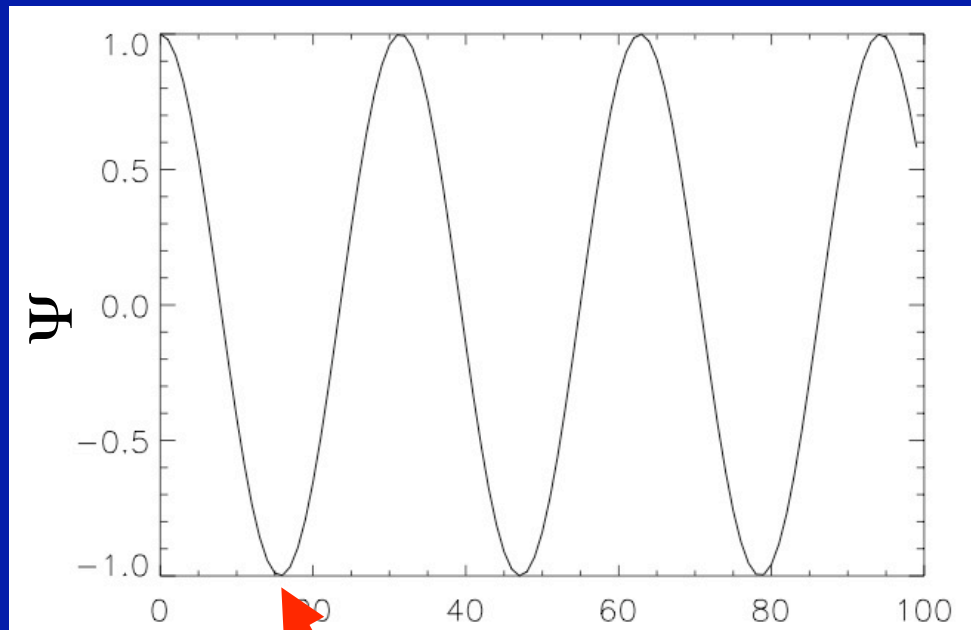
# Evolution of Single Fourier Mode



Potential Well

Potential Hill

# A Single Fourier Mode



space

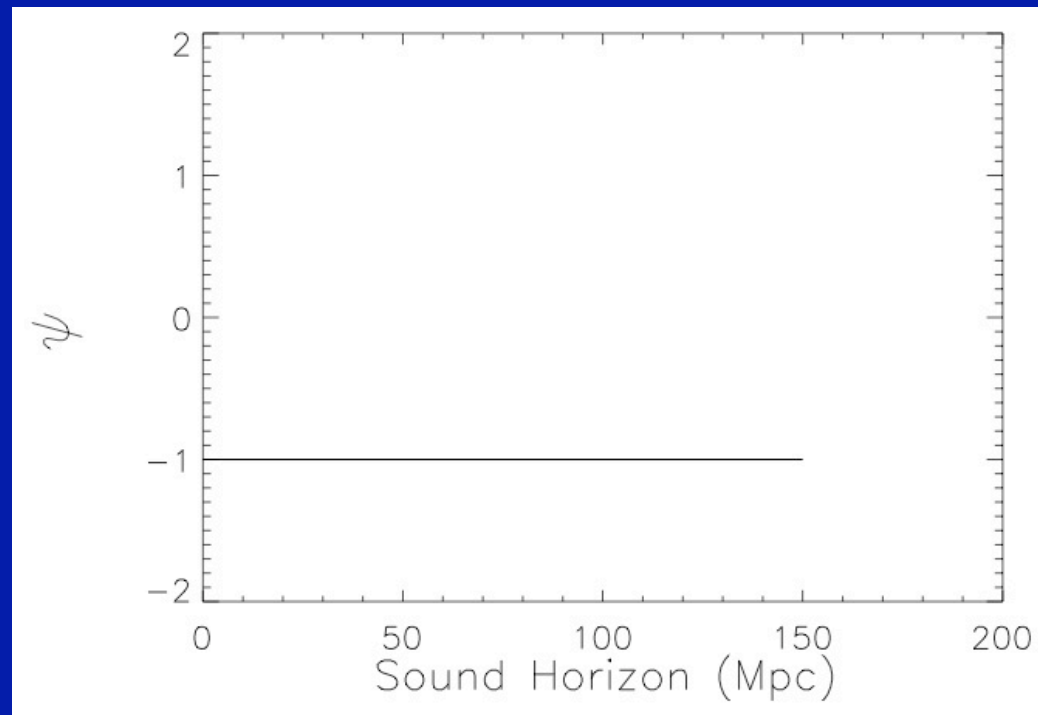
We will be considering how this single Fourier mode evolves with time.

For specificity, we will be tracking the amplitude of temperature and  $\Psi$  at this point in space.

# Gravitational Potential, $\Psi$ , as a function of time in a Matter-Dominated Universe

(We will be using the comoving size of the sound horizon as our time-like variable)

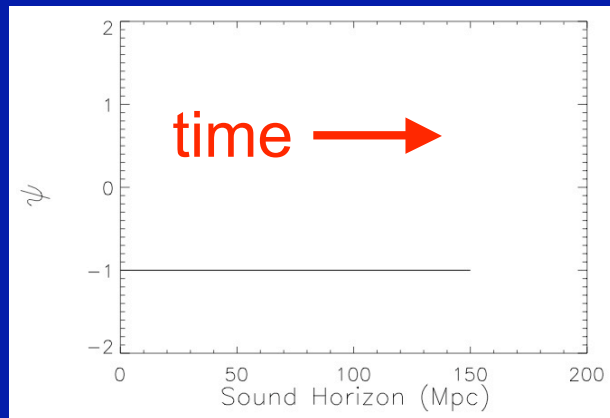
# Gravitational Potential, $\Psi$ , as a function of time in a Matter-Dominated Universe



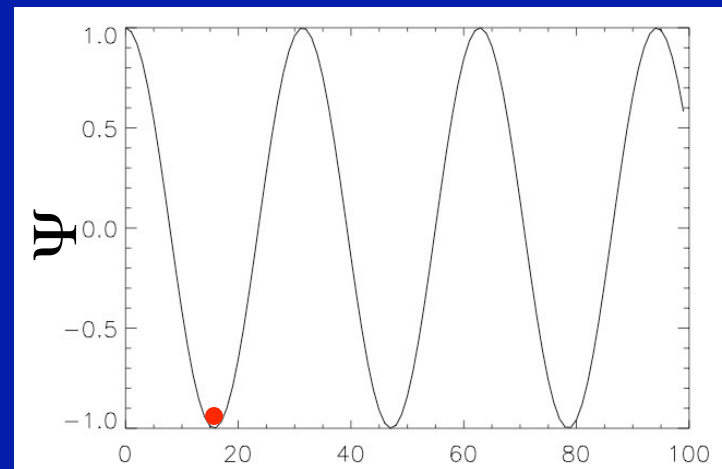
(We will be using the comoving size of the sound horizon as our time-like variable)



# Evolution Assuming Matter Domination

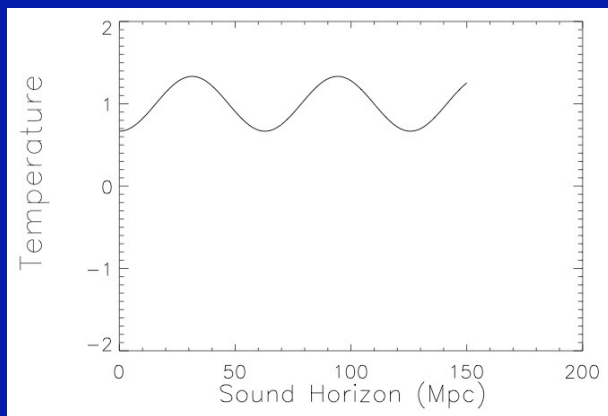
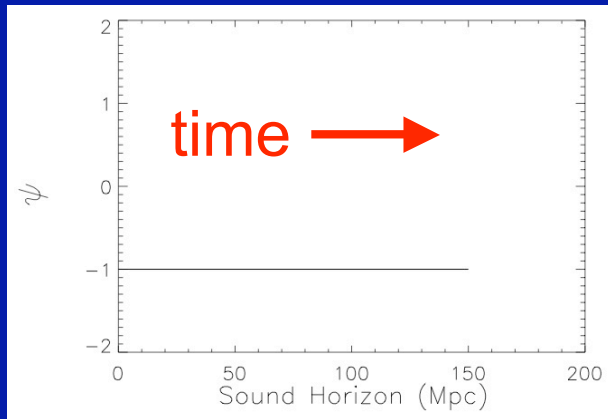


## Initial spatial dependence

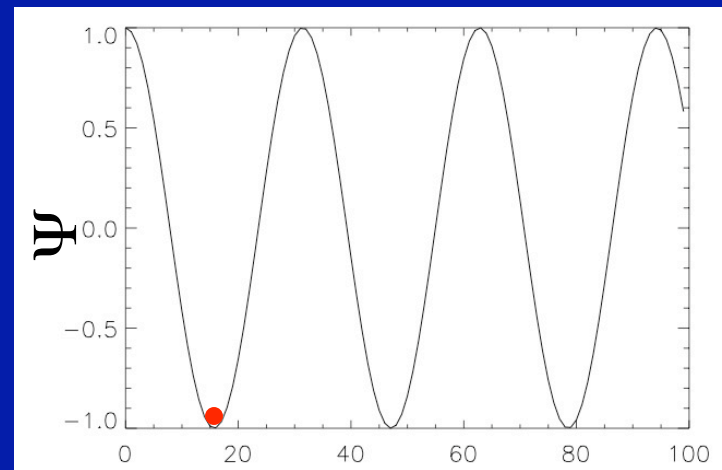


space

# Evolution Assuming Matter Domination



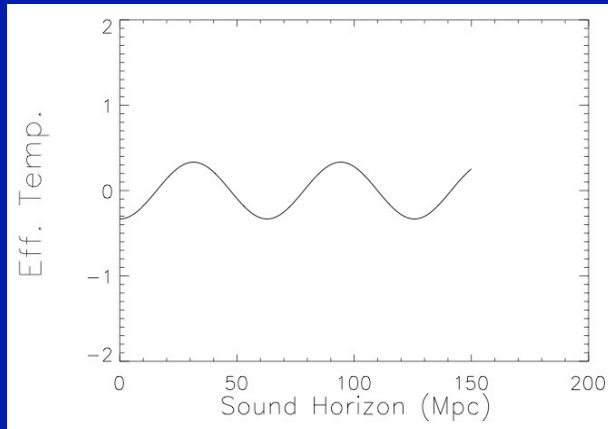
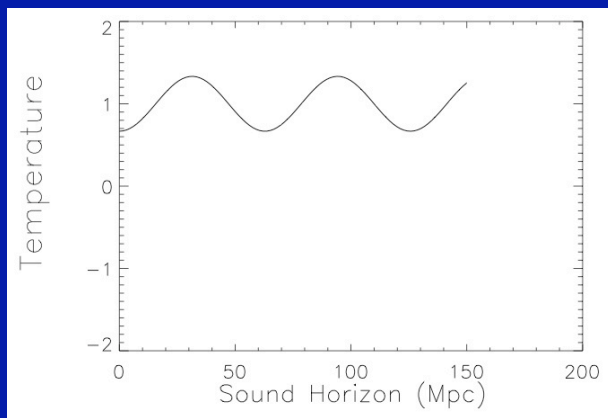
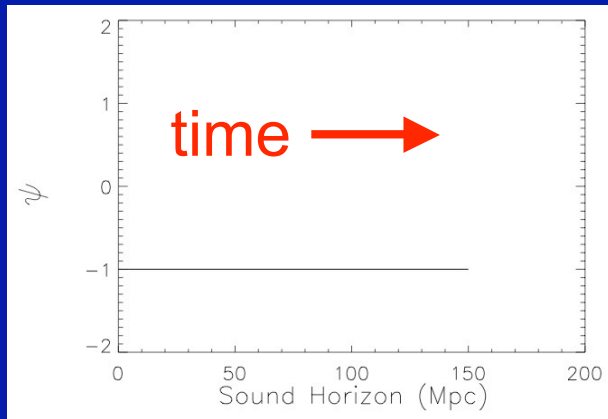
## Initial spatial dependence



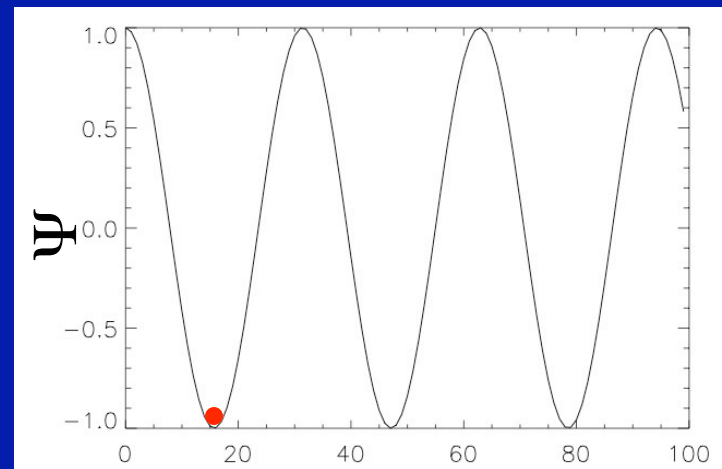
space

$$\text{"Temperature"} = \Theta_0 = \delta T/T$$

# Evolution Assuming Matter Domination



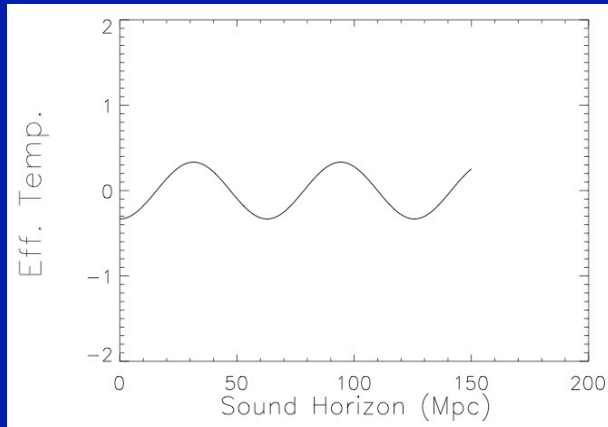
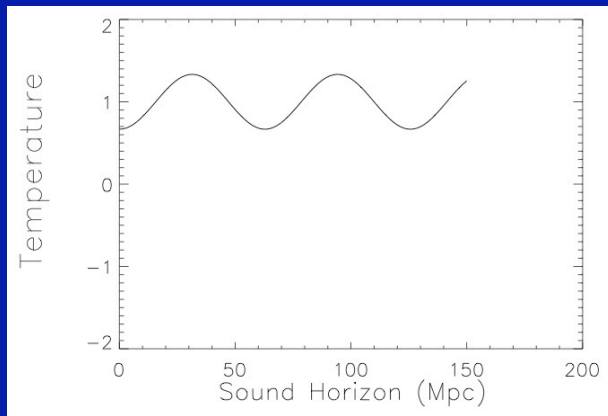
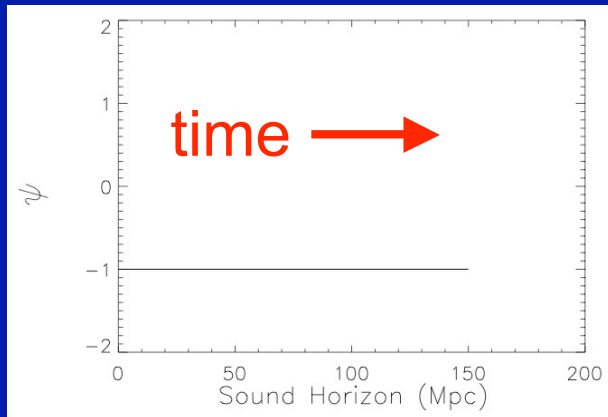
Initial spatial dependence



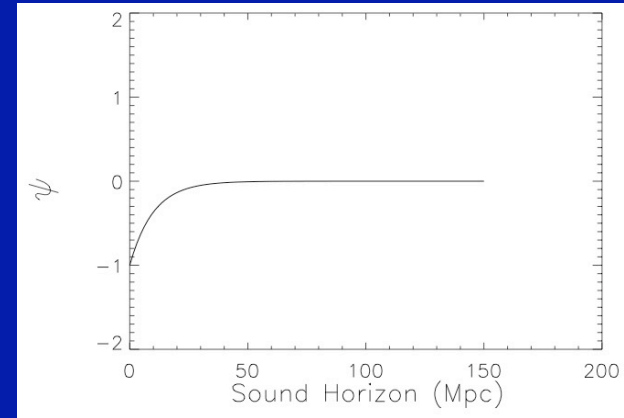
space

$$\text{“Effective Temperature”} = \Theta_0 + \Psi$$

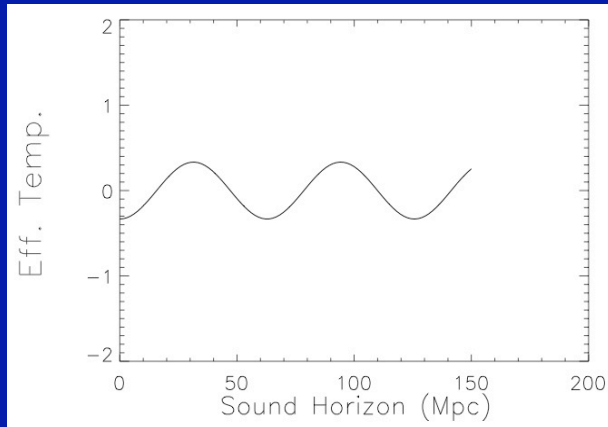
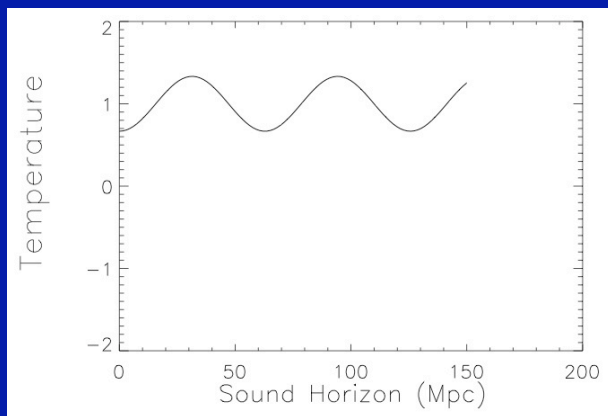
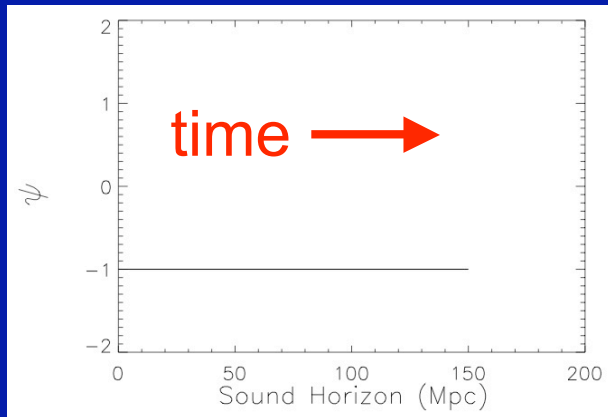
## Evolution Assuming Matter Domination



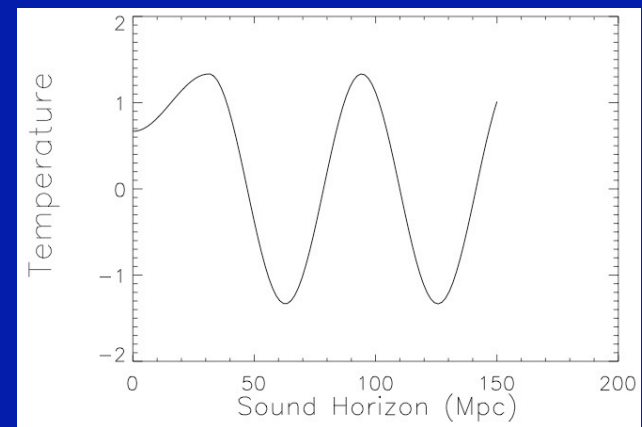
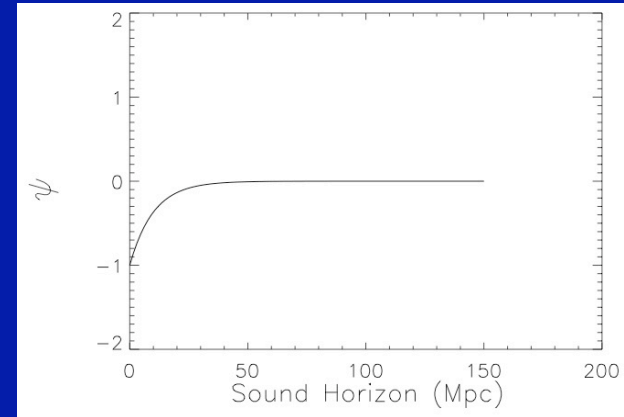
## Evolution Assuming Radiation Domination



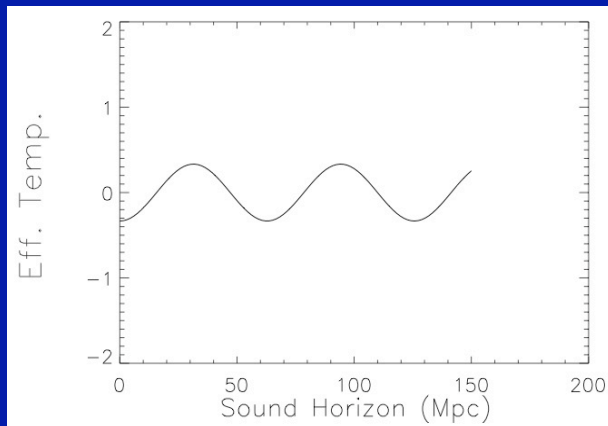
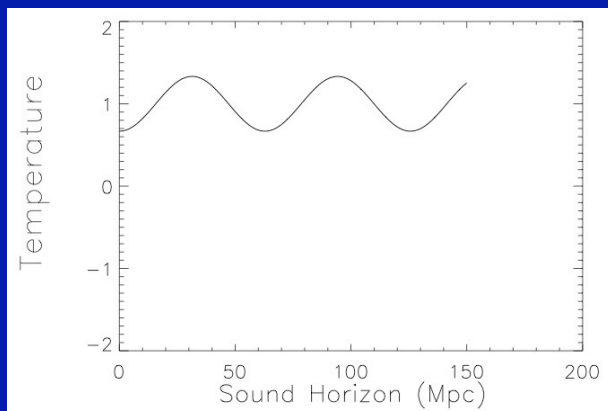
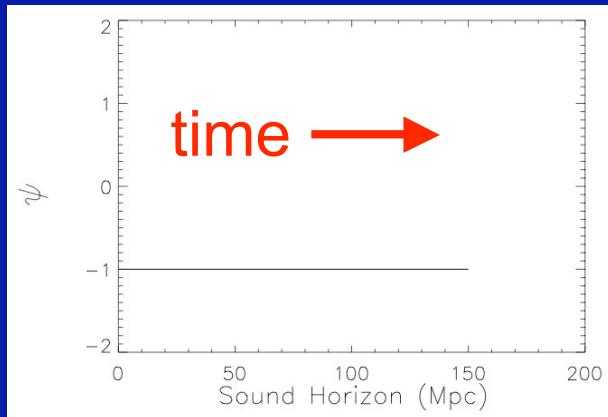
## Evolution Assuming Matter Domination



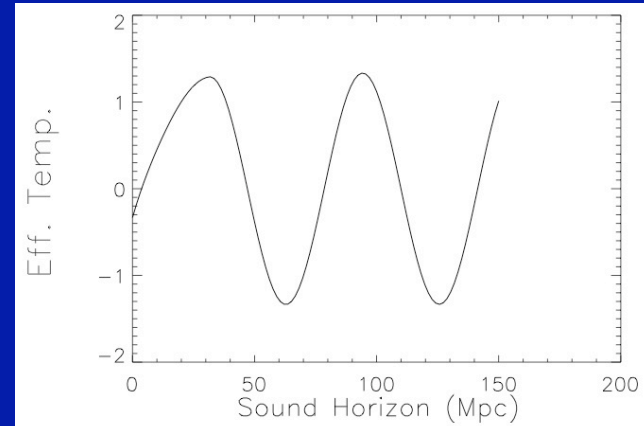
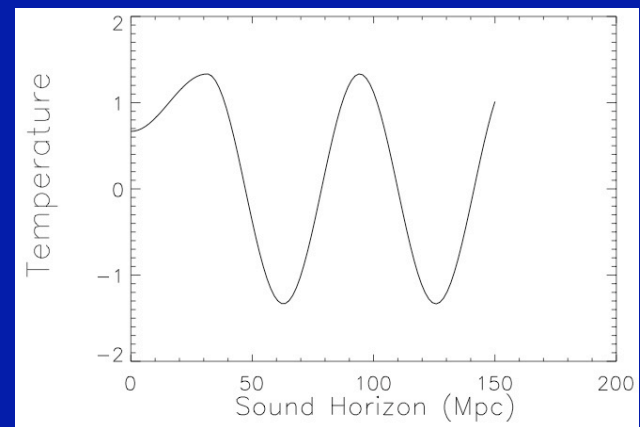
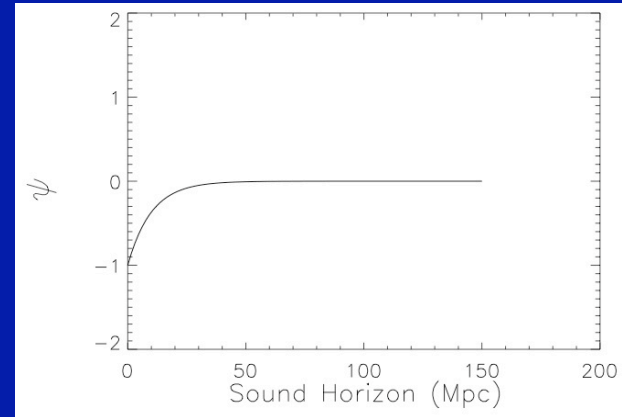
## Evolution Assuming Radiation Domination



## Evolution Assuming Matter Domination

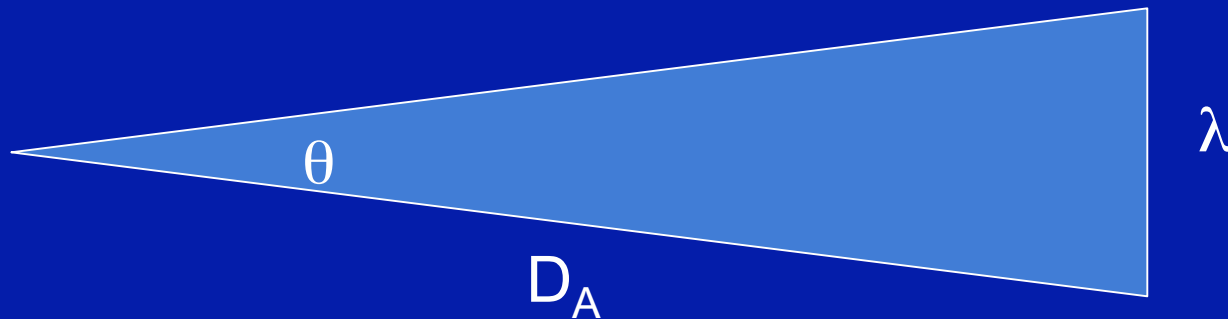


## Evolution Assuming Radiation Domination



$r_{\text{EQ}} = H^{-1}_{\text{EQ}}/a_{\text{EQ}}$  is an  
important length scale

The amplitude of the “radiation driving” effect is controlled by the ratio of matter to radiation when oscillations begin (when  $\lambda = H^{-1}/a$ ) and therefore by  $\theta/\theta_{\text{EQ}} = \lambda/r_{\text{EQ}}$ .

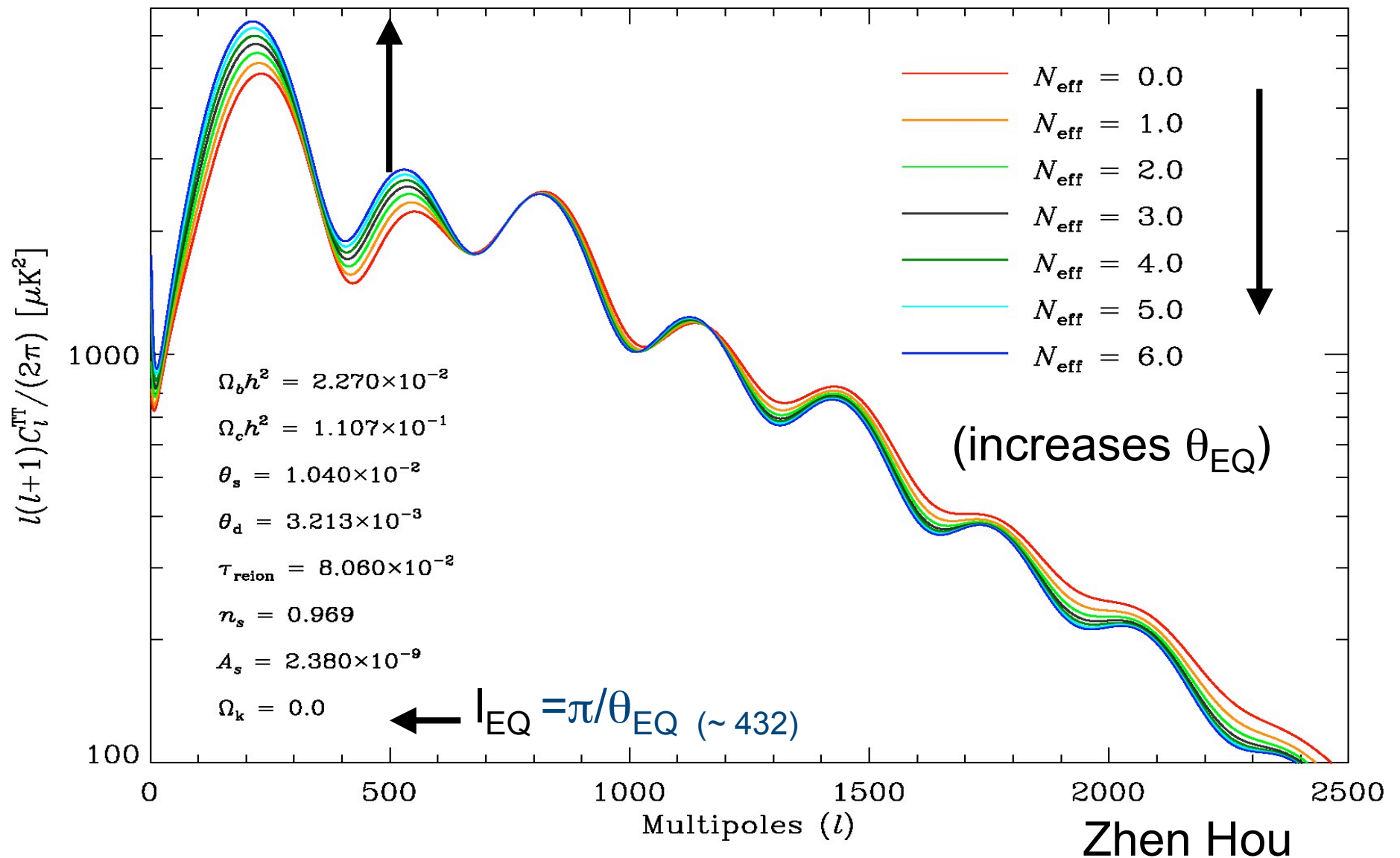


$$\theta_{\text{EQ}} = r_{\text{EQ}}/D_A$$

$$l = \pi/\theta$$

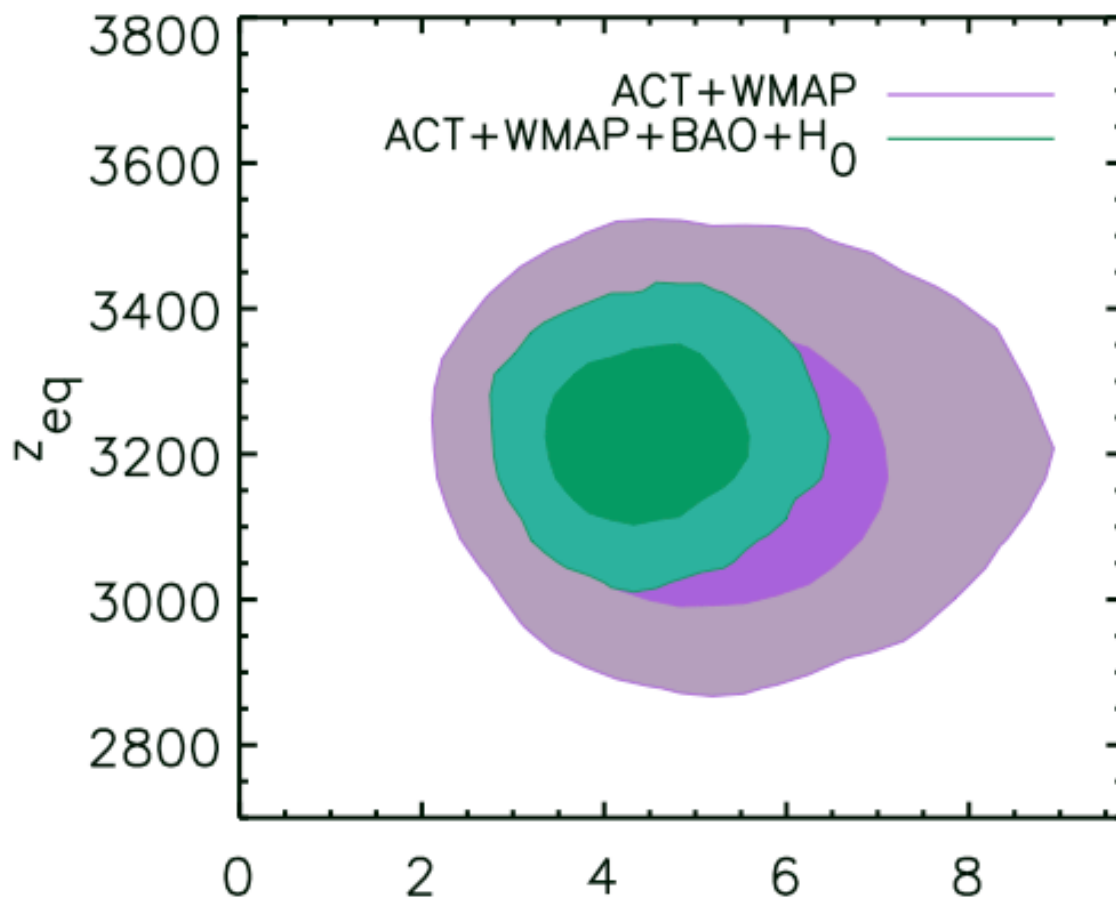
$$l_{\text{EQ}} = \pi/\theta_{\text{EQ}}$$

# Changing $\theta_{\text{EQ}}$ at fixed $\theta_s$ and $\theta_d$





$\theta_{\text{EQ}} = I(\Omega_m) / \sqrt{1 + z_{\text{EQ}}}$  where  $I(\Omega_m)$  is a very slowly-varying function of  $\Omega_m$



Dunkley et al. (2010)  $N_{\text{eff}}$

As  $N_{\text{eff}}$  is varied,  $\rho_m$  is increased to keep  $z_{\text{EQ}}$  (and therefore  $\theta_{\text{EQ}}$ ) fixed, because  $\theta_{\text{EQ}}$  is robustly determined by the data.

Komatsu et al. (2010)

# The Sound Horizon

sound horizon: distance sound could travel by the time of last scattering.



$\Theta_0 + \Psi \sim \cos(kr_s(\eta))$  so  $kr_s(\eta_*) = kr_s$  controls oscillation phase at last scattering and therefore whether  $k$  corresponds to a peak or a trough. Or if you want to swap  $l$  for  $k$ :

$kr_s = kD_A (r_s/D_A) = l\theta_s$   $l\theta_s$  controls oscillation phase of mode that projects to multipole moment  $l$ .

# Effect of extra $\nu$ on $r_s$

$$100 \theta_s = 1.04 \pm 0.0016$$

Keisler et al. (2011)

sound horizon: distance sound could travel by the time of last scattering.  $\theta_s$  controls peak locations.



$$r_s = \int_0^{a^*} c_s da / (a^2 H)$$

Extra  $\nu \implies$  higher  $\rho \implies$  higher  $H \implies$  takes less time to cool to  $T_{\text{rec}} \implies r_s$  is smaller

$$H^2 = 8\pi G\rho/3$$

**If** we knew  $D_A$  we could find  $r_s = \theta_s D_A$  and determine  $H$

# Effect of extra $\nu$ on $r_d$

Random-walk so goes as sq. root of time  $\implies r_d \sim 1/H^{0.5}$

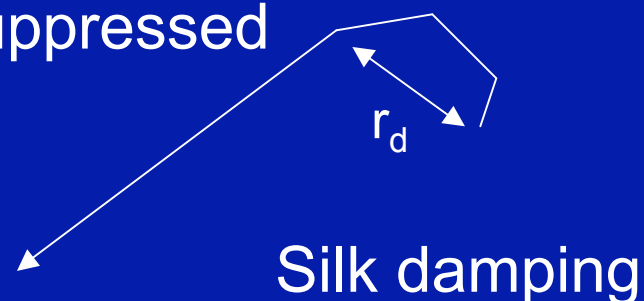
(Remember  $r_s \sim 1/H$ )

$$\theta_d/\theta_s = r_d/r_s \sim H^{0.5}$$

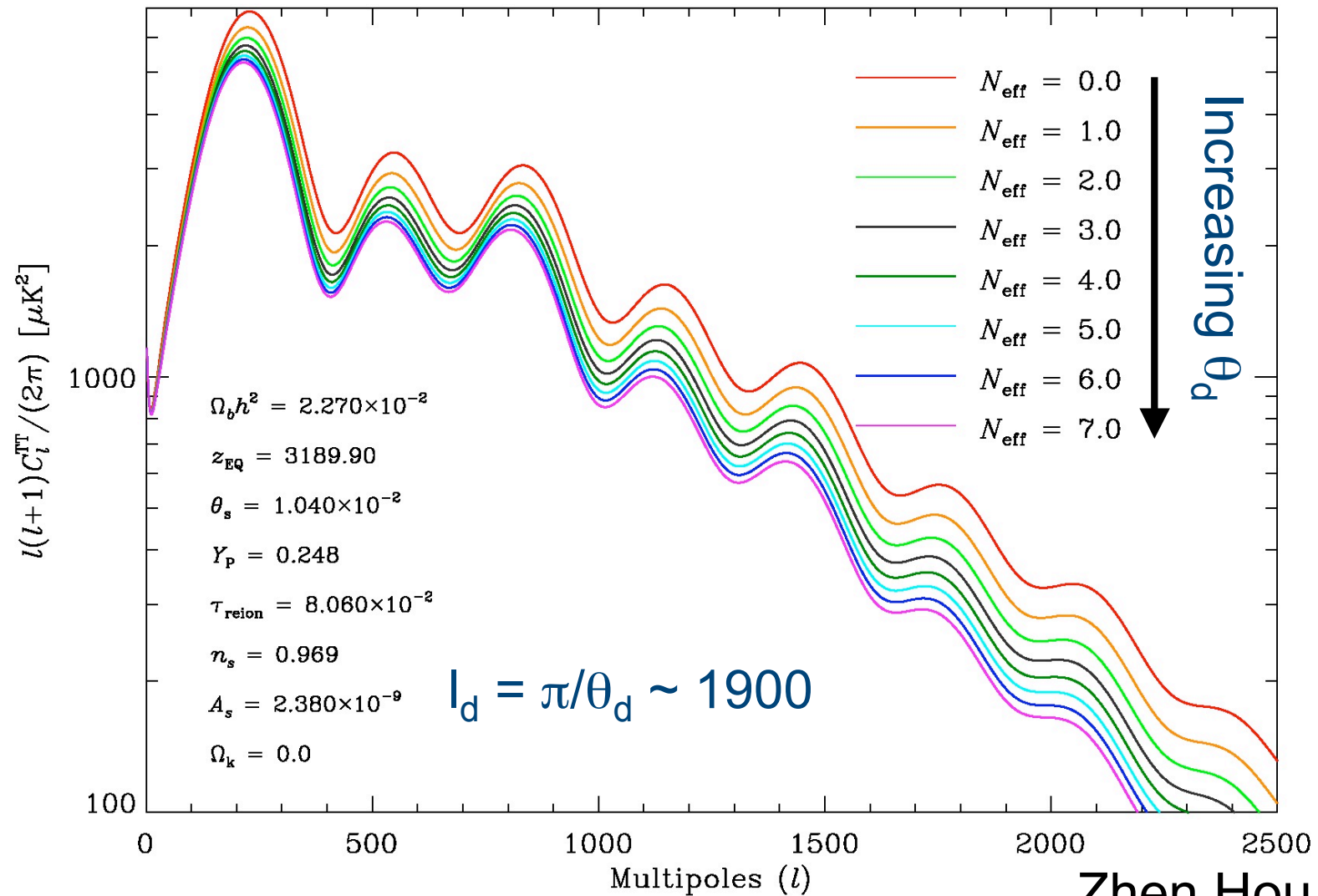
Dependence on  $D_A$  has  
dropped out!



Modes with  $\lambda < r_d$  are  
suppressed



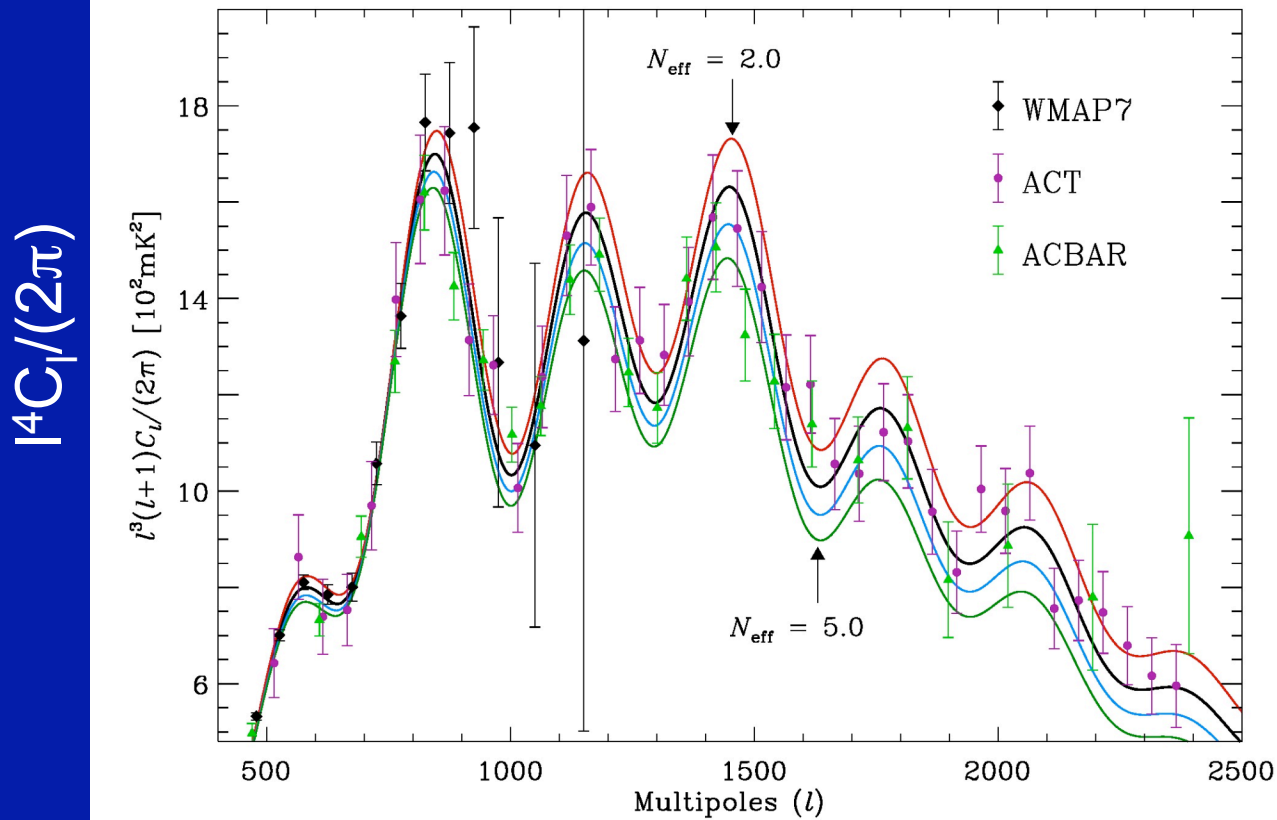
# Changing $\theta_d$ at fixed $\theta_{\text{EQ}}$ and $\theta_s$



Zhen Hou

# Increasing $N_{\text{eff}}$ increases $\theta_d$ , reducing small-scale power

Hou, Keisler, LK, Millea & Reichardt (2011)

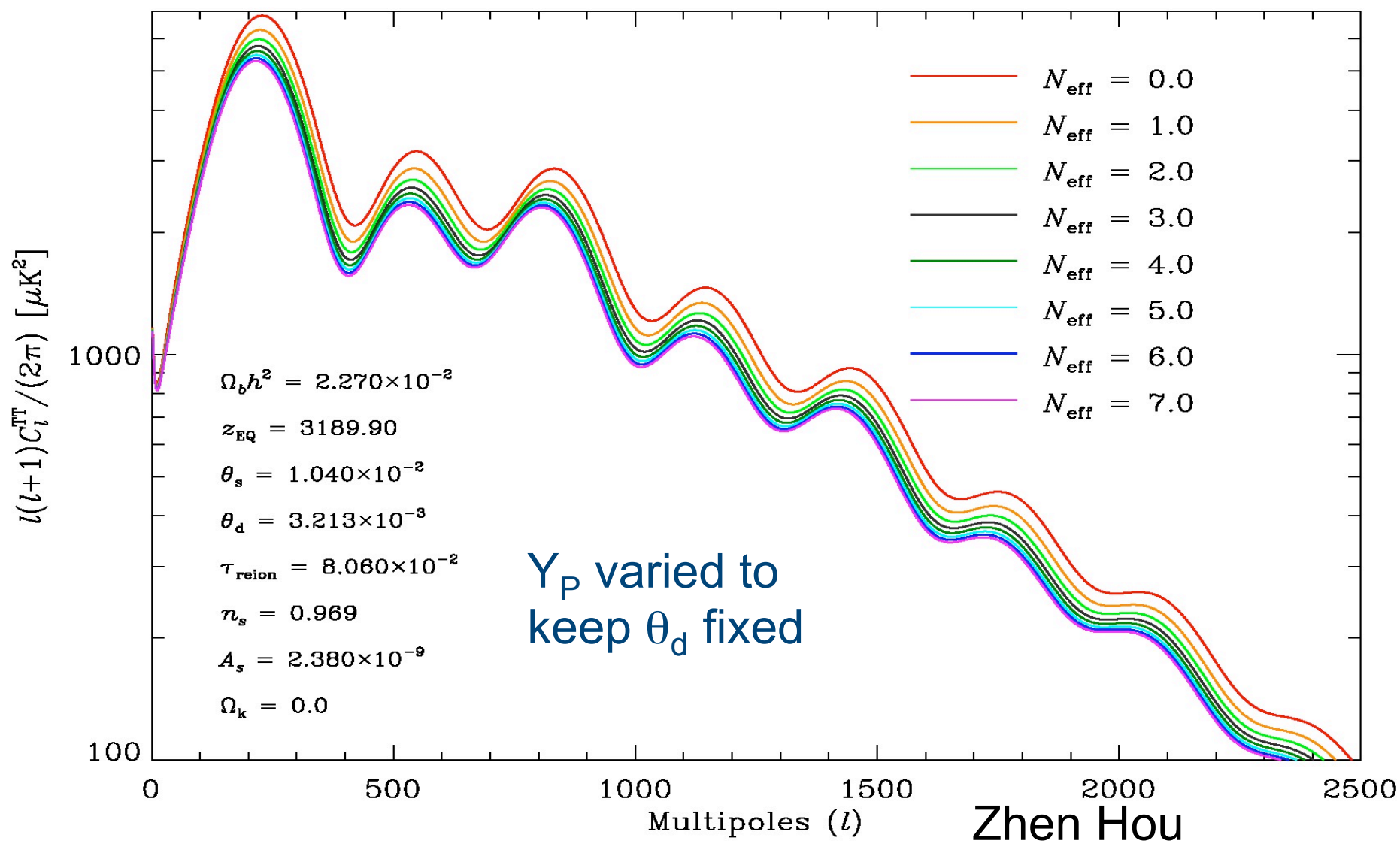


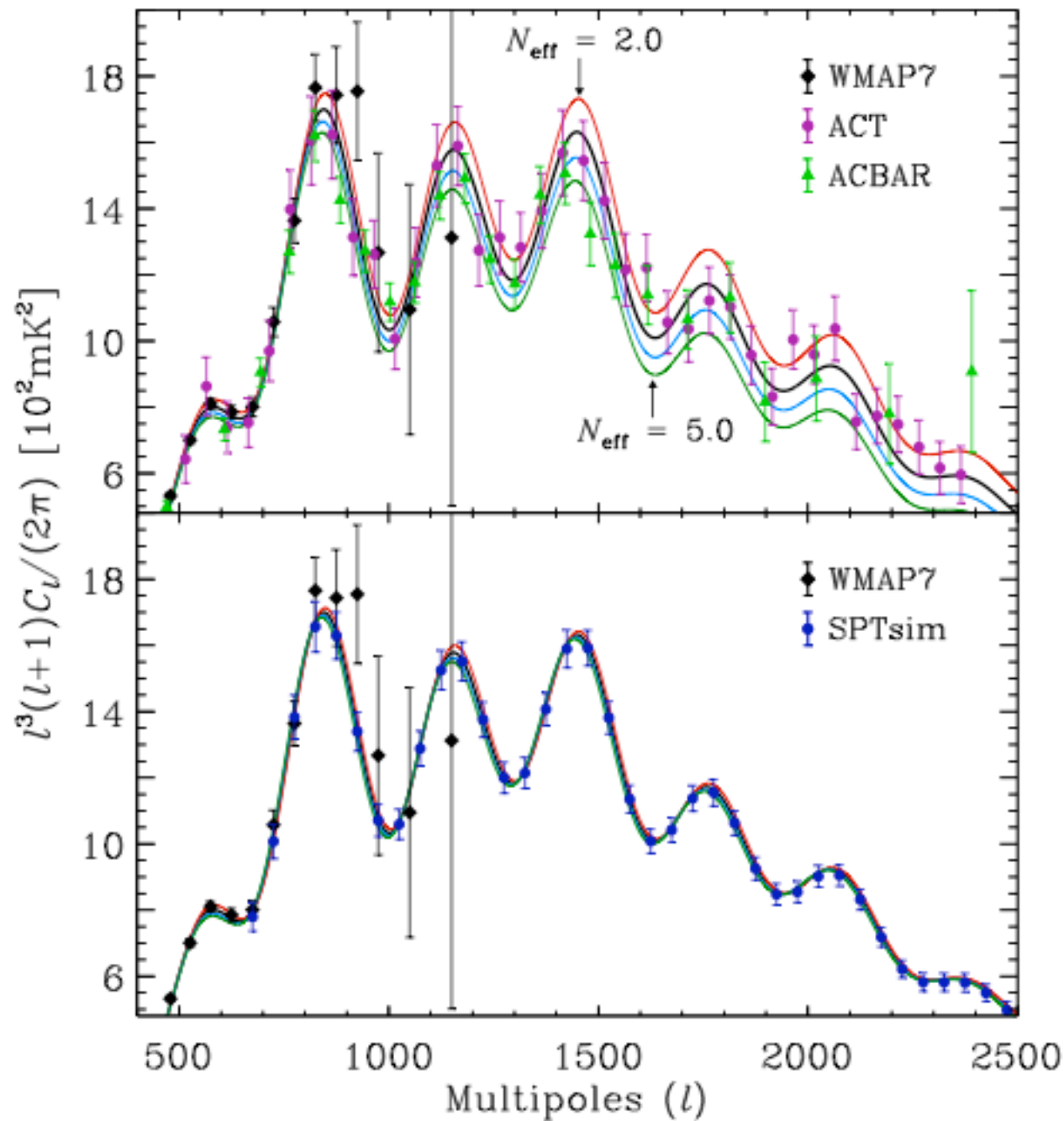
98.4%  
confidence  
that  $N_{\text{eff}} >$   
standard  
model value  
(Hou et al.  
2011)

$N_{\text{eff}}$  is increased here from 2 to 5 with fixed  $\theta_{\text{EQ}}$  and  $\theta_s$ .

To fix  $\theta_{\text{EQ}}$  we increase  $\rho_{\text{cdm}}$ . To fix  $\theta_s$  we adjust  $\rho_{\Lambda}$  to change  $D_{\Lambda}$ .

# Changing $N_{\text{eff}}$ at fixed $\theta_d$ , $\theta_{\text{EQ}}$ and $\theta_s$





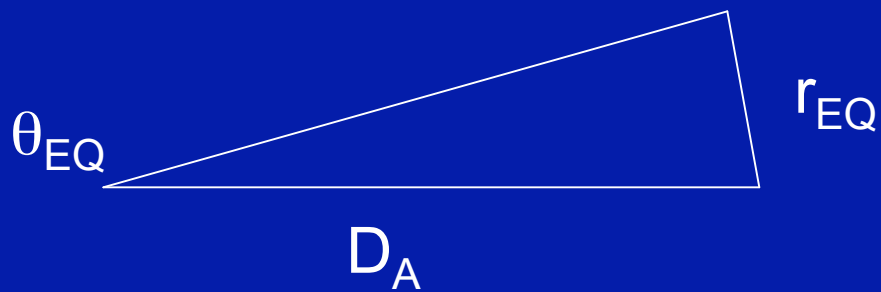
Same models but with  $\theta_d$  fixed as well (by varying the Helium fraction).

The effect is indeed due to change to  $\theta_d$

Bashinsky & Seljak (2004)



# Summary of Three Scales



$r_{EQ}$  controls radiation driving  
sound horizon: distance  
sound could travel by  
the time of last  
scattering.  $\theta/\theta_s$  controls  
oscillation phase at last  
scattering.



Modes with  $\lambda < r_d$  are  
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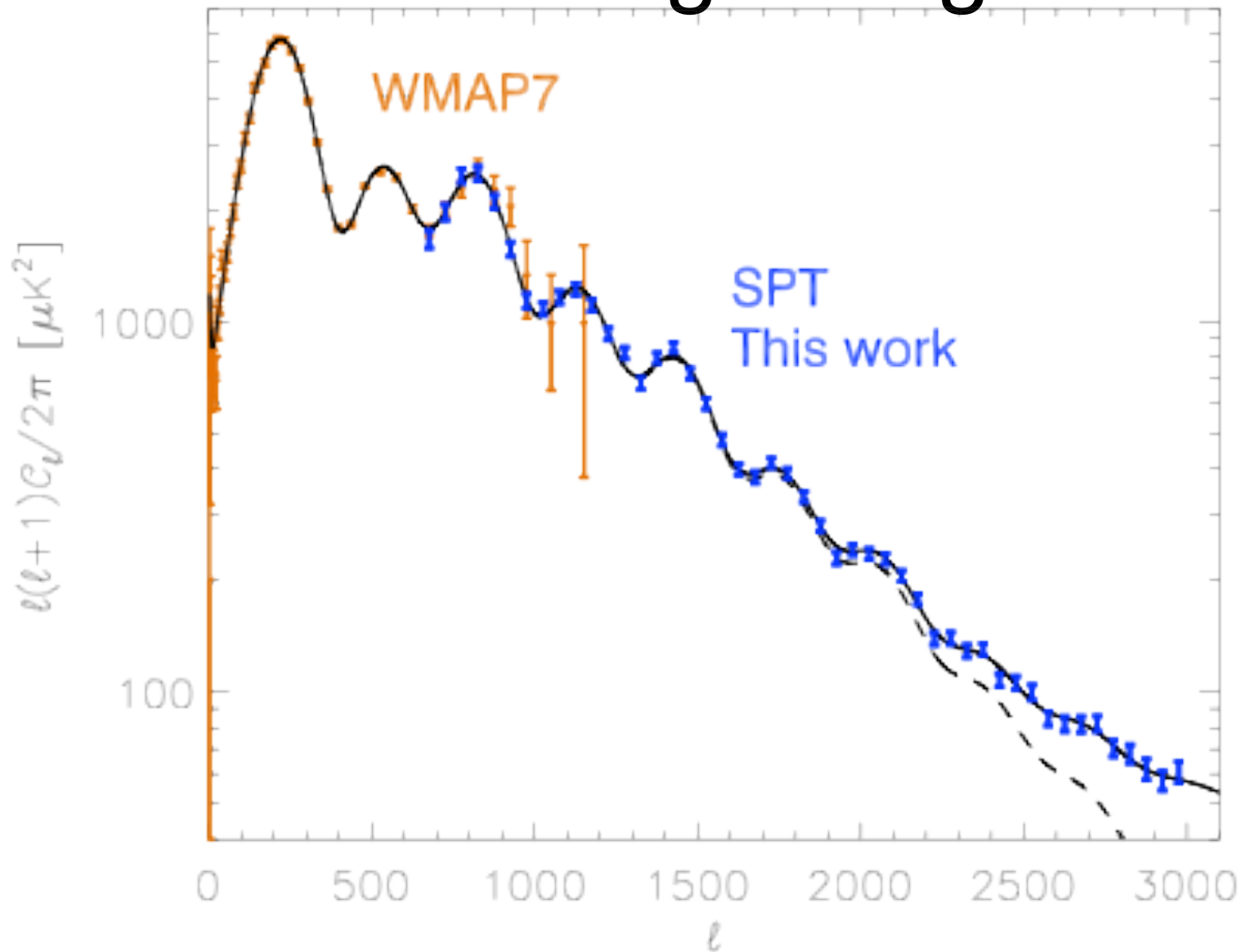


Silk damping

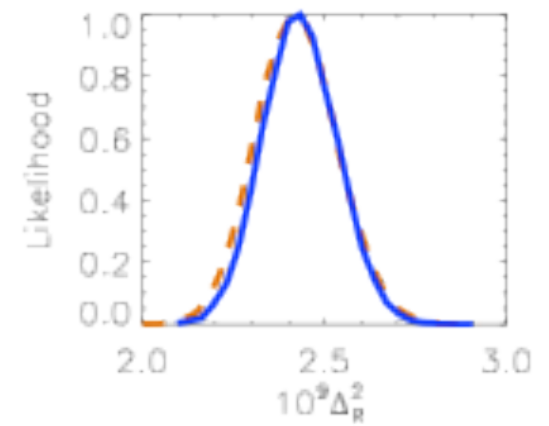
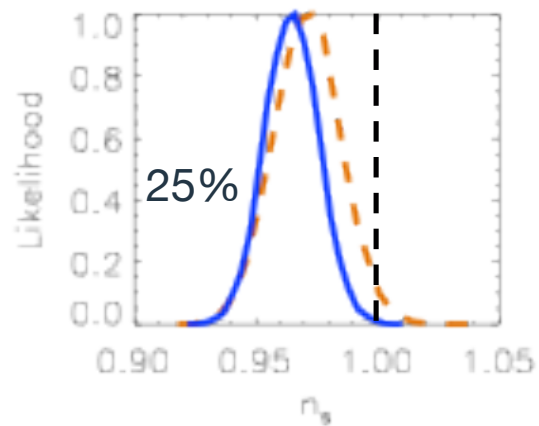
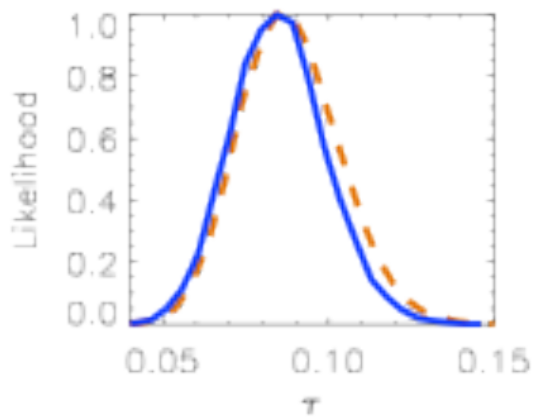
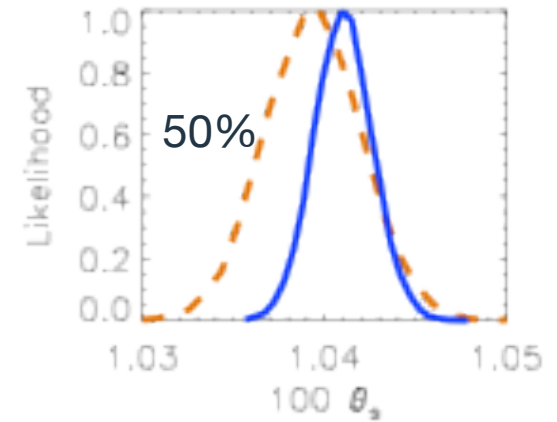
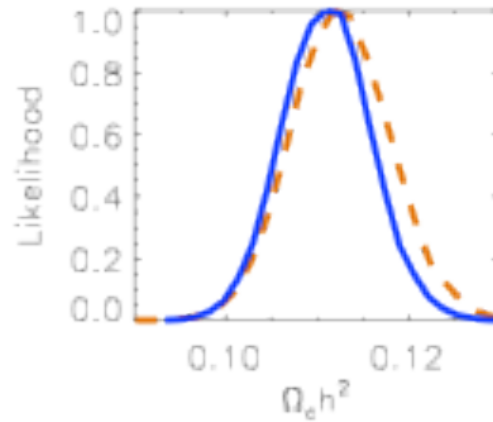
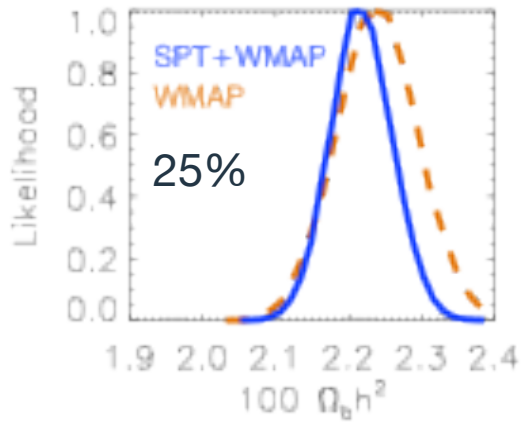
# Outline

- CMB Theory for CMB Experimentalists
  - A Transfer Function Controlled by Three Angular Scales
- What we can learn from the damping tail
- Non-CMB evidence for neutrinos

SPT error bars are small  
and over large range in  $\ell$



# SPT provides modest improvement on 6 “vanilla” cosmo parameters



# Six-parameter Model

## Assumptions

Input spectrum parameters

Transfer function parameters

A

$n_s$

$\tau$

$\rho_b$

$\rho_m$

$\rho_\Lambda$

1) Standard radiation content ( $T_\gamma$  from FIRAS, 3 SM neutrinos)

2)  $Y_P = f(N_{\text{eff}}, \rho_b)$

3)  $dn_s/d\ln k = 0$

4) Dark energy =  $\Lambda$  and  $\Omega_k = 0$

# Six-parameter Model

## Assumptions

Input spectrum parameters

Transfer function parameters

- 1) Standard radiation content ( $T_\gamma$  from FIRAS, 3 SM neutrinos)
- 2)  $Y_P = f(N_{\text{eff}}, \rho_b)$
- 3)  $dn_s/d\ln k = 0$
- 4) Dark energy =  $\Lambda$  and  $\Omega_k = 0$

A

$\tau$

$n_s$

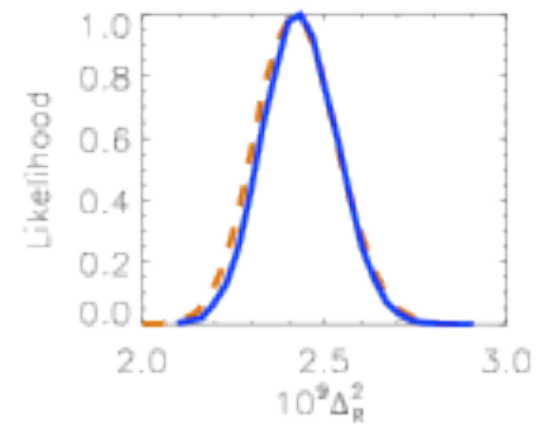
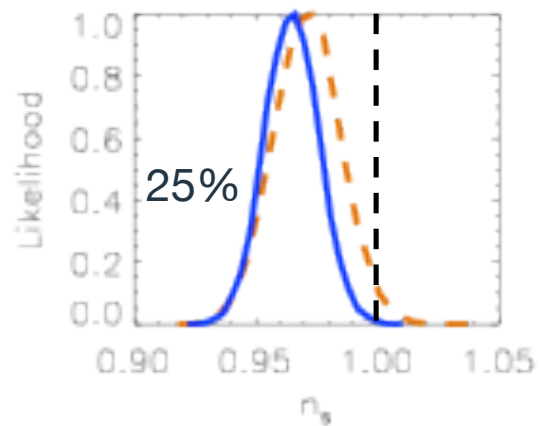
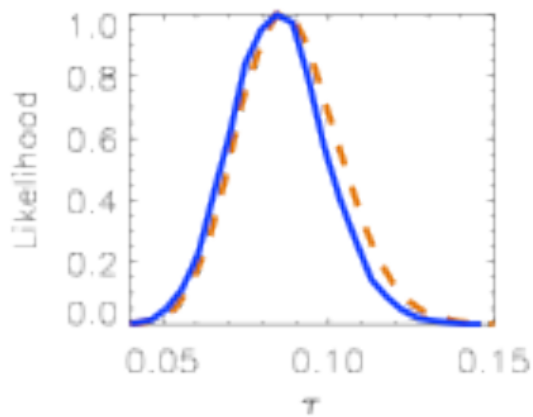
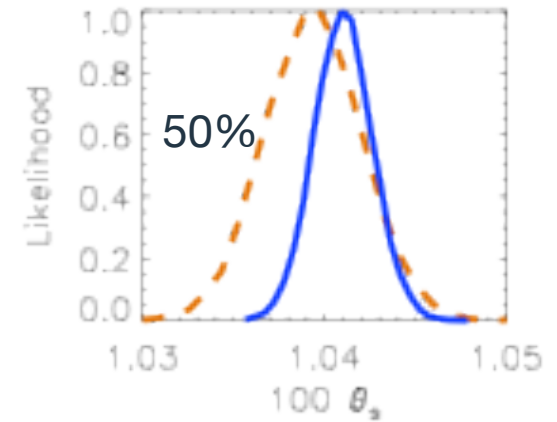
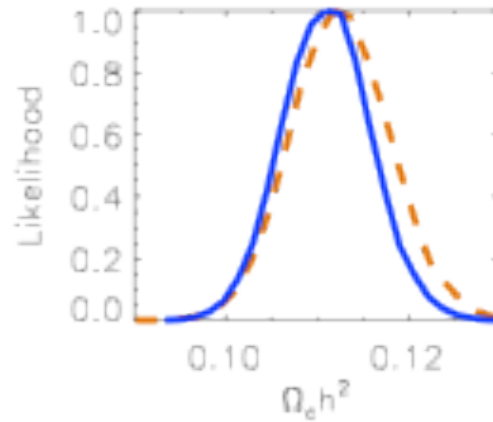
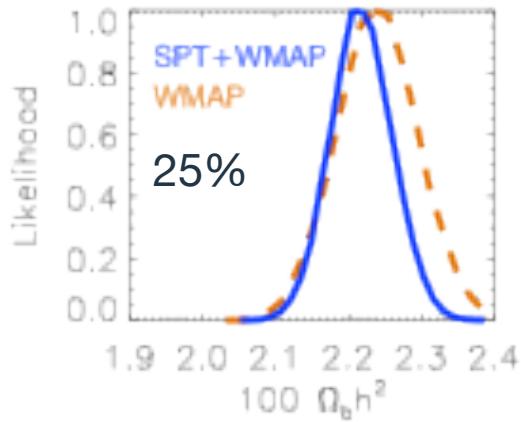
$\rho_b$

$\rho_m$  ( $\theta_{\text{EQ}}$ )

$\rho_\Lambda$  ( $\theta_s$ )

For WMAP7, effects that lead to constraints on  $\tau$ ,  $\rho_b$  and  $\rho_m$  are gone at higher  $ell$ .

# SPT provides modest improvement on 6 “vanilla” cosmo parameters



# Six-parameter Model

## Assumptions

Input spectrum parameters

Transfer function parameters

1) Standard radiation content ( $T_\gamma$  from FIRAS, 3 SM neutrinos)

A

$\tau$

2)  $Y_p = 0.24$

$n_s$

$\rho_b$

3)  $dn_s/d\ln k = 0$

$\rho_m$  ( $\theta_{EQ}$ )

$\rho_\Lambda$  ( $\theta_s$ )

4) Dark energy =  $\Lambda$  and  $\Omega_k = 0$

High ell data ==> sensitive to  $\theta_d$ , which can be predicted from  $\rho_b, \rho_m, \rho_\Lambda$  which are already determined from low ell.



SPT provides a strong test of the 6-parameter model rather than great refinement of the parameter values

$\theta_d$  predicted

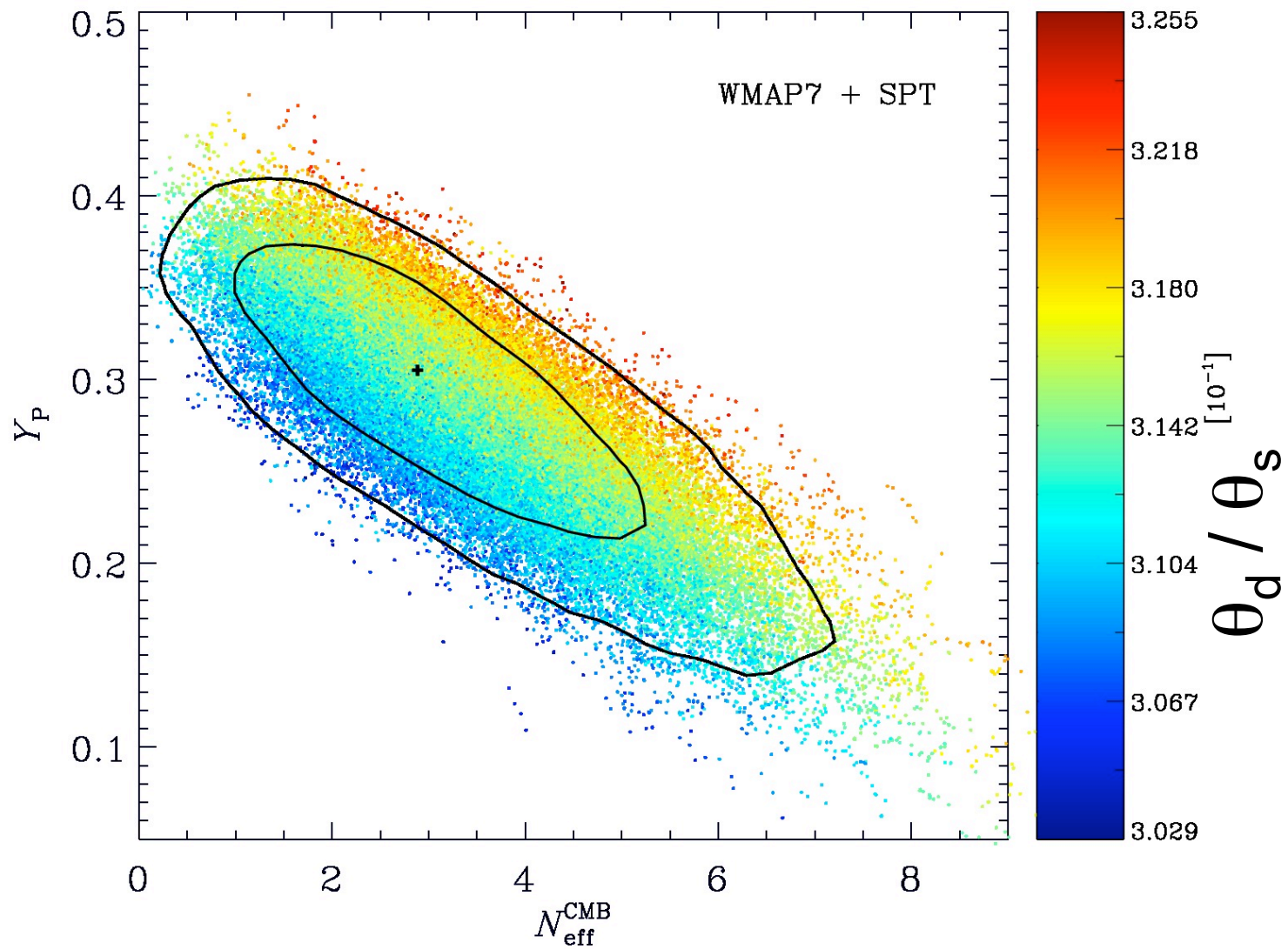
How does the prediction compare with measurement?

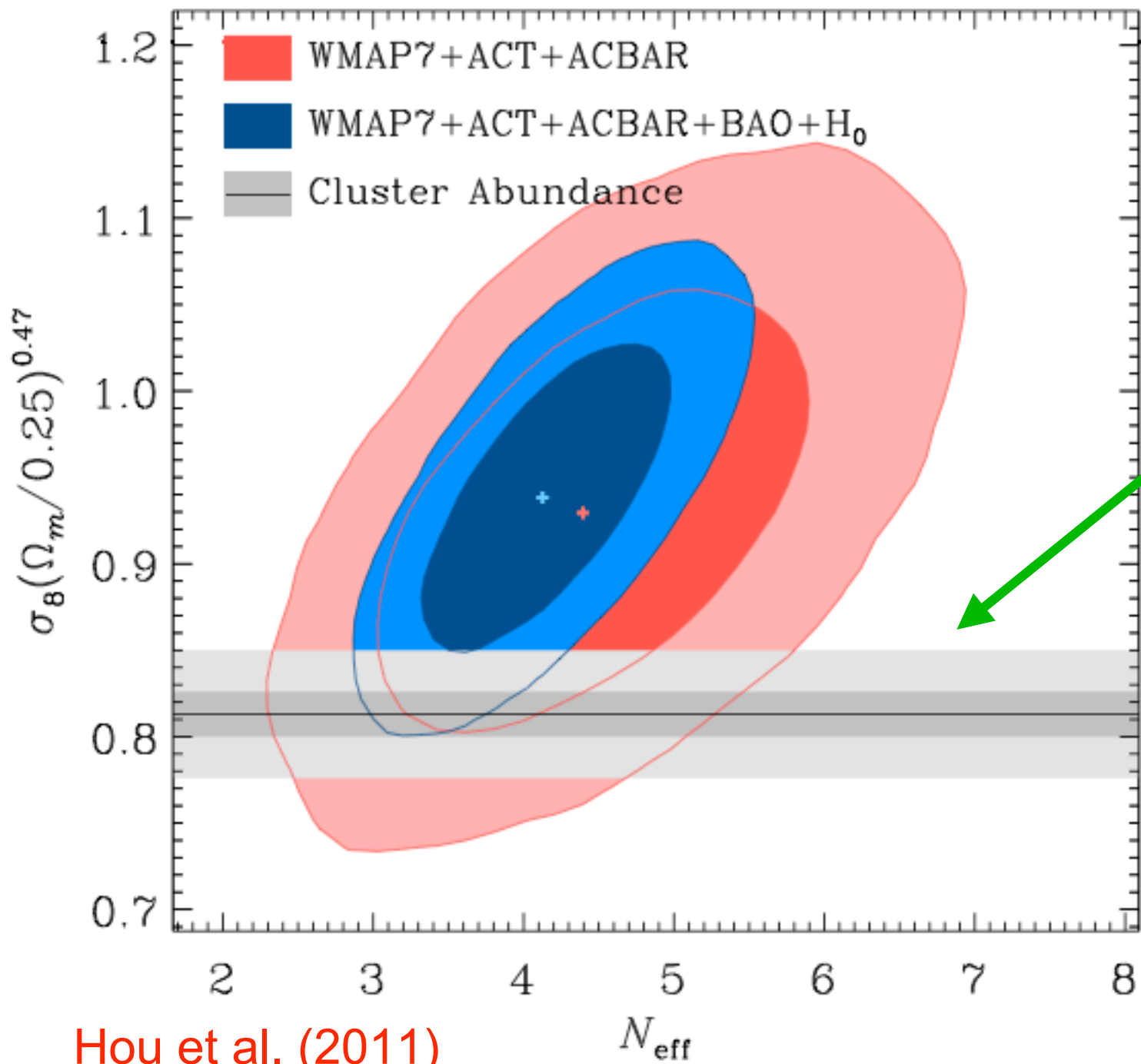
Mild preference ( $\sim 1.7\sigma$ ) for models with less power in damping tail than for the best-fit 6-parameter model

## Constraints on Extensions

	WMAP7+SPT	WMAP7+SPT +BAO+H <sub>0</sub>
$\theta_d$ { N <sub>eff</sub> (3.046)	3.85 +/-0.62	3.86 +/-0.42
Y <sub>P</sub> (0.24)	0.296 +/-0.030	0.30 +/- 0.030
dn <sub>s</sub> /dlnk ((1-n <sub>s</sub> ) <sup>2</sup> = 0)	-0.024 +/- 0.013	-0.020 +/- 0.012
r	< 0.21 @ 95% confidence	< 0.17 @ 95% confidence

# $N_{\text{eff}}$ vs $Y_{\text{p}}$





Vikhlinin et al. (2009) constraint from X-ray cluster abundances

Hou et al. (2011)

# Low z cluster abundances break degeneracies

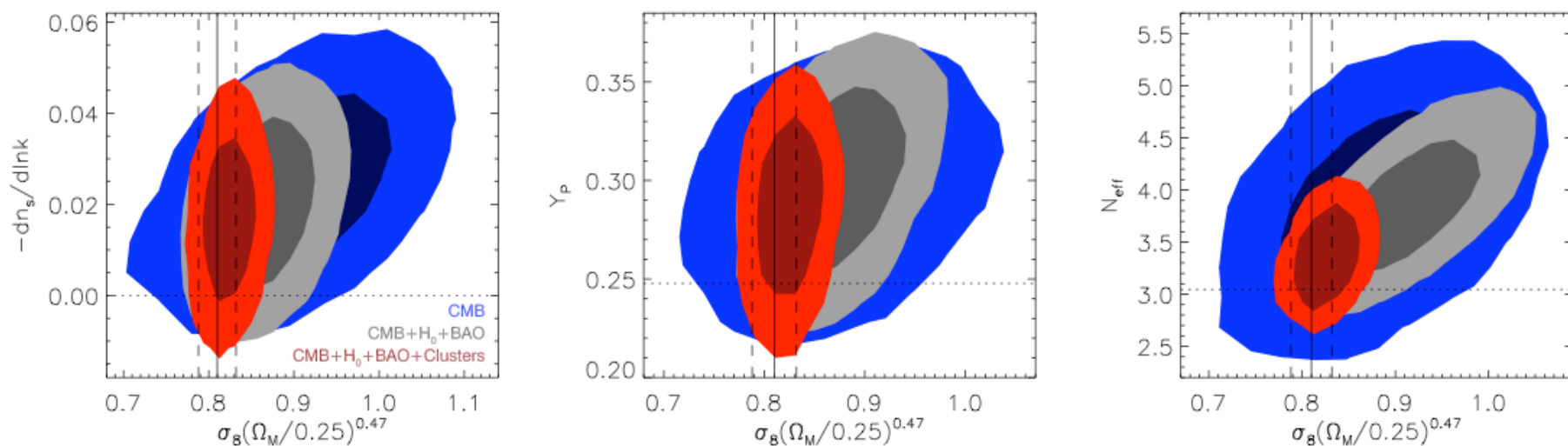


FIG. 14.— The two-dimensional marginalized constraint on spectral running, primordial helium, or the effective number of relativistic species versus the combination  $\sigma_8(\Omega_M/0.25)^{0.47}$ , which is well constrained by the cluster abundance measurement of Vikhlinin et al. (2009). “CMB” corresponds to SPT+WMAP7. The constraint on  $\sigma_8(\Omega_M/0.25)^{0.47}$  from the clusters and the corresponding  $1\sigma$  uncertainties are shown by the vertical lines. The standard values of the spectral running, primordial helium, and the effective number of relativistic species are shown by the dotted horizontal lines. Adding the cluster abundance information moves the constraints on these parameters closer to their standard values.

# Outline

- CMB Theory for CMB Experimentalists
  - A Transfer Function Controlled by Three Angular Scales
- Why do “standard” constraints improve so little?
- What we can learn from the damping tail
- Non-CMB evidence for extra neutrinos

# Neutrino Fever

# Neutrino Fever

6. [arXiv:1006.5276](#) [[pdf](#), [ps](#), [other](#)]

## **Cosmology seeking friendship with sterile neutrinos**

[Jan Hamann](#), [Steen Hannestad](#), [Georg G. Raffelt](#), [Irene Tamborra](#), [Yvonne Y.Y. Wong](#)

Comments: 4 pages, 1 figure, matches version published in PRL

Journal-ref: Phys.Rev.Lett.105:181301,2010

Subjects: **High Energy Physics – Phenomenology (hep-ph)**; Cosmology and Extragalactic Astrophysics (astro-ph.CO)



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Phys. Rev. Lett. 105, 181301 (2010) [4 pages]

## Cosmology Favoring Extra Radiation and Sub-eV Mass Sterile Neutrinos as an Option

Abstract

References

Citing Articles (10)

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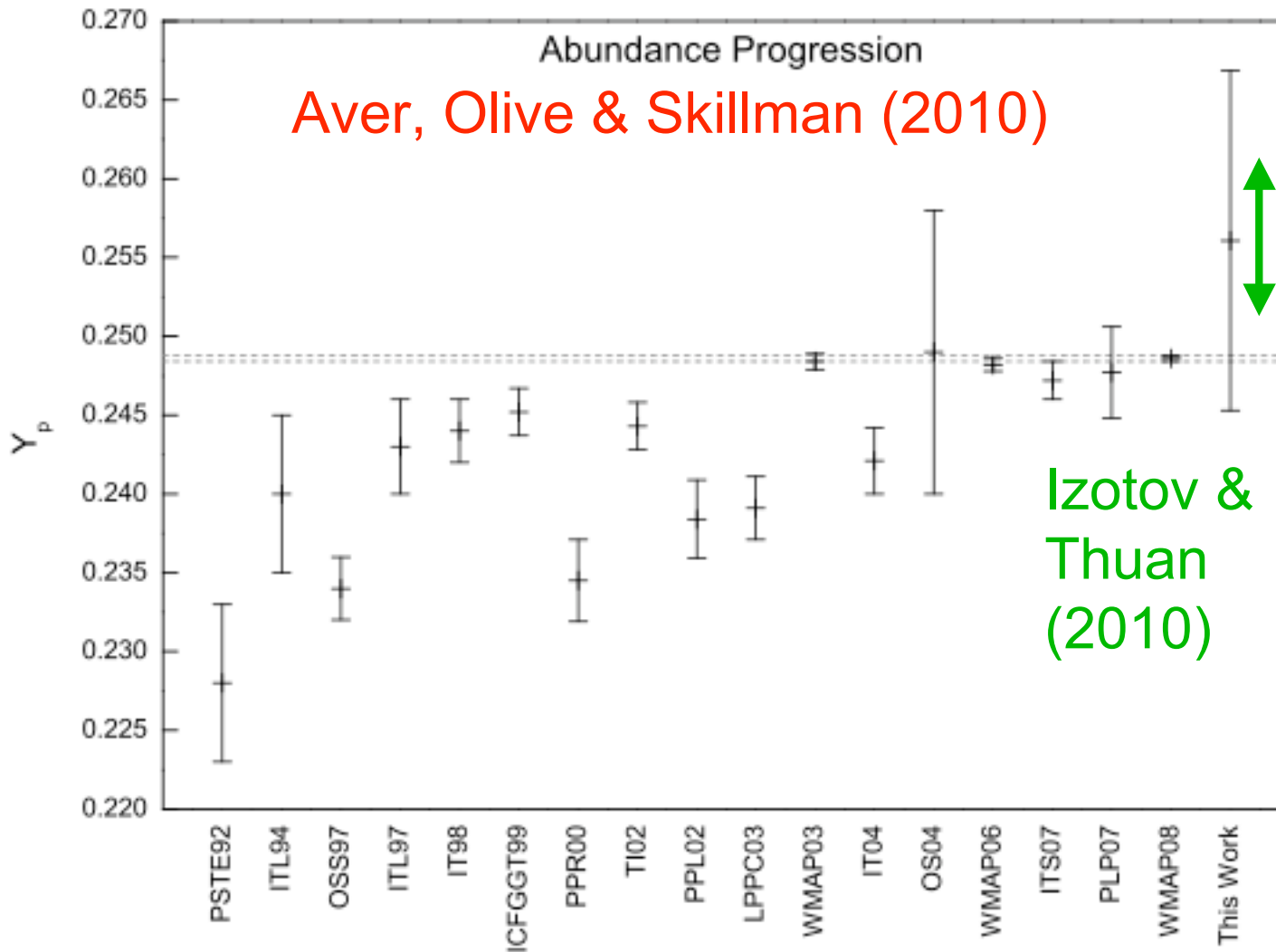
[Jan Hamann](#)<sup>1</sup>, [Steen Hannestad](#)<sup>1</sup>, [Georg G. Raffelt](#)<sup>2</sup>, [Irene Tamborra](#)<sup>2,3,4</sup>, and [Yvonne Y. Y. Wong](#)<sup>5</sup>

# Extra Cosmological Neutrinos?

## Arguments For

- Mild preference for lower damping tail power than in standard cosmological model.
- Measurements of  $Y$  have increased in magnitude and uncertainty allowing  $N_{\text{eff}} = 4$  to be consistent with BBN and perhaps preferred (Izotov & Thuan 2010, Aver, Olive & Skillman 2010, 2011)
- Oscillation evidence for sterile neutrinos from mini-Boone / LSND / Minos
- Oscillation to sterile neutrinos can explain reactor anomalies too.

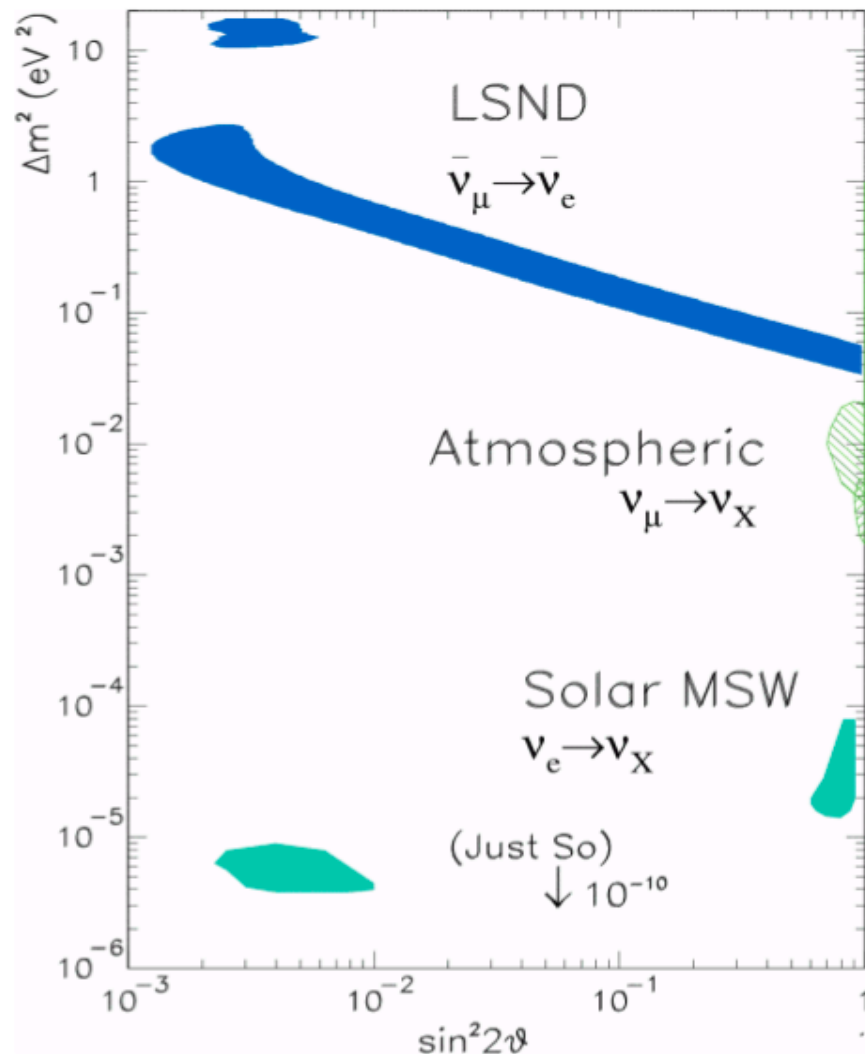
# $Y_p$ Measurements



From  
extragalactic  
regions of  
ionized low-  
metallicity  
gas

(except  
for WMAP  
points)

# Decade-old evidence for an $m \sim eV$ sterile neutrino



LEP proved that there are only three light neutrinos coupling to the  $Z^0$ .

Therefore there can be at most two neutrino mass difference scales.

But the oscillation results from atmospheric and solar neutrinos are well established.

If LSND is right it implies new physics such as a fourth neutrino that is sterile.

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# Extra Cosmological Neutrinos?

## Arguments For and Against

- Mild preference for lower damping tail power than in standard cosmological model.  $< 2\sigma$ , tension with  $\sigma_8$
- Measurements of  $Y$  have increased in magnitude and uncertainty allowing  $N_{\text{eff}} = 4$  to be consistent with BBN and perhaps preferred (Izotov & Thuan 2010, Aver, Olive & Skillman 2010, 2011)
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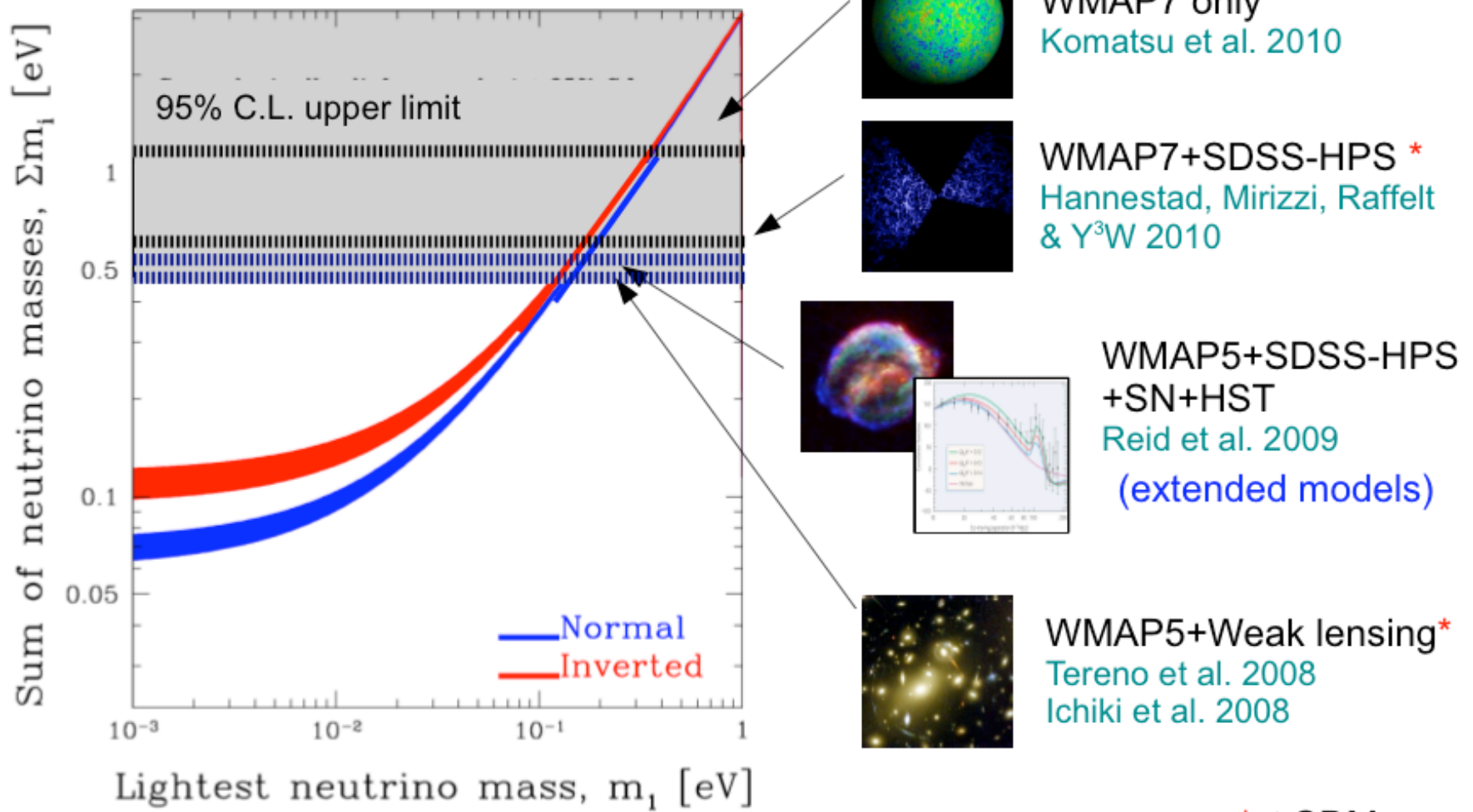
# Extra Cosmological Neutrinos?

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- Oscillation to sterile neutrinos can explain reactor anomalies too.   
only  $2\sigma$

Plus: we don't want a thermal background of 1eV mass sterile neutrinos!

## Present status...

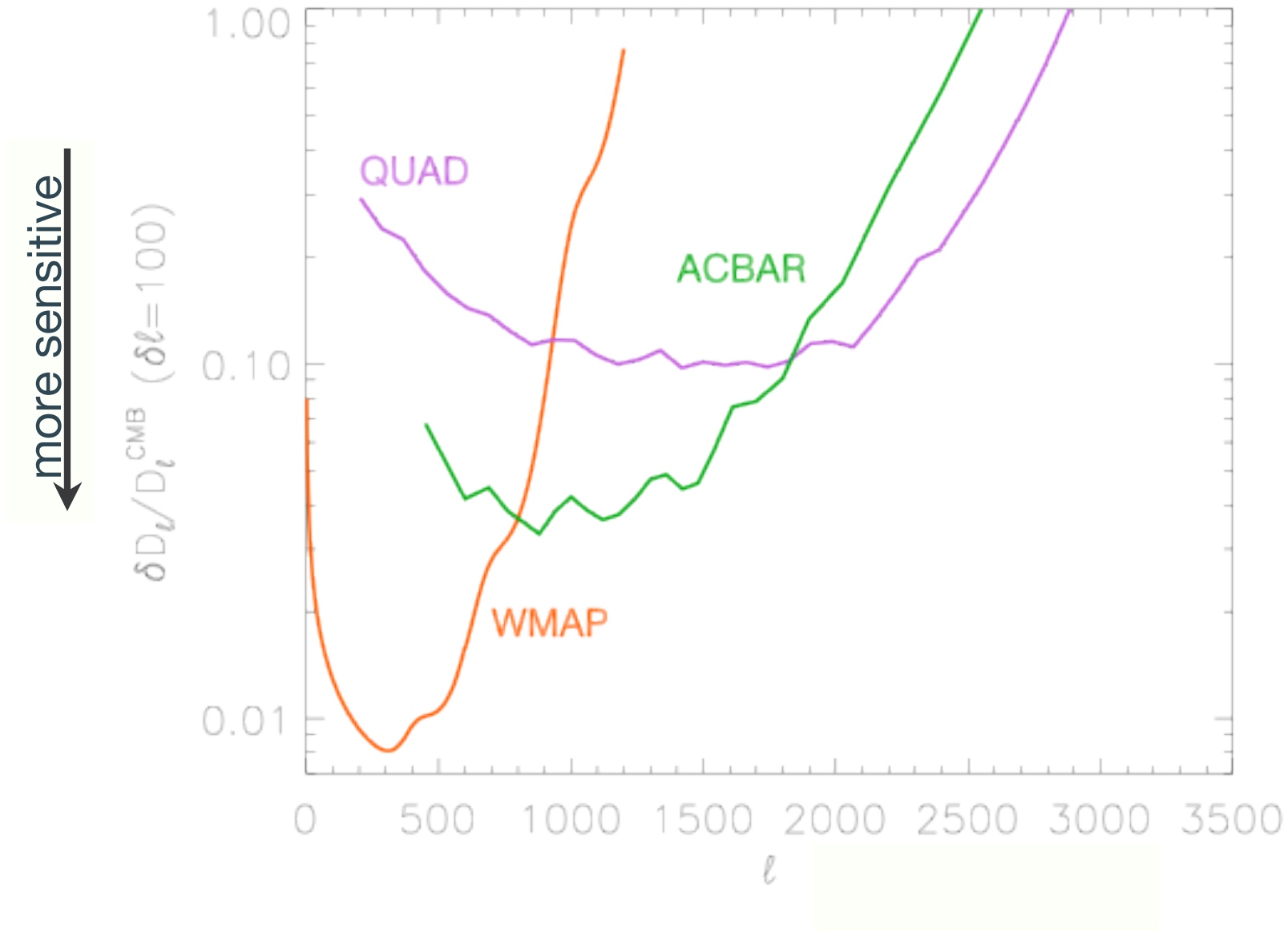


\*  $\Lambda$ CDM+ $m_\nu$

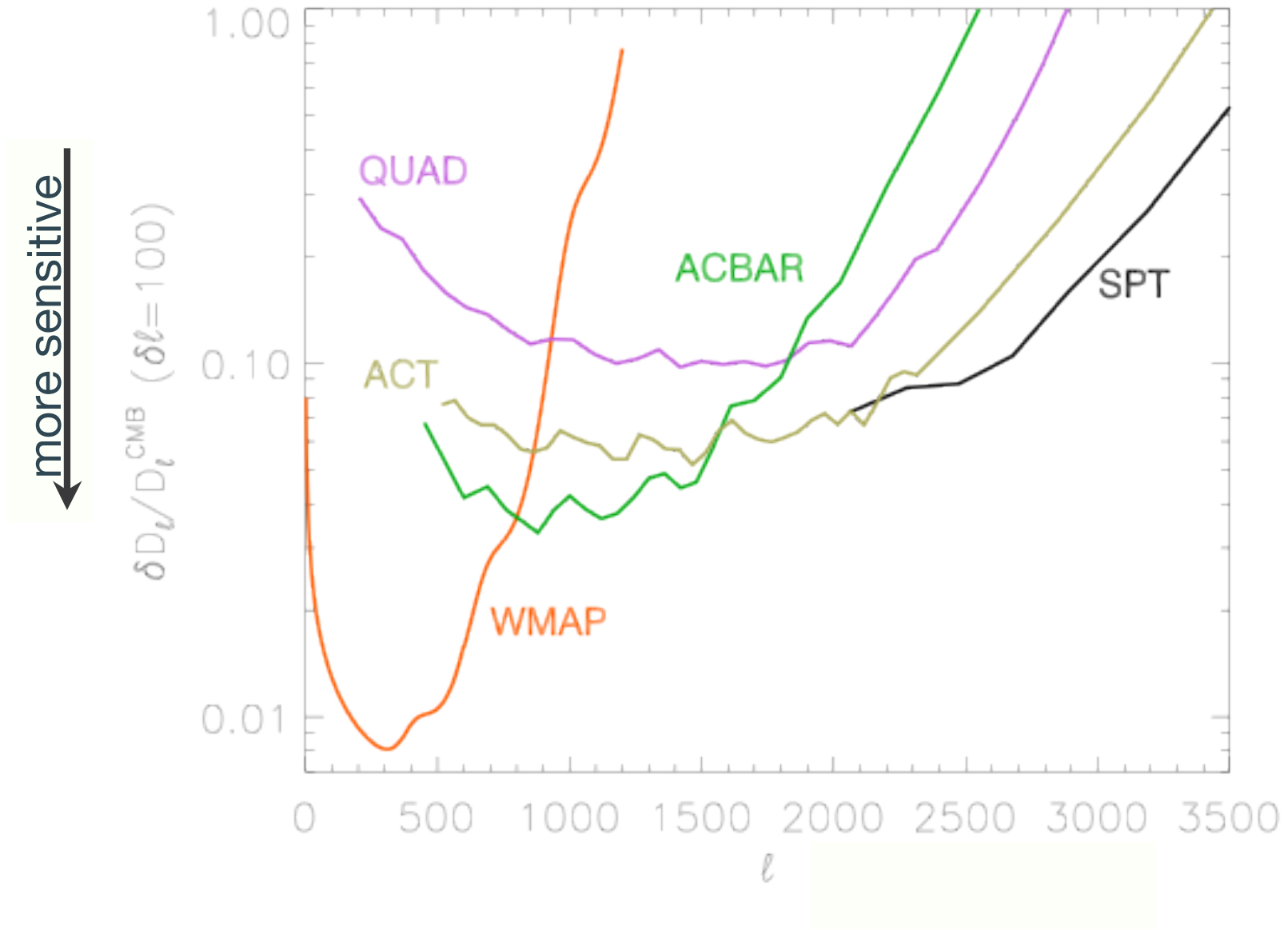
From Yvette Wong's Avignon presentation

# The Future

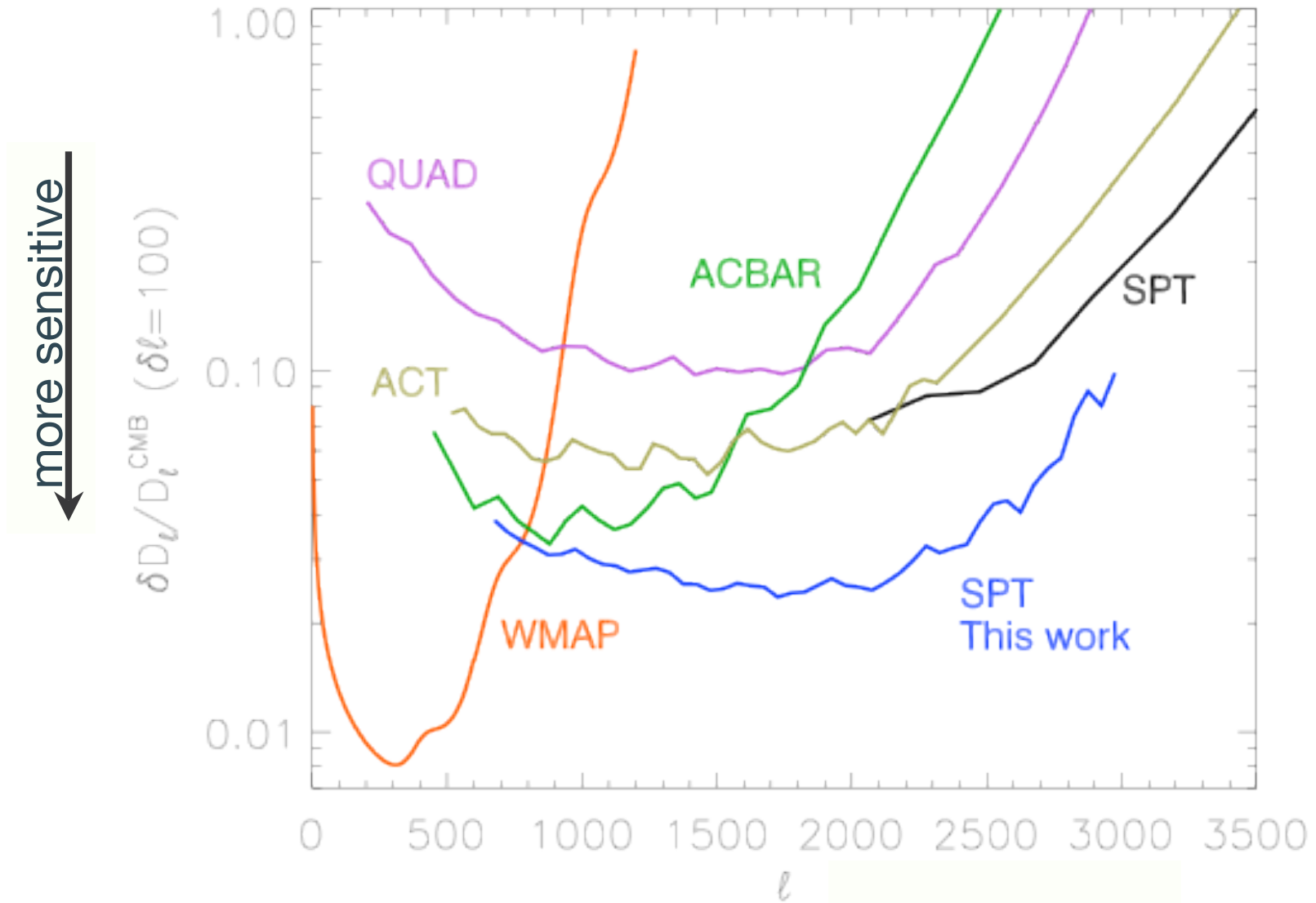
# lay of the land



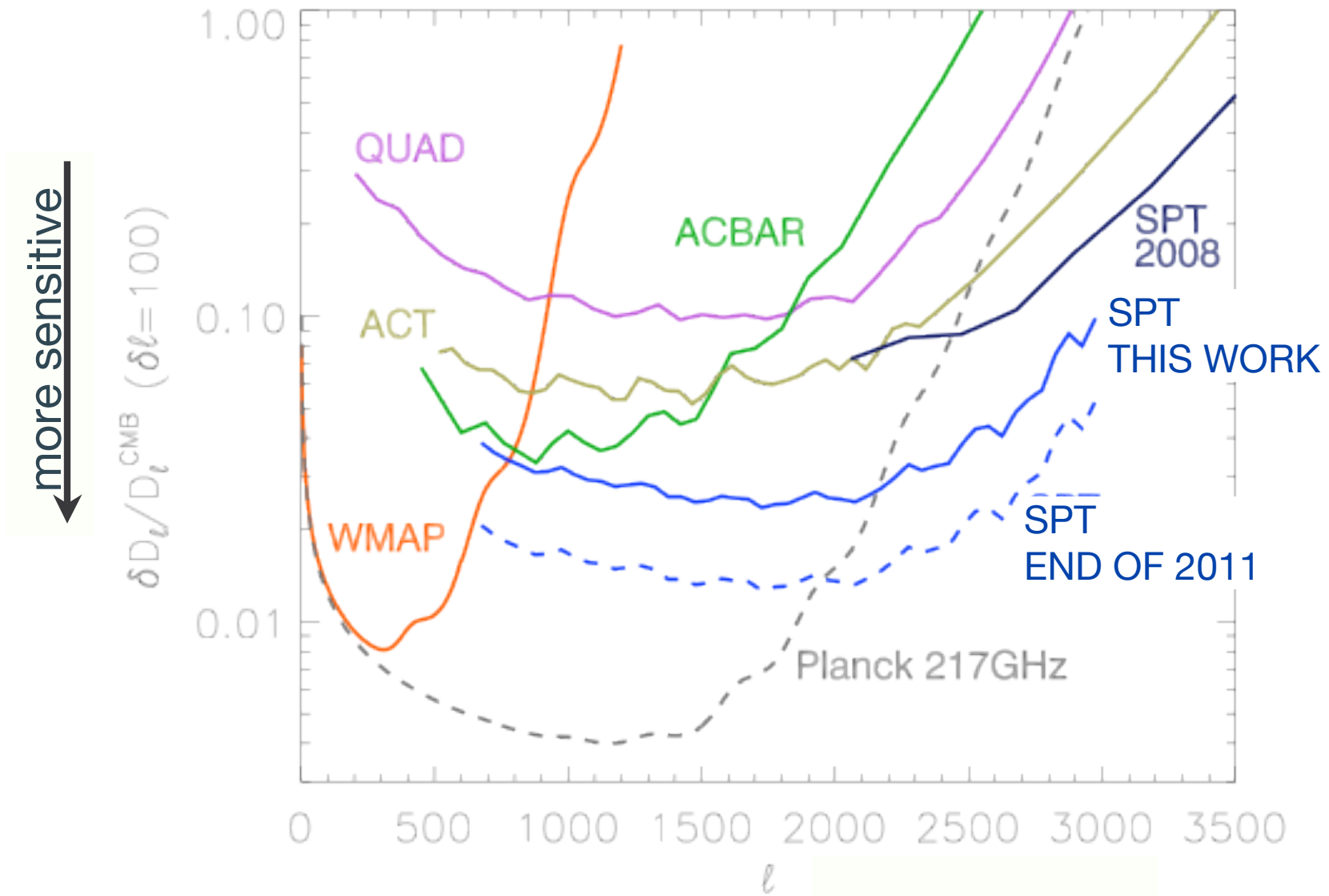
# lay of the land



# lay of the land

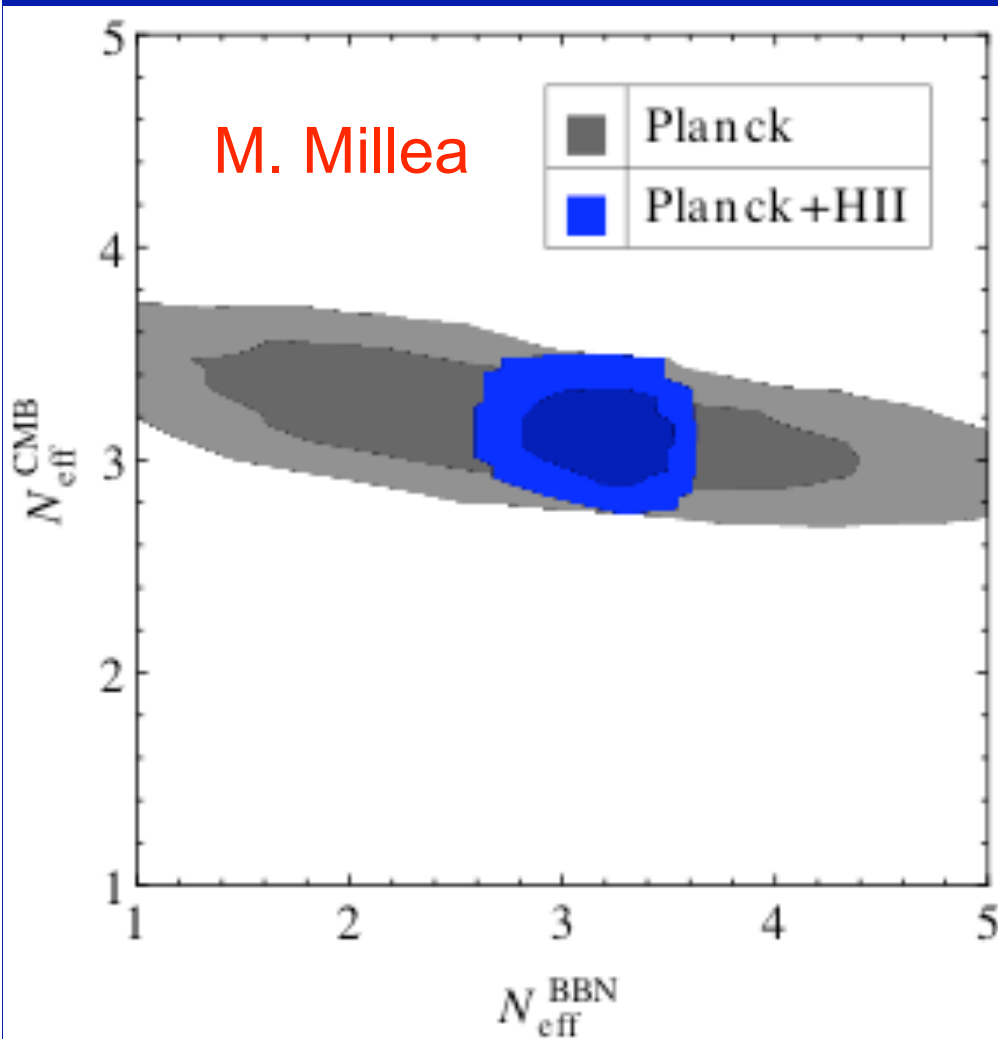


# lay of the land



# The Future

With better data we can relax assumption that  $N_{\text{eff}}^{\text{BBN}} = N_{\text{eff}}^{\text{CMB}}$  (so far assumed implicitly throughout this talk).



Forecast for Planck

Forecast for Planck +  $Y_{\text{p}}$  measurement with error same size as reported by Izotov & Thuan (2010).

With luck, these will disagree! (e.g. Fischler & Myers (2010))



# Summary and Conclusions

- SPT collaboration has measured CMB power spectrum at high resolution from 800 sq. deg.
- Results are consistent with the (very tight) predictions of the standard cosmological model.
- High-resolution observations allow us to probe the third angular scale in the CMB transfer function, which gives us sensitivity to the expansion rate leading up to recombination, as well as  $Y_p$ .
- Current data (including lab and reactor) do not paint a compelling picture for additional neutrinos.
- We are hopeful for surprises from Planck.