

# Gravitational-wave lensing within ground-based gravitational-wave detectors

Otto Akseli Hannuksela

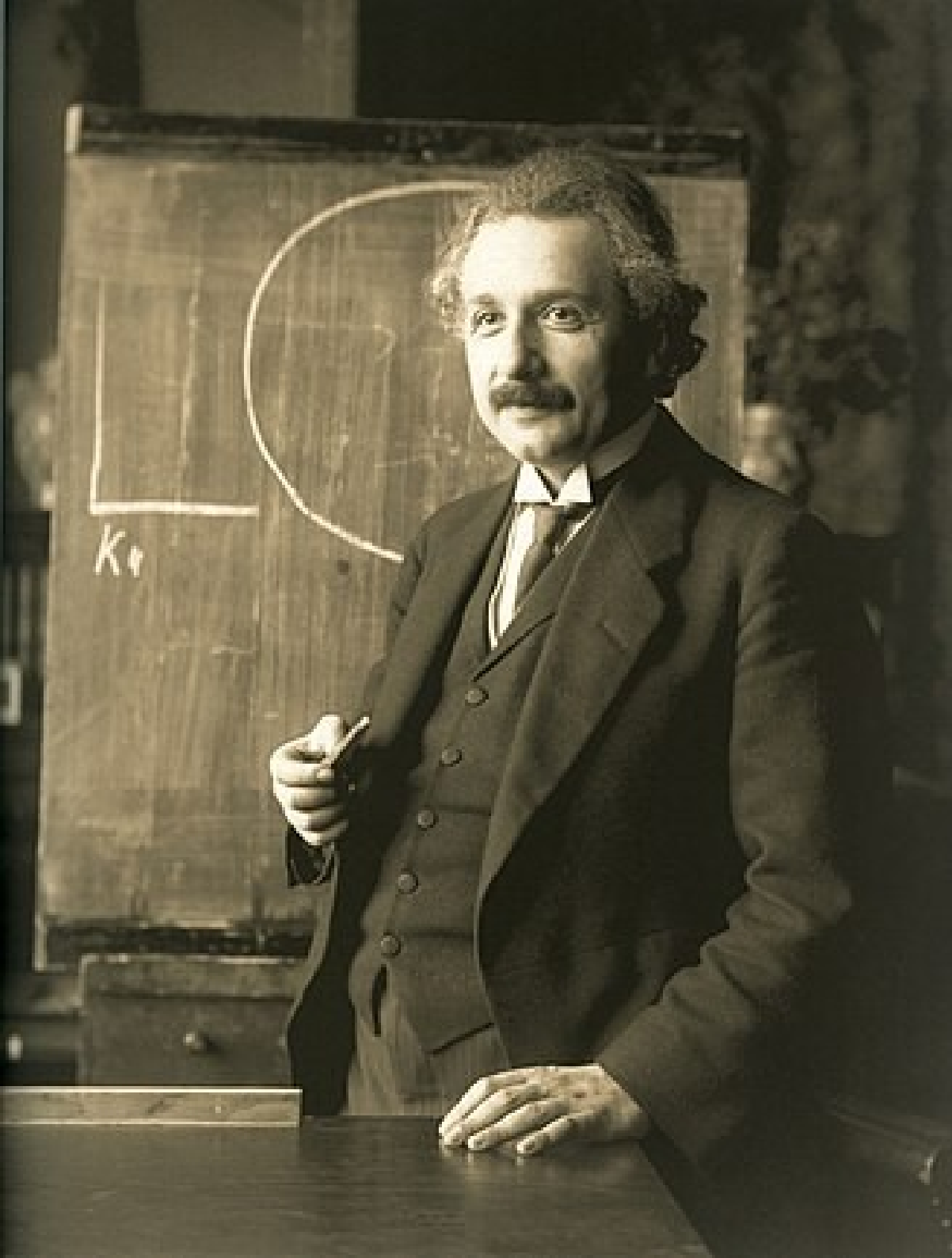
*P. Ajith, T. Broadhurst, J.M. Diego, K. Haris, D. Keitel, K. Kim,  
S. Kumar, K.H. Lai, T.G.F. Li, K.K.Y Ng,  
P.L. Kelly A.K. Mehta, G. Pagano, G.F. Smoot III,  
I. Wong, Peter T. H. Pang, Tim Dietrich, Ian Harry*

Virtual Seminar at Institut d'astrophysique de Paris



**Utrecht University**

# Gravitational Waves



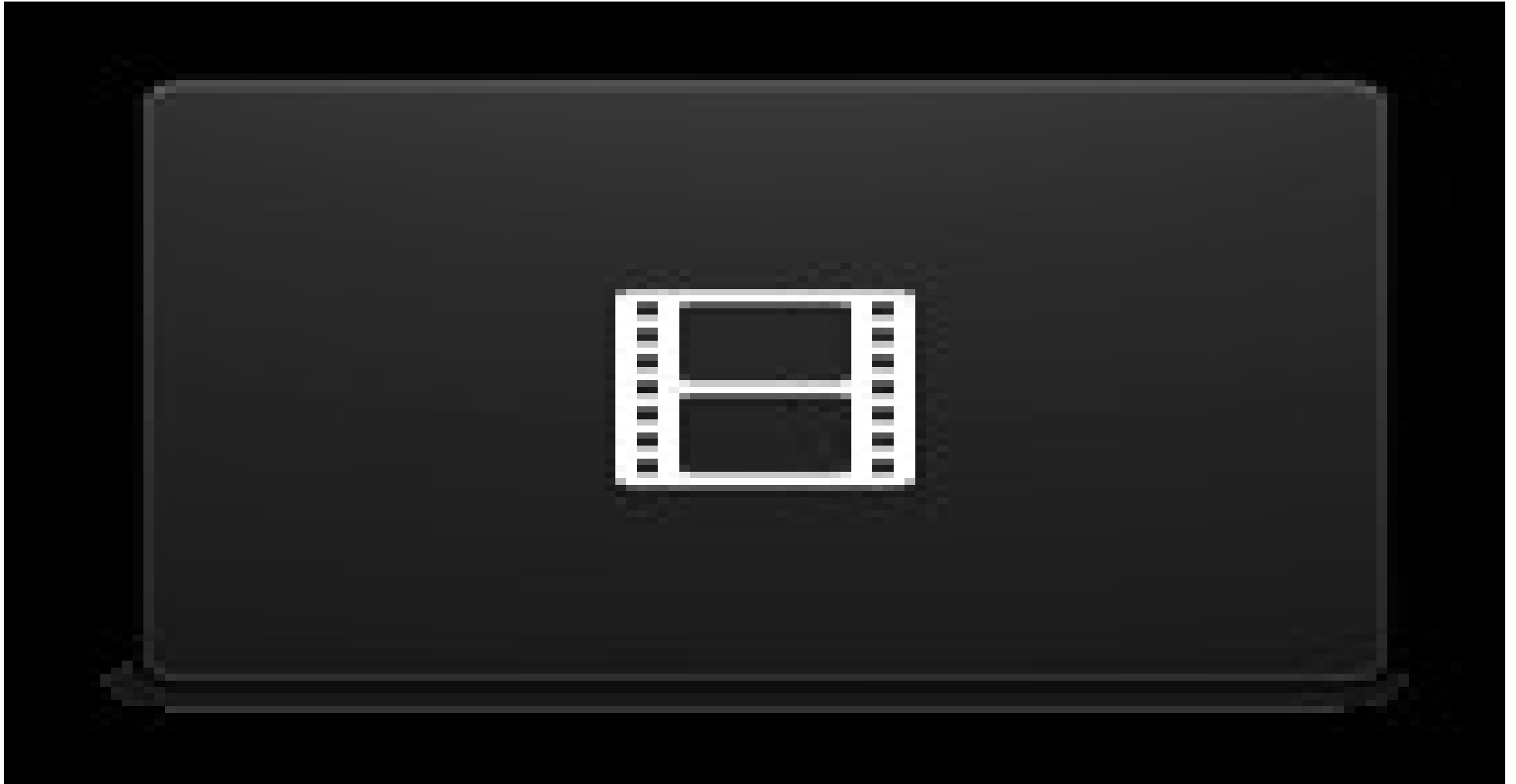
- Predicted by Einstein in 1916

Properties:

- Travels at the speed of light
- Two polarizations
- Passes through matter unimpeded

$$G_{\mu\nu} = 8\pi T_{\mu\nu}$$

# Gravitational-Wave Generation

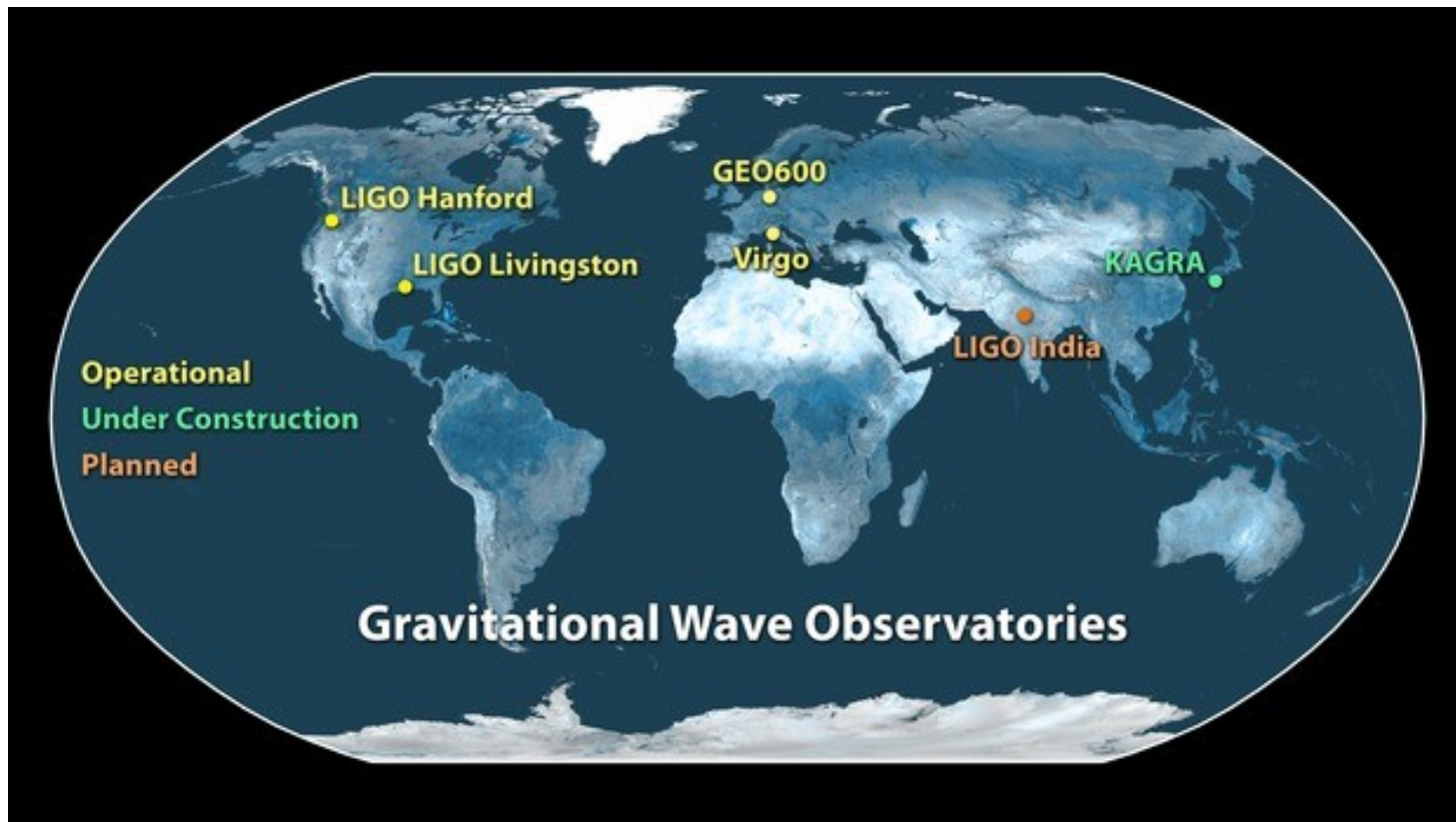


# Gravitational-Wave Detection

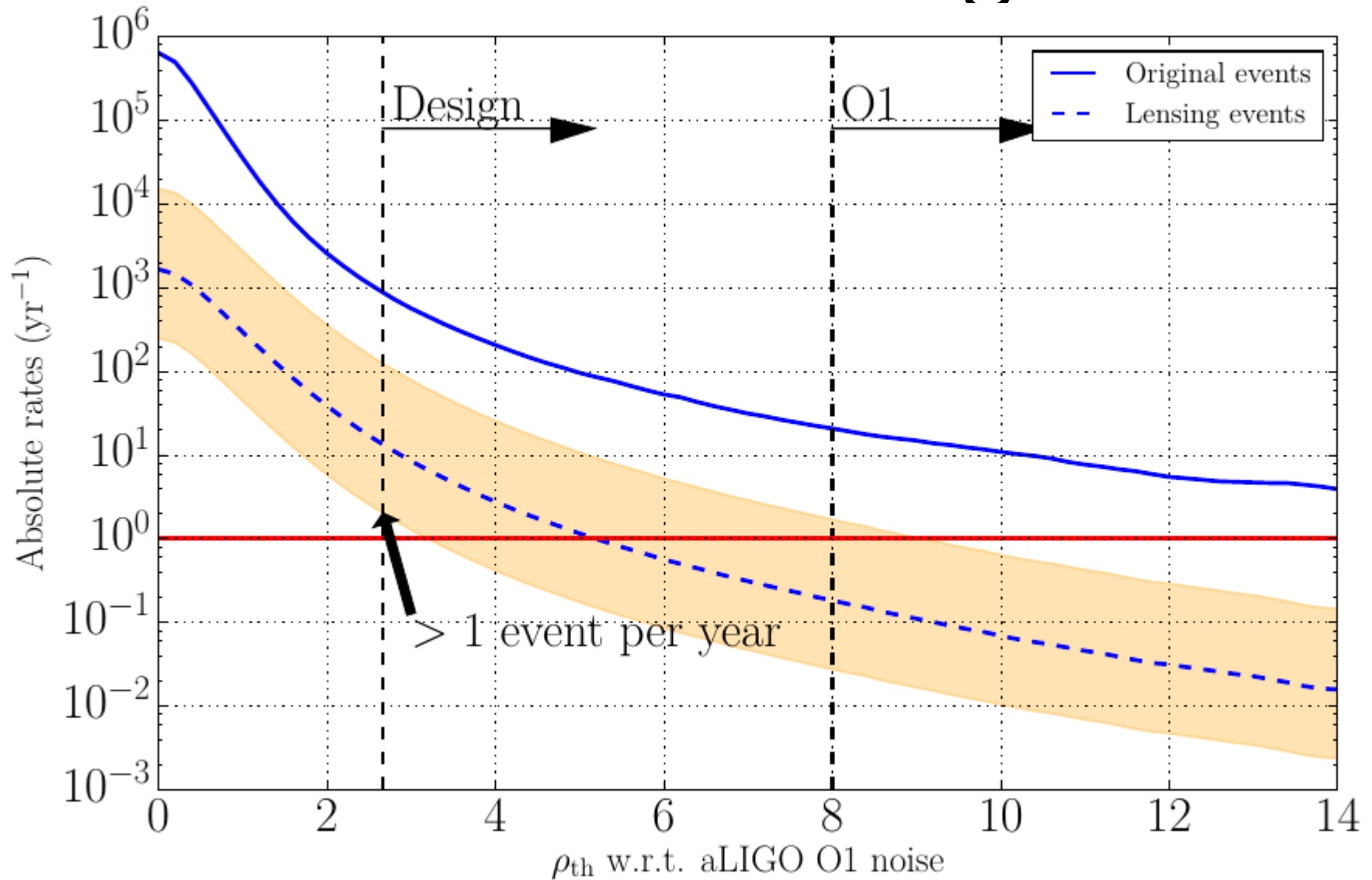


# O1/O2 detections

Event	UTC Time	PyCBC	FAR [ $y^{-1}$ ]			Network SNR		
			GstLAL	cWB	PyCBC	GstLAL	cWB	
GW150914	09:50:45.4	$< 1.53 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	$< 1.63 \times 10^{-4}$	23.6	24.4	25.2	
GW151012	09:54:43.4	0.17	$7.92 \times 10^{-3}$	–	9.5	10.0	–	
GW151226	03:38:53.6	$< 1.69 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	0.02	13.1	13.1	11.9	
GW170104	10:11:58.6	$< 1.37 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	$2.91 \times 10^{-4}$	13.0	13.0	13.0	
GW170608	02:01:16.5	$< 3.09 \times 10^{-4}$	$< 1.00 \times 10^{-7}$	$1.44 \times 10^{-4}$	15.4	14.9	14.1	
GW170729	18:56:29.3	1.36	0.18	0.02	9.8	10.8	10.2	
GW170809	08:28:21.8	$1.45 \times 10^{-4}$	$< 1.00 \times 10^{-7}$	–	12.2	12.4	–	
GW170814	10:30:43.5	$< 1.25 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	$< 2.08 \times 10^{-4}$	16.3	15.9	17.2	
GW170817	12:41:04.4	$< 1.25 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	–	30.9	33.0	–	
GW170818	02:25:09.1	–	$4.20 \times 10^{-5}$	–	–	11.3	–	
GW170823	13:13:58.5	$< 3.29 \times 10^{-5}$	$< 1.00 \times 10^{-7}$	$2.14 \times 10^{-3}$	11.1	11.5	10.8	

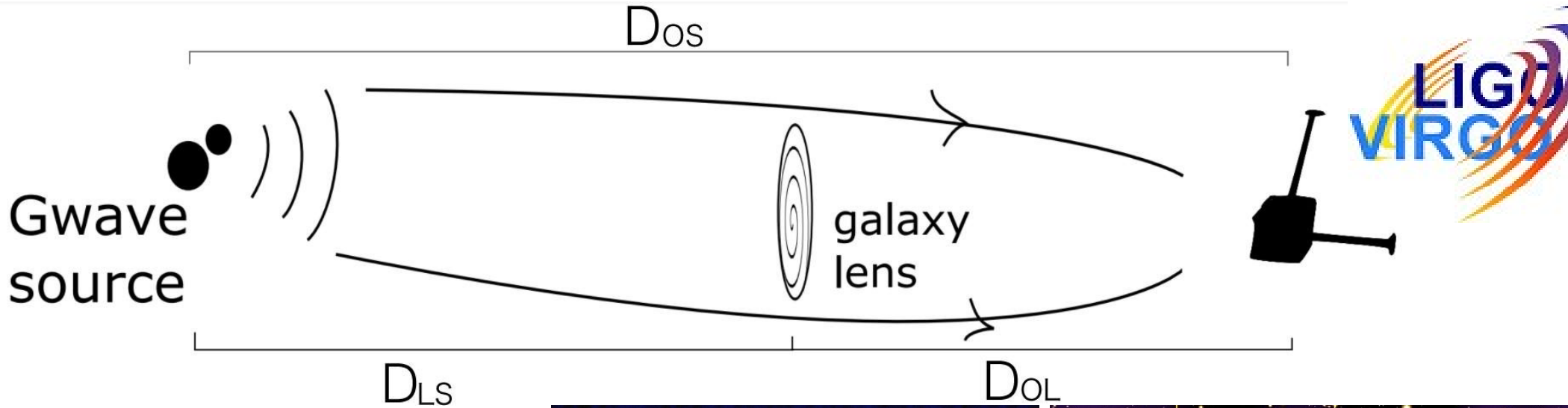


# Rate of Lensing

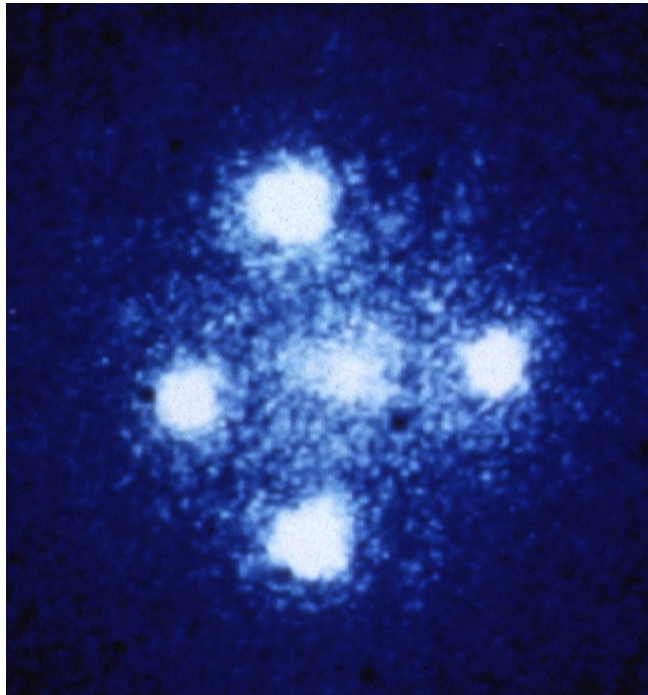


Ng et al., Physical Review D 97.2 (2018): 023012.; see also Li et al., MNRAS 476.2 (2018): 2220-2229; Oguri, MNRAS 480.3 (2018): 3842-3855.

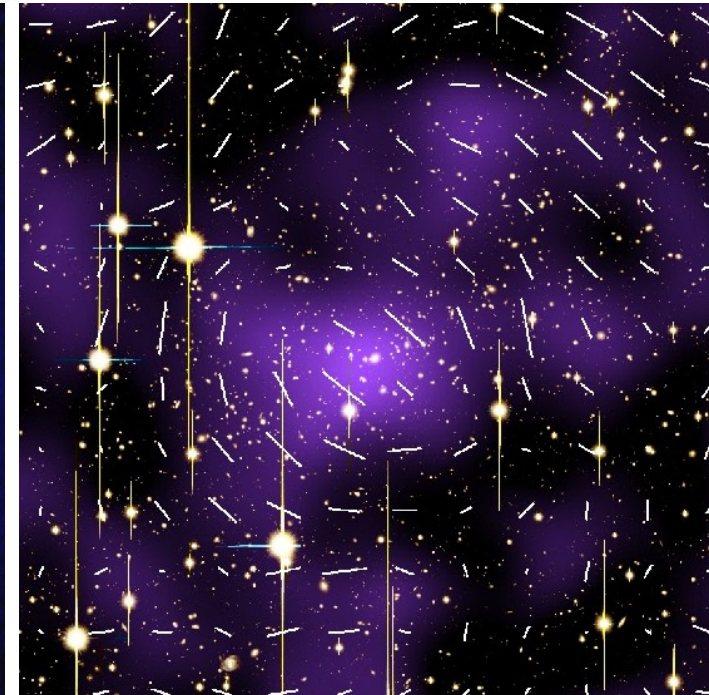
# Gravitational Lensing



ESA/Hubble & NASA

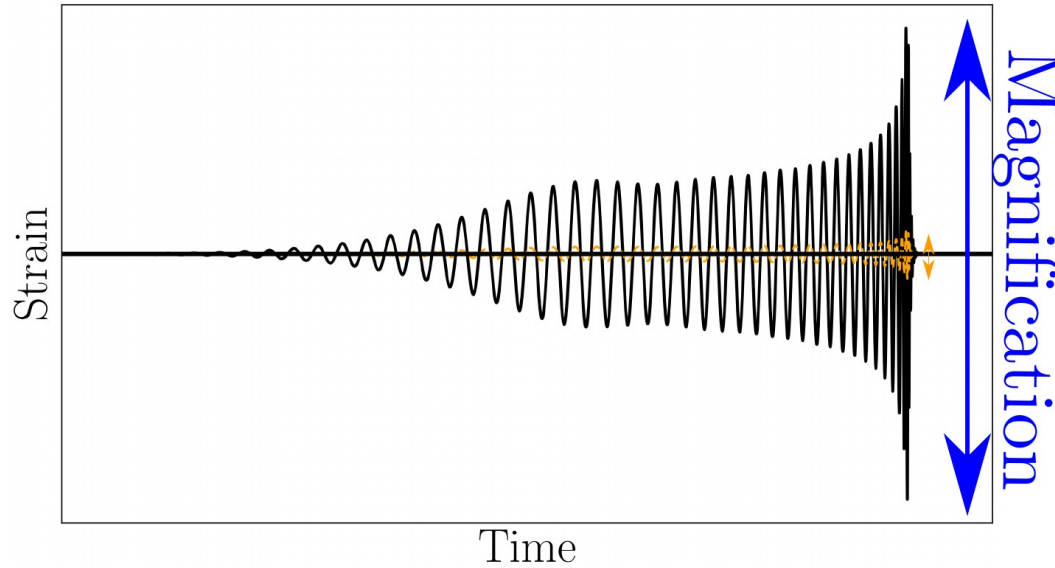


NASA, ESA & STScI



Oguri et al.

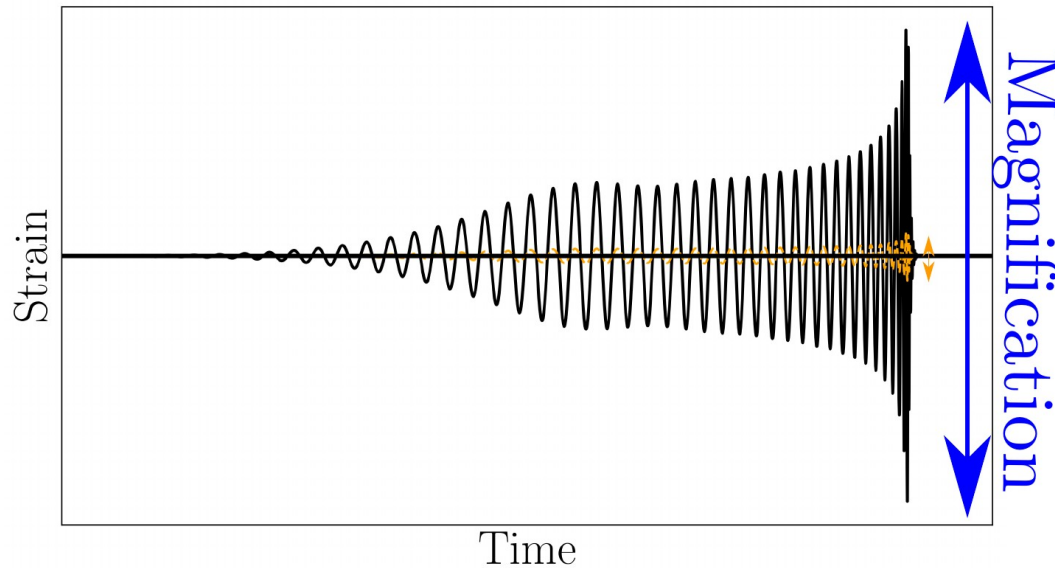
# Strong Lensing Magnification



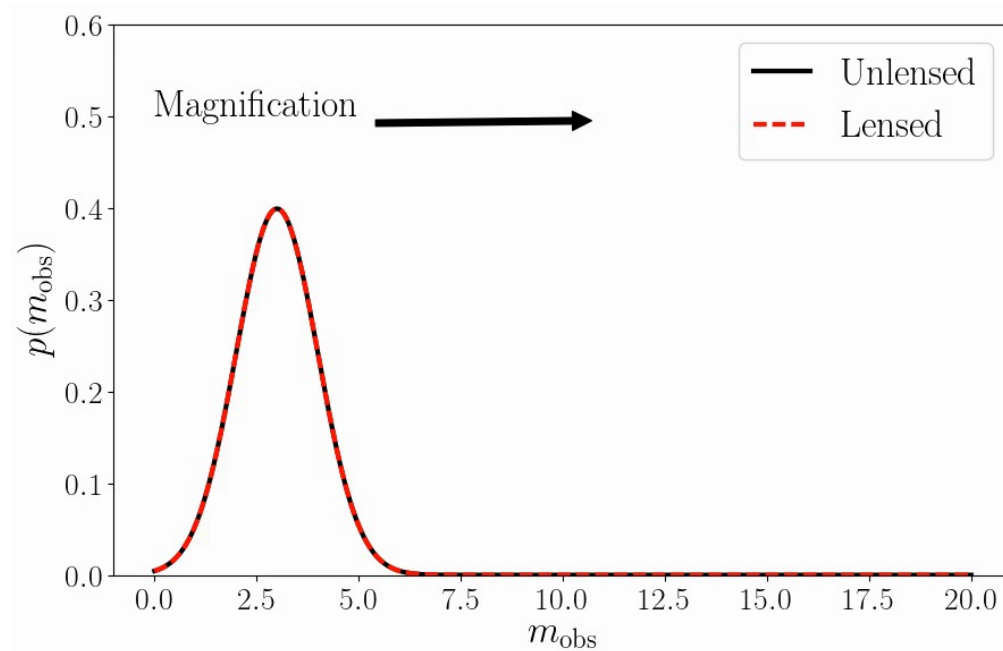
$$(1 + z)m_i = (1 + z_L)m_i^L,$$
$$D_L = D/\sqrt{\mu}$$



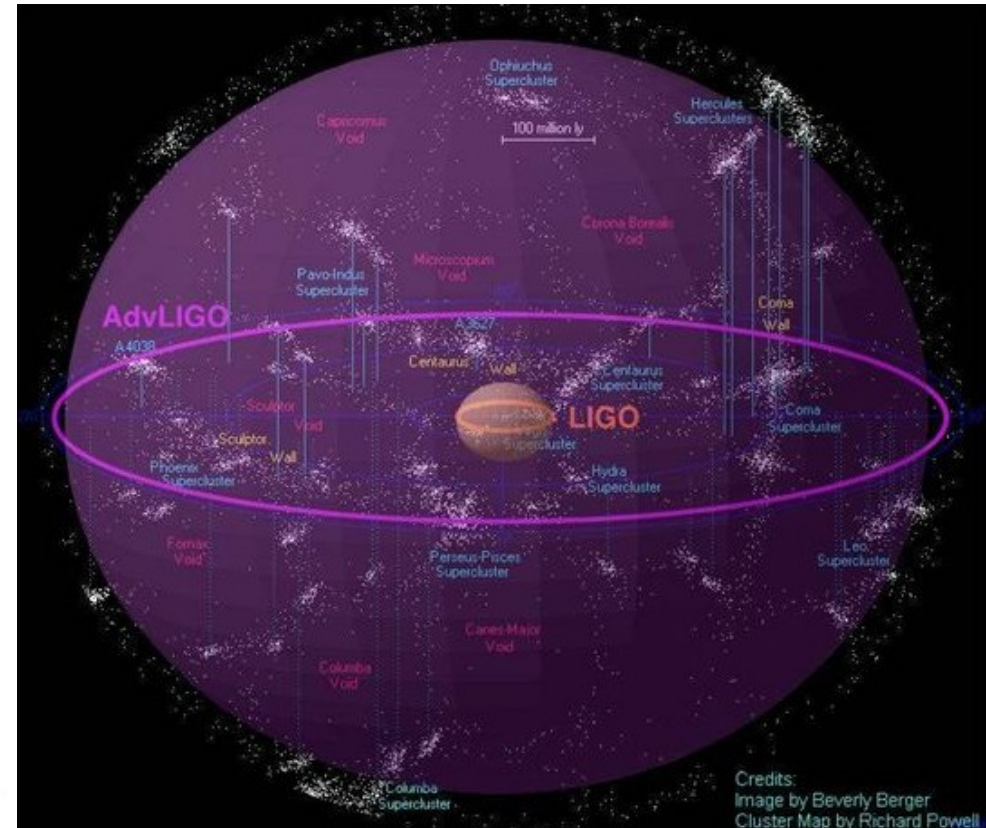
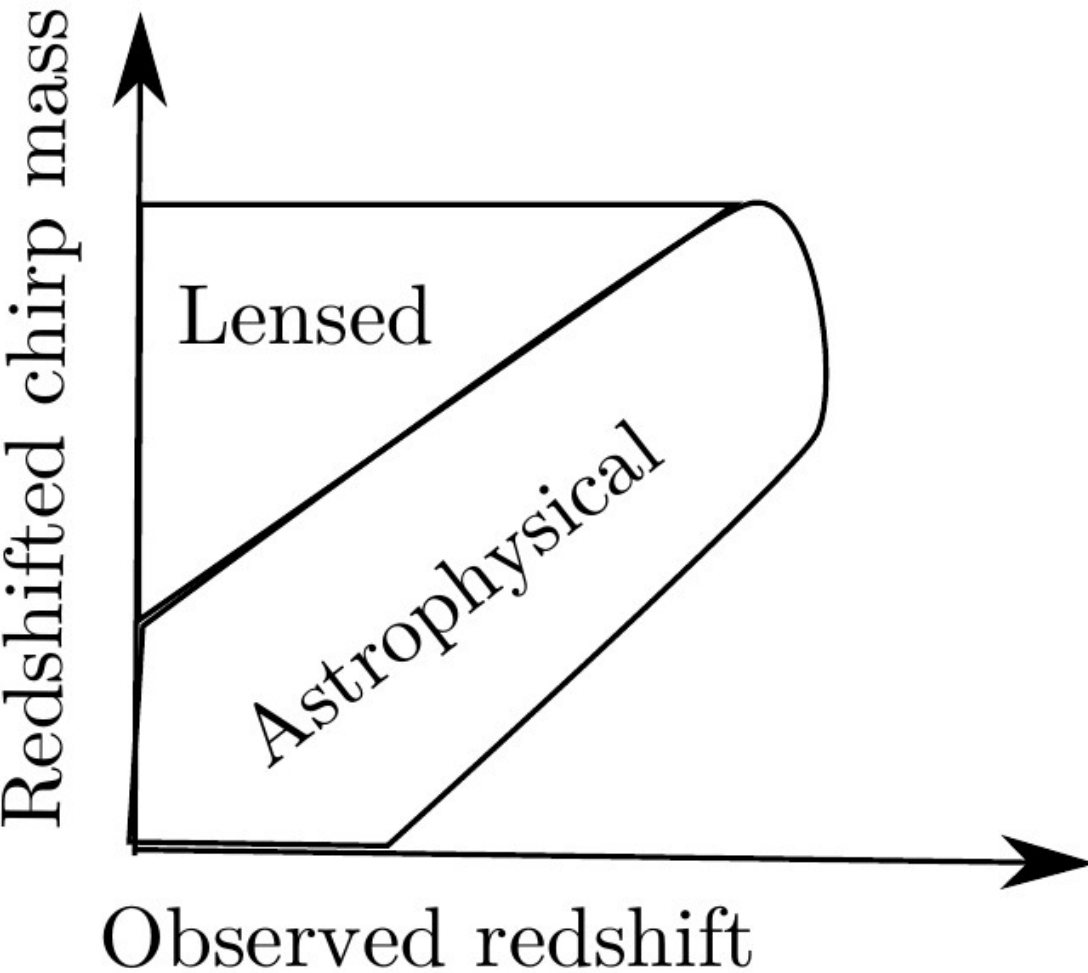
# Strong Lensing Magnification



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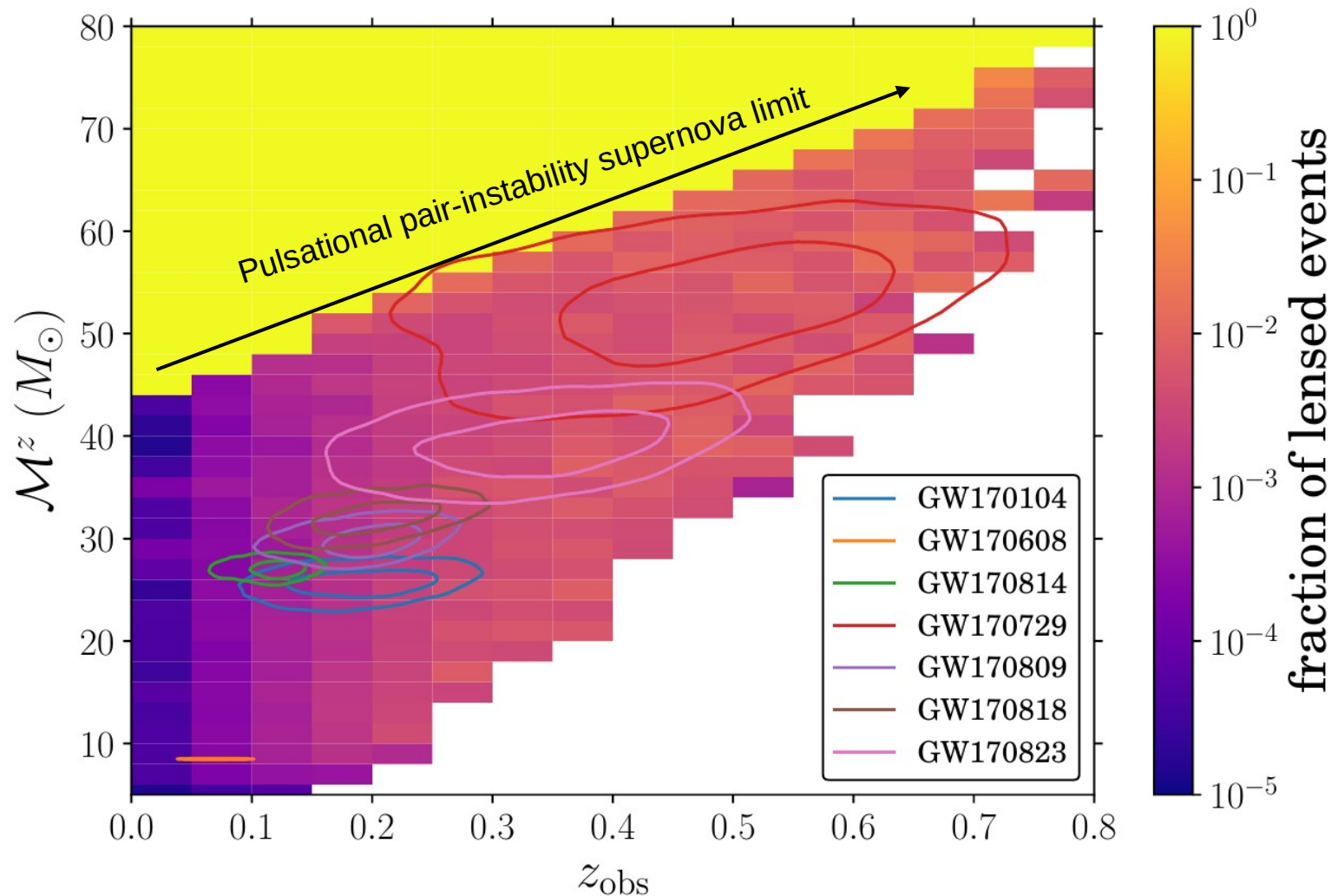


# Strong Lensing Magnification

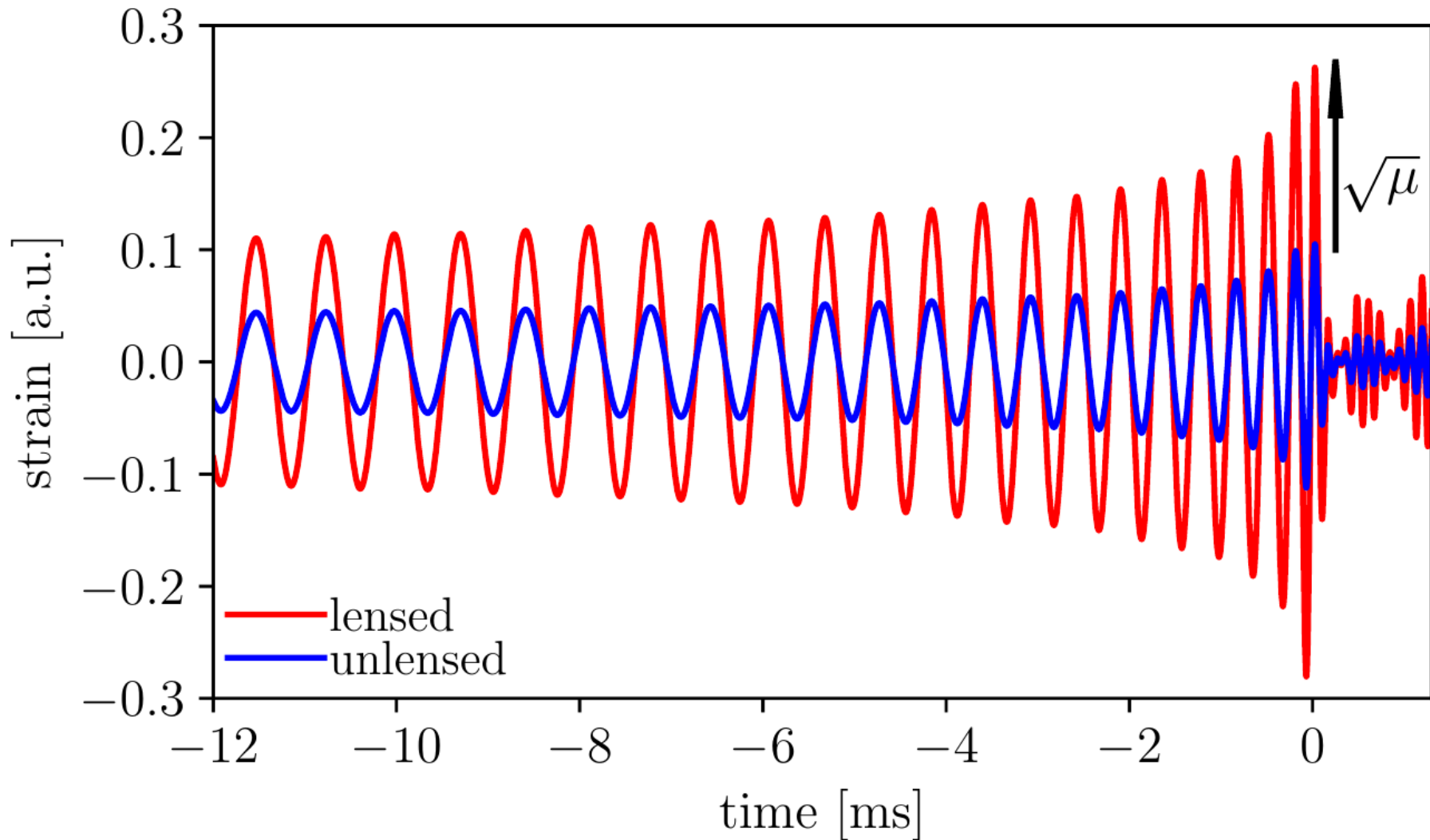


Credits: LIGO/Virgo

# GWTC-1: Strong Lensing Magnification

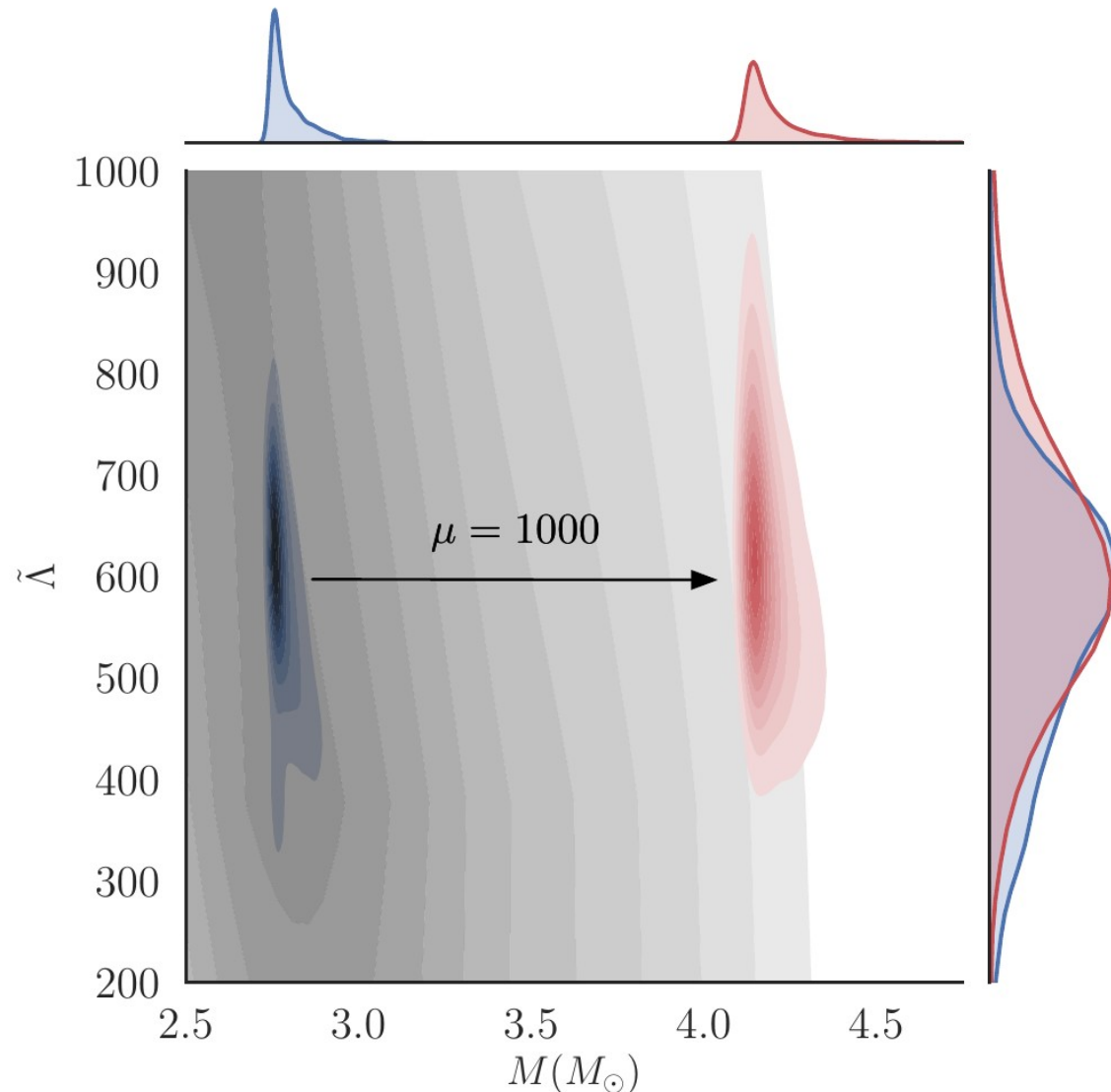


# Heavy neutron stars (e.g. GW190425)



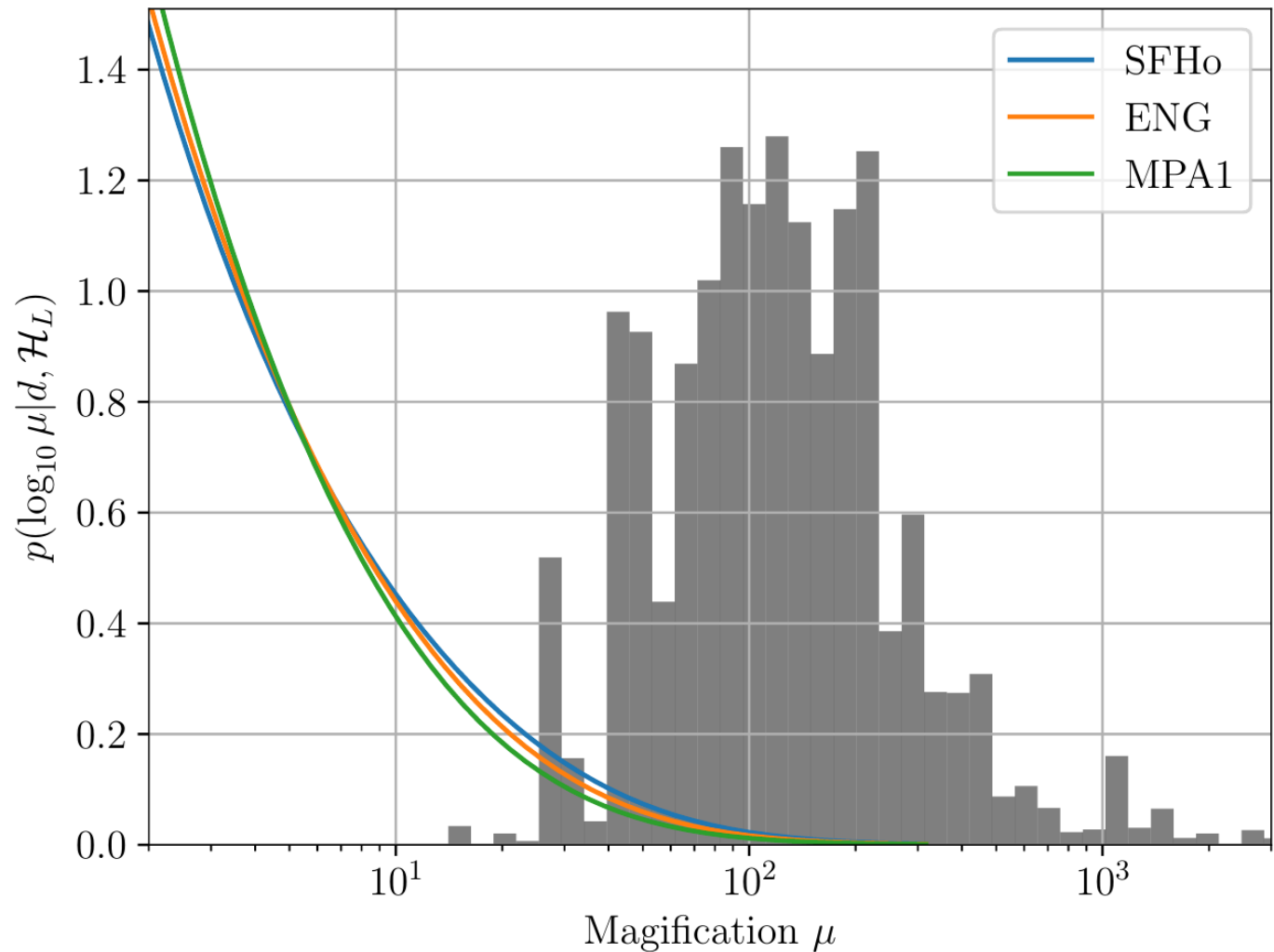
# Heavy neutron stars (e.g. GW190425)

- Binary neutron stars (BNSs) offer tidal measurements that would not be biased by lensing magnification
- Thus, a lensed BNS would appear as a massive BNS with a tidal deformability of a lower-mass BNS.
- Given an equation of state, we might rule out/confirm lensing for BNSs.



# Heavy neutron stars (e.g. GW190425)

- Methodology could be used to confirm/rule out lensing.
- No evidence of GW lensing magnification for GW190425
- Future detections with better tidal measurements will likely yield better constraints



# Why study magnification?

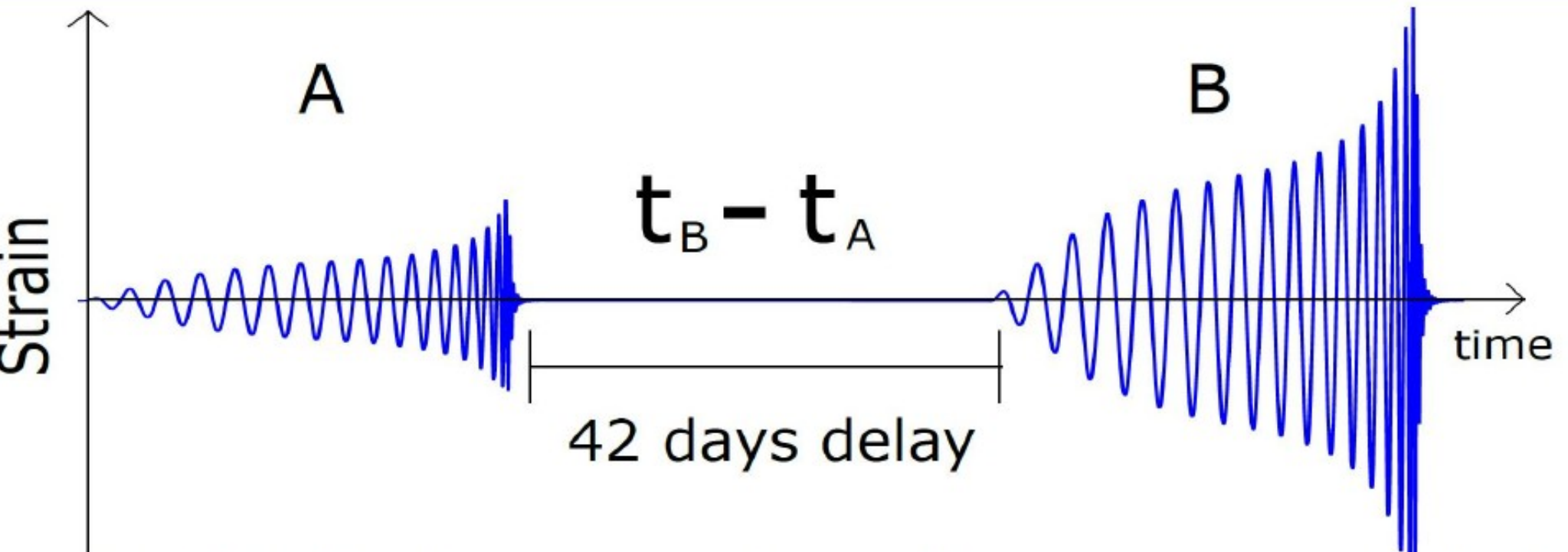
Example work:

- High-redshift BBH probes (Dai et al. 2017)
- Primordial black hole probes (Dai et al. 2017)
- Wave effects (Diego et al. 2019)
- Combined with tidal measurements, could allow for evidence of lensing for binaries with EM counterparts (Pang et al. 2020)

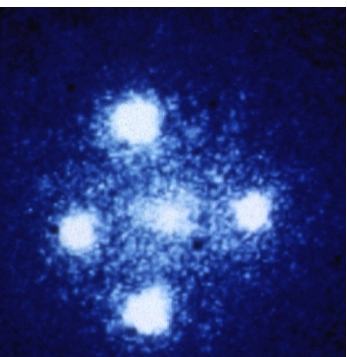


Credits:  
Image by Beverly Berger  
Cluster Map by Richard Powell

# Strong Lensing Multi-Images

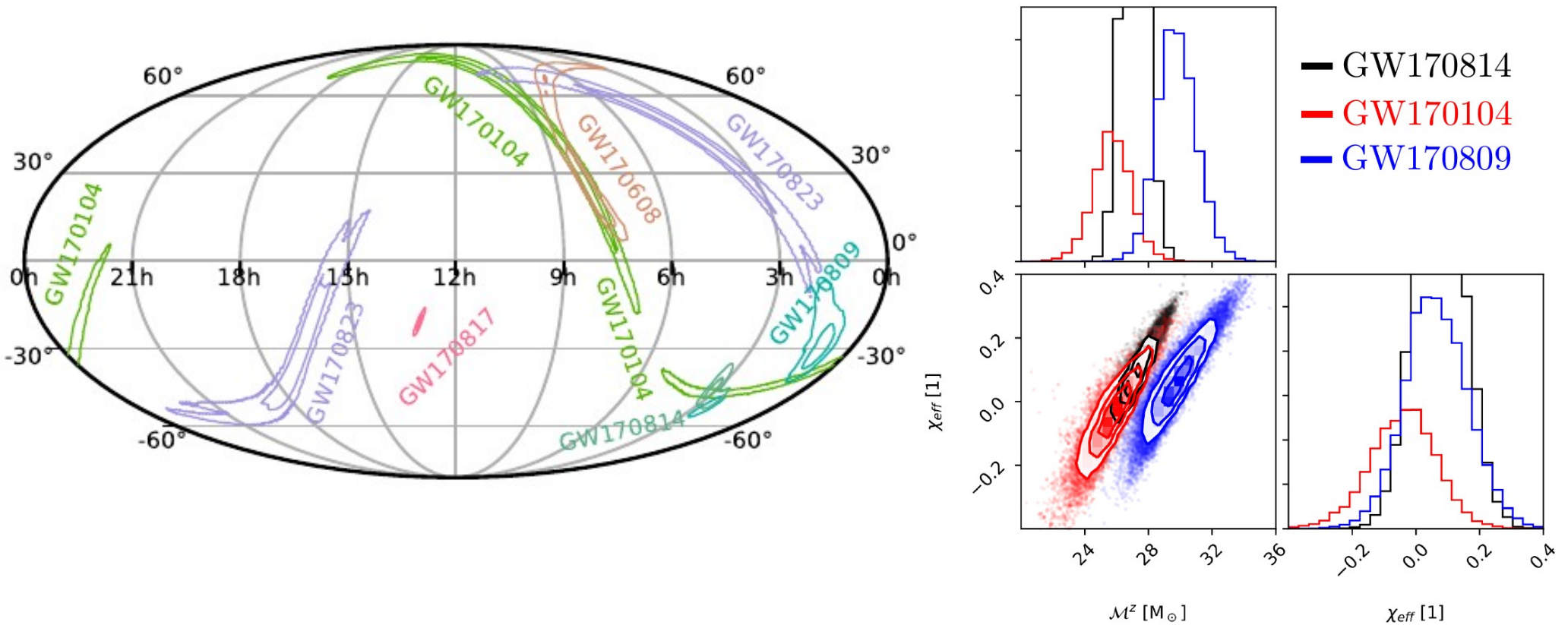


Multiple image signals are possible!

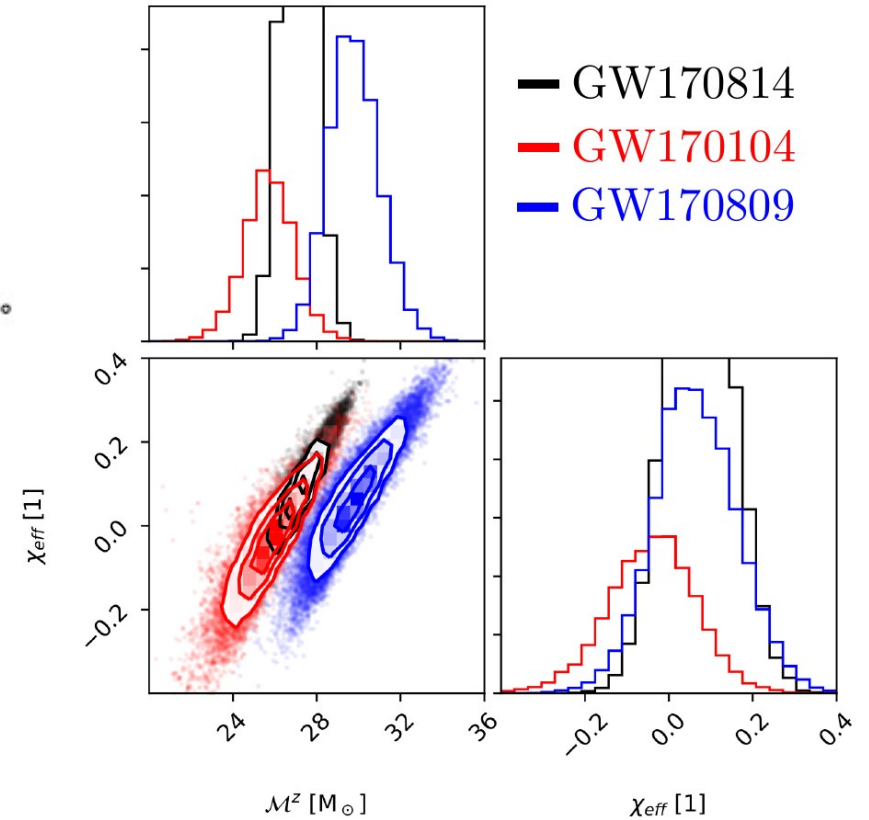
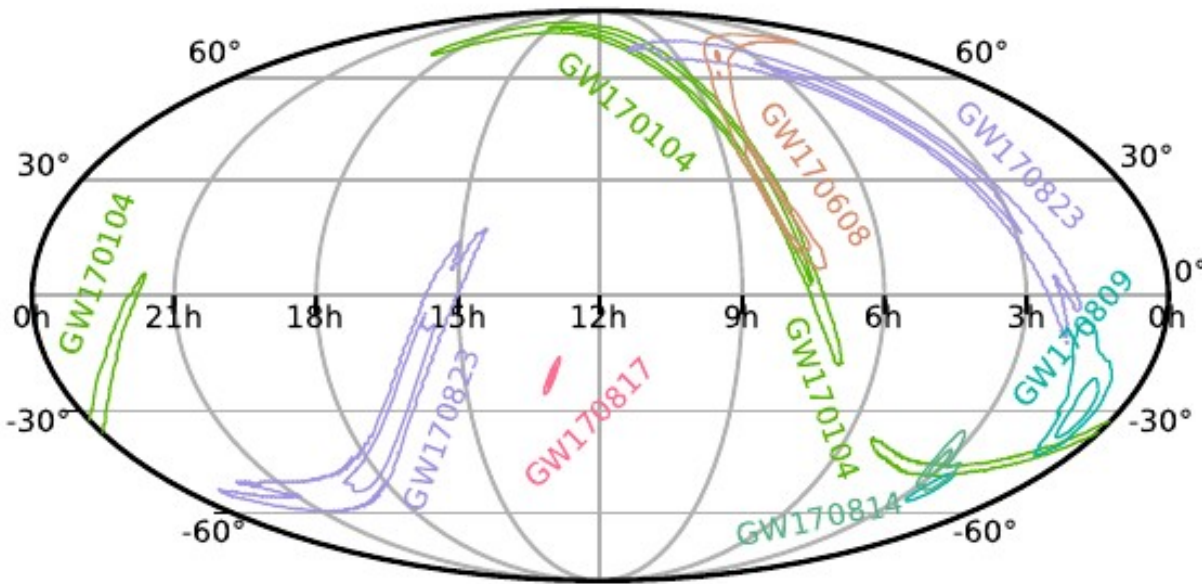




# Strong Lensing Multi-Images



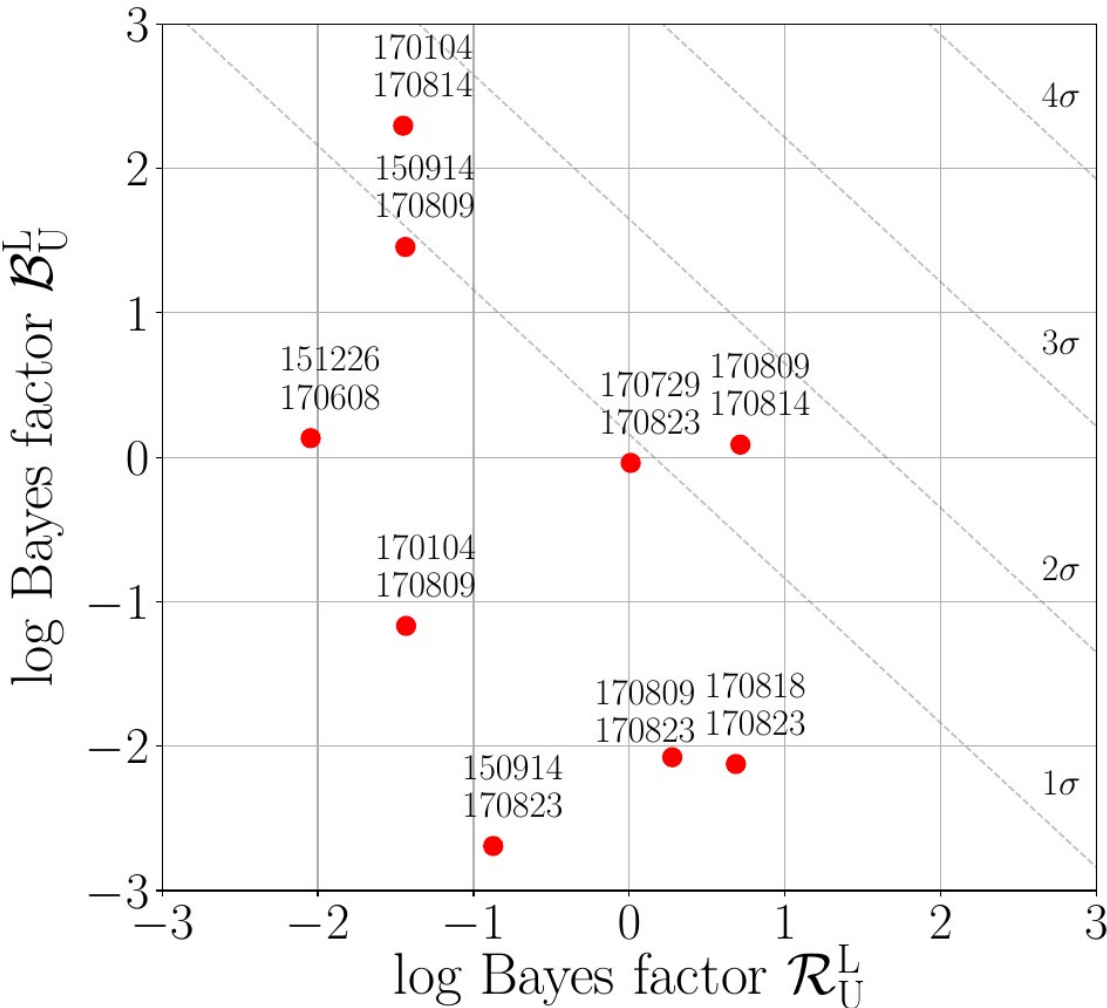
# Strong Lensing Multi-Images



$$\mathcal{B}_U^L := \frac{\mathcal{Z}_L}{\mathcal{Z}_U} = \int d\theta \frac{P(\theta|d_1) P(\theta|d_2)}{P(\theta)}$$

$$\mathcal{R}_U^L = \frac{P(\Delta t_0|\mathcal{H}_L)}{P(\Delta t_0|\mathcal{H}_U)}$$

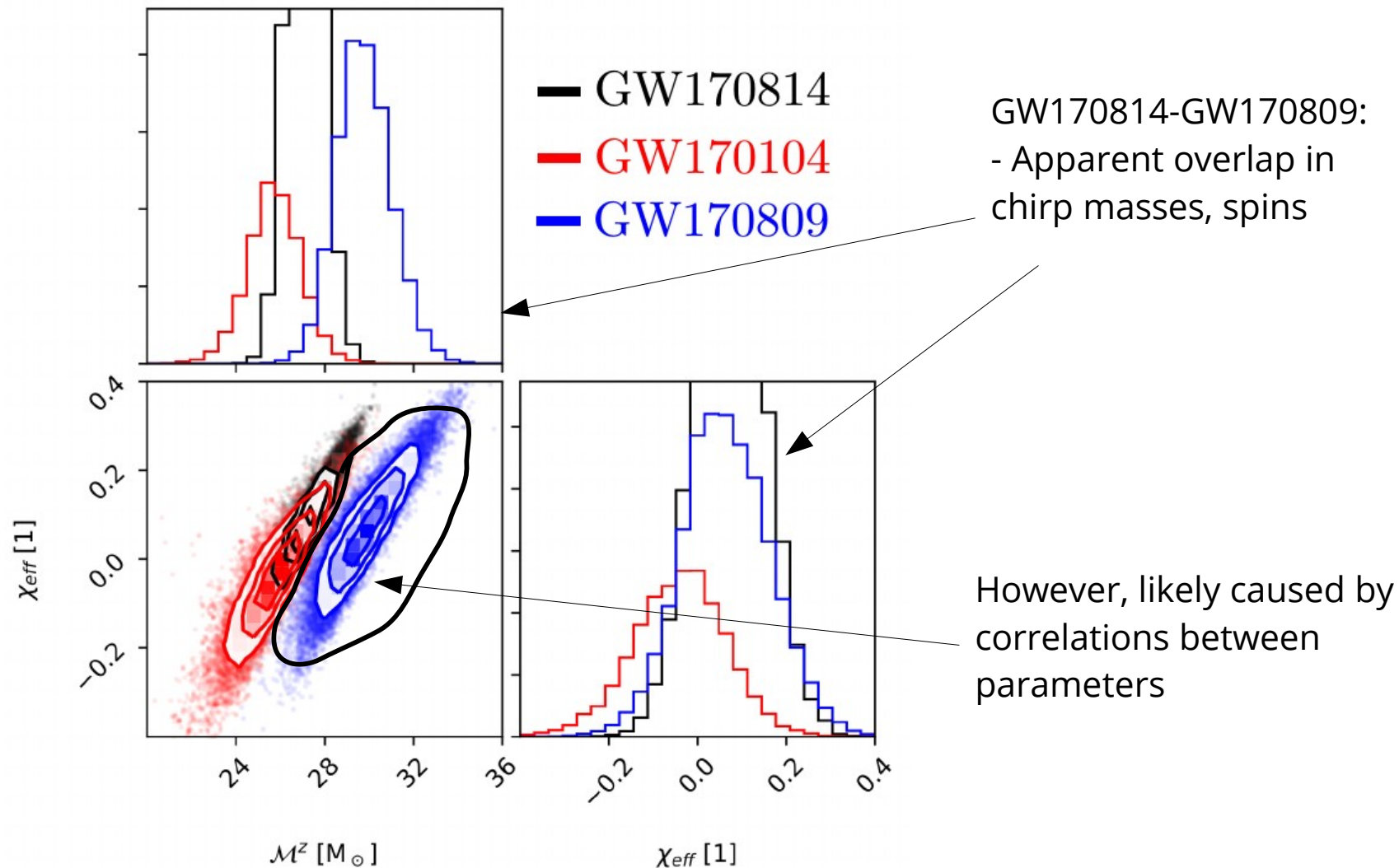
# GWTC-1: Strong Lensing Multi-Images



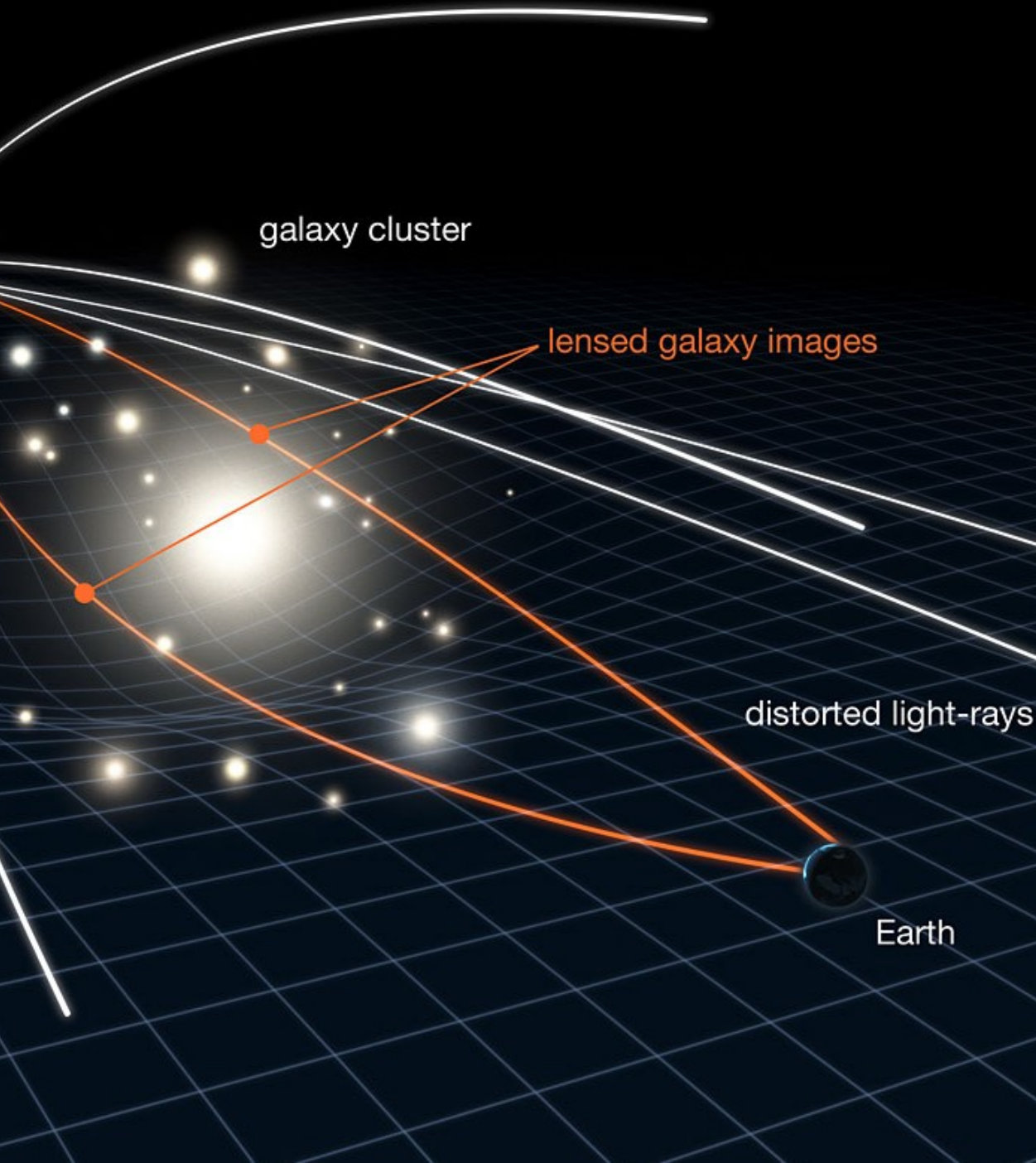
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$$\mathcal{R}_U^L = \frac{P(\Delta t_0|\mathcal{H}_L)}{P(\Delta t_0|\mathcal{H}_U)}$$

# GWTC-1: Strong Lensing Multi-Images



# Why study multi-images



Example work:

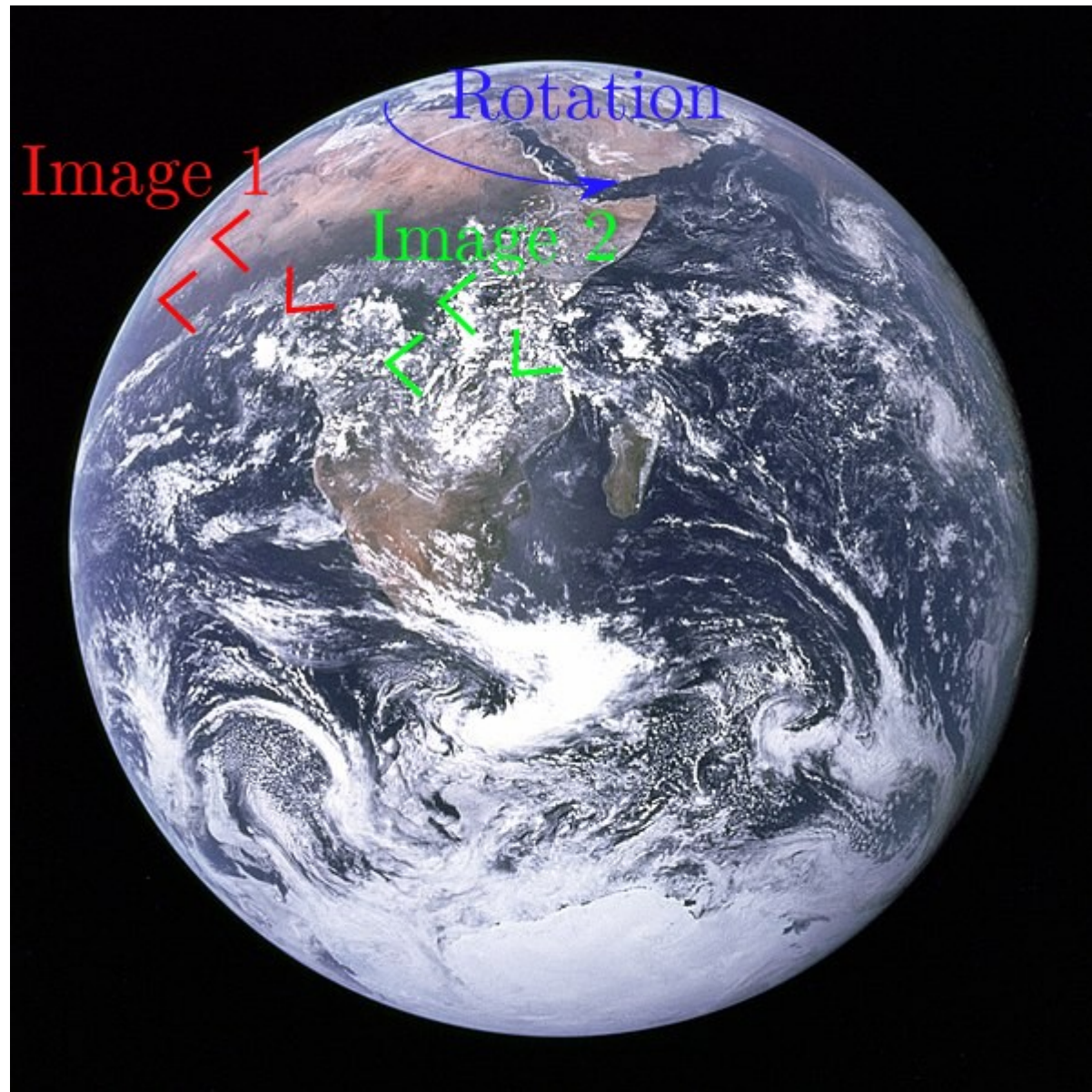
- Tests of speed of gravity (Collett & Bacon 2017, Fan et al. 2017)

- Strong lensing cosmography (Baker & Trodden 2017, Liao et al. 2017)

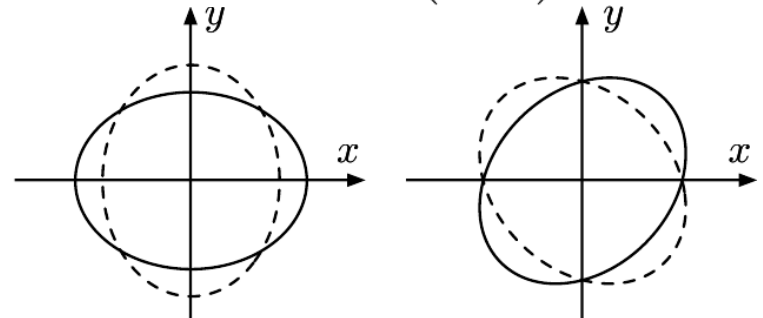
- Hubble constant measurements (Liao et al. 2017)

- Polarization tests (Wong et al., in prep)

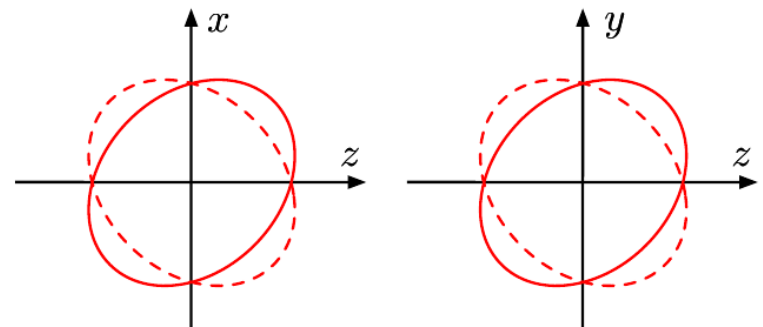
# Polarization tests (preliminary)



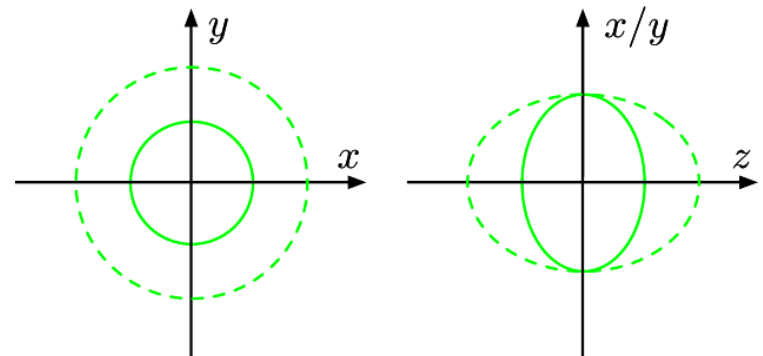
Tensor modes (GR)



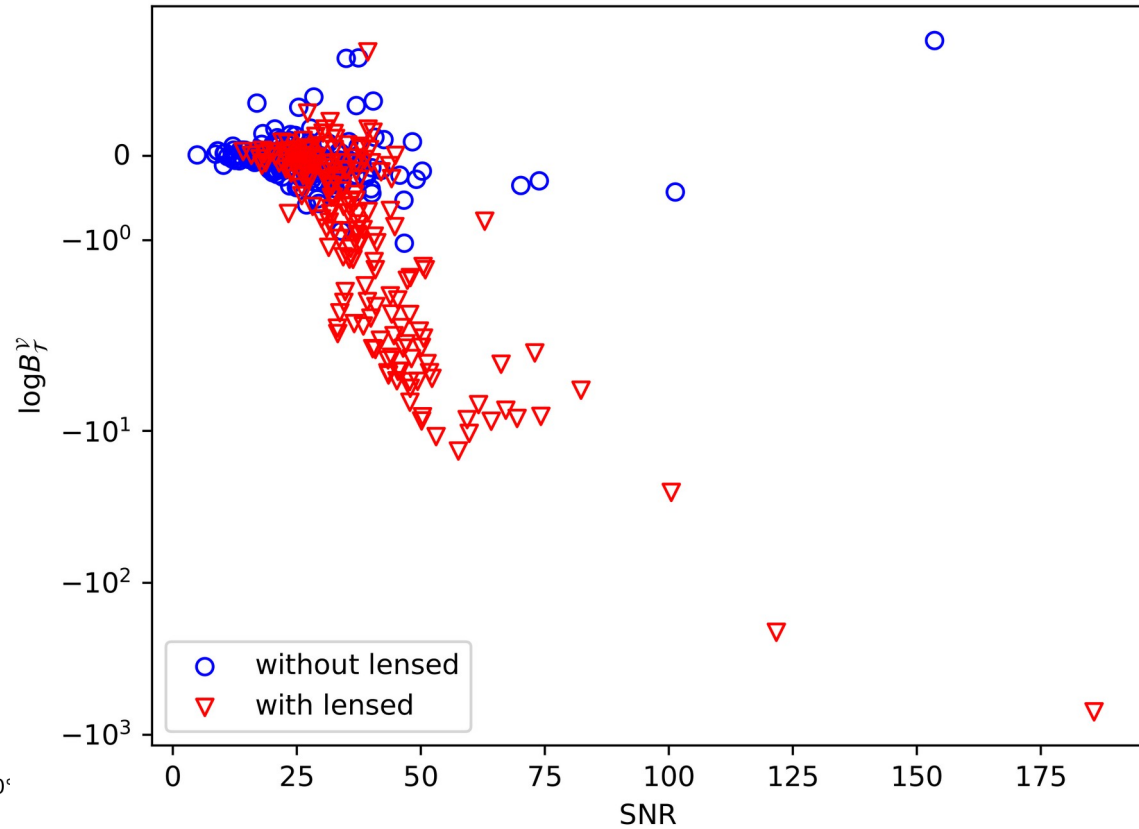
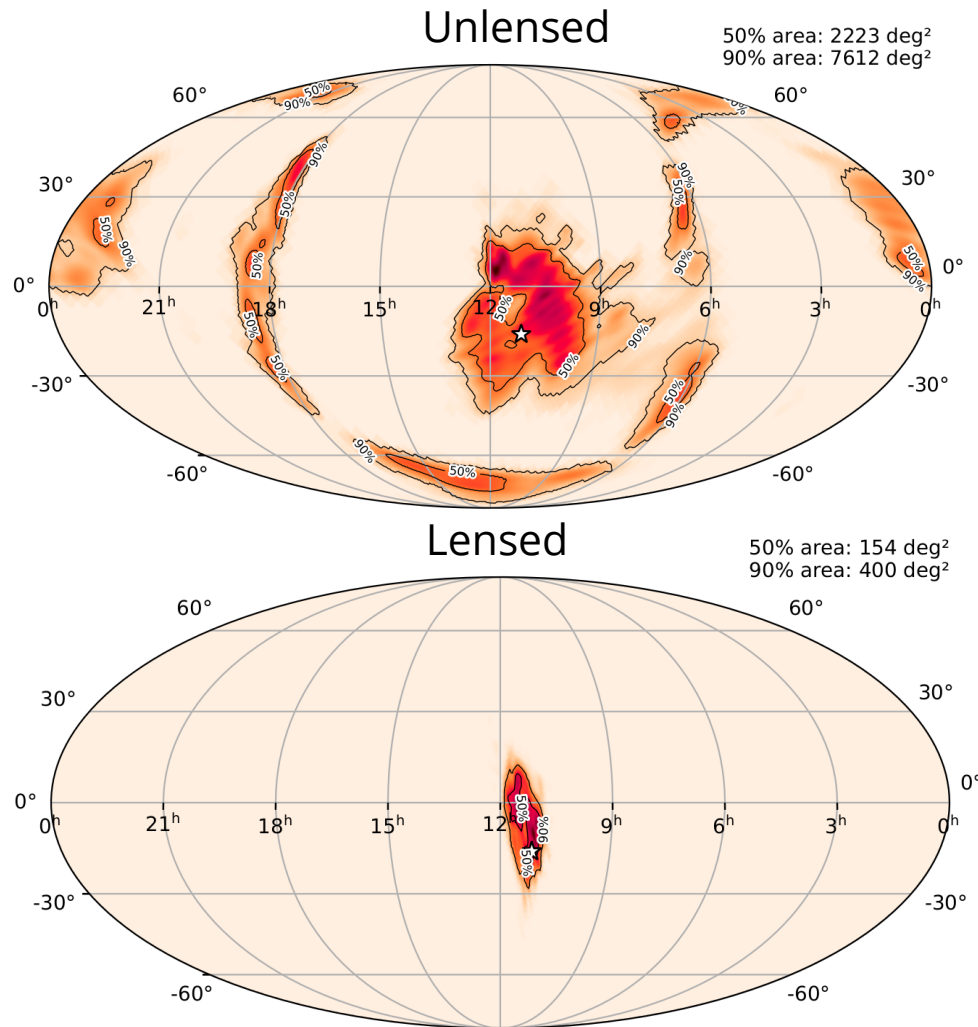
Vector modes (nonGR)



Scalar modes (nonGR)

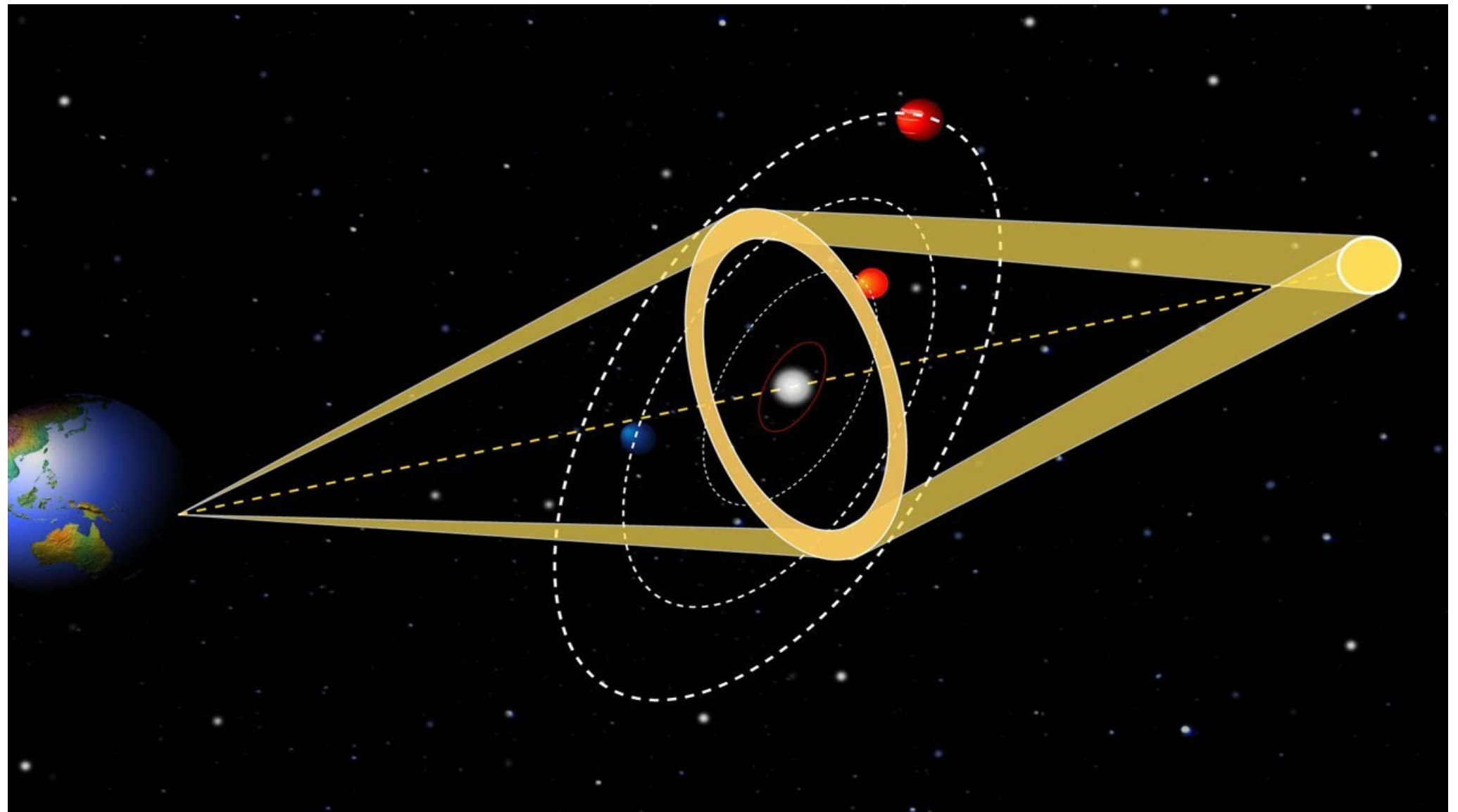


# Polarization tests (preliminary)



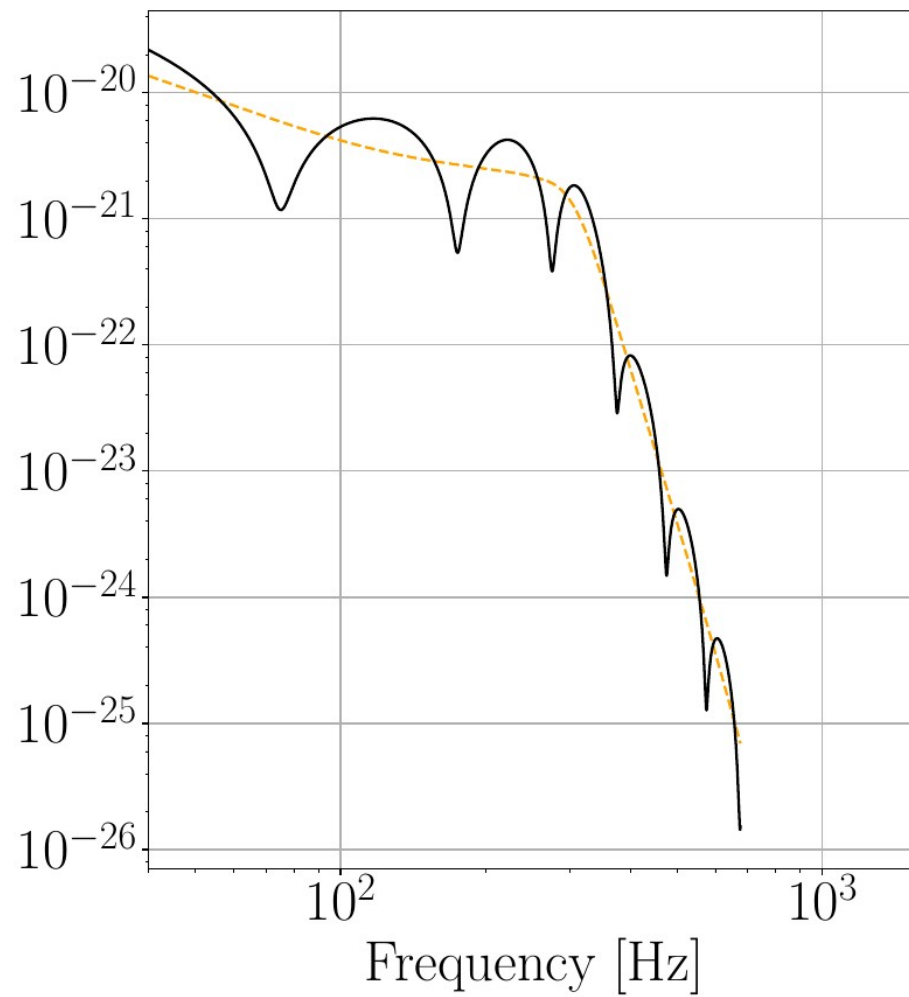
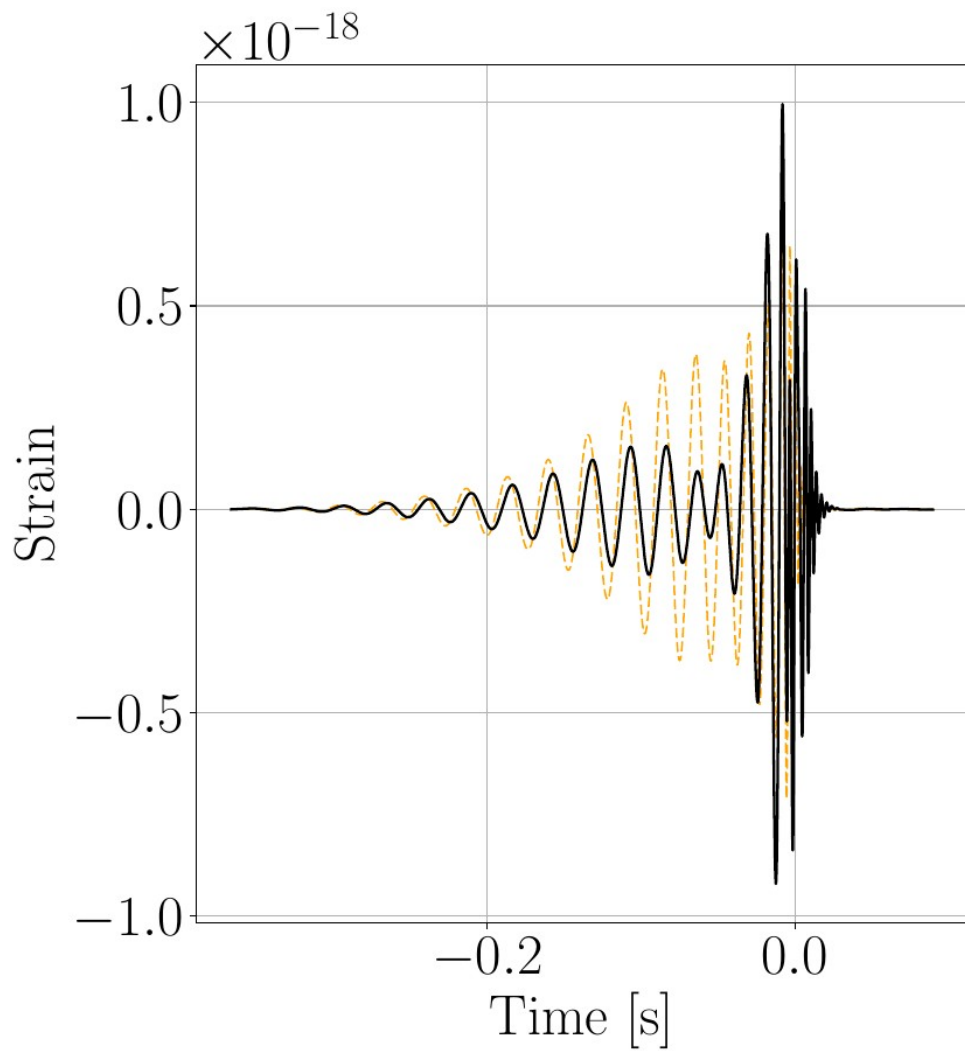
- Because multiple images arrive at a time-delay and thus different detector orientation, it allows for tests with effectively larger number of detectors

# Microlensing



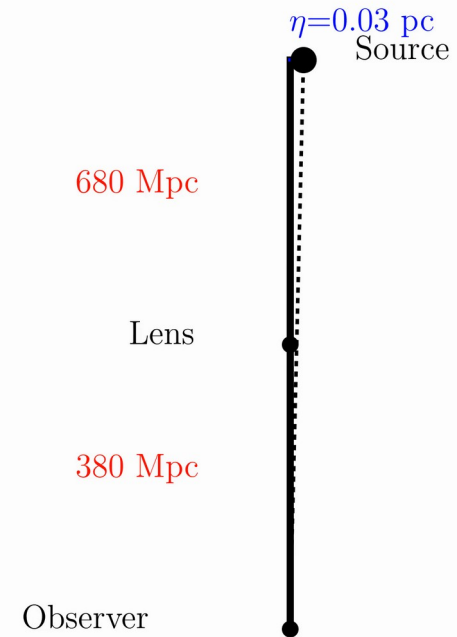
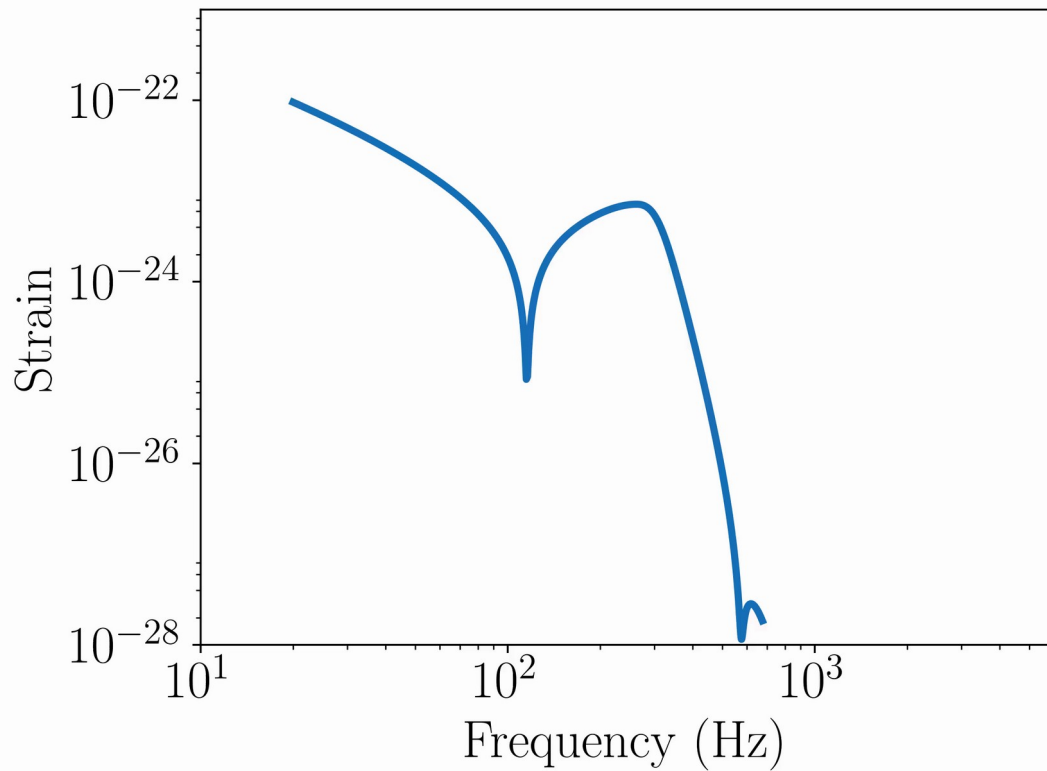


# Microlensing



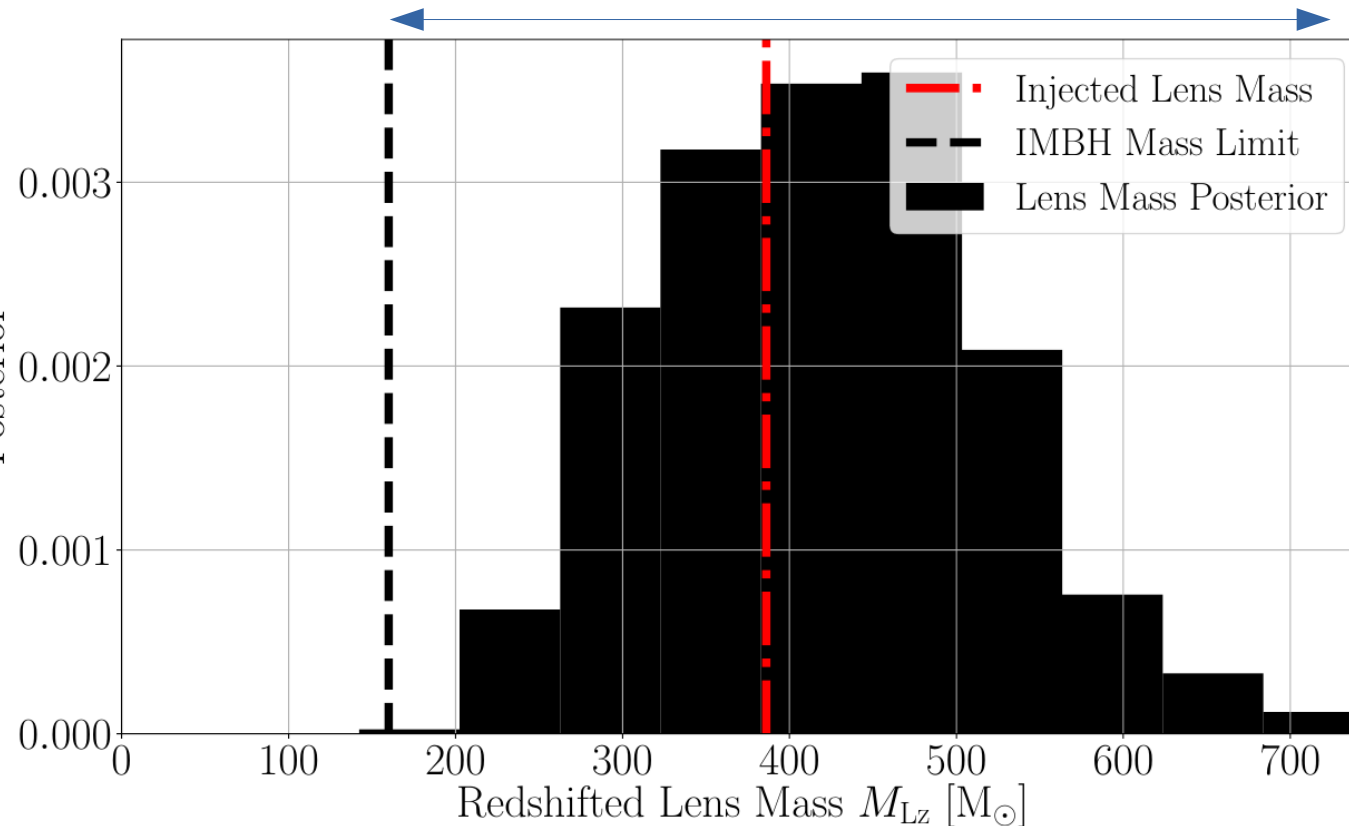
# Microlensing

Point mass lens



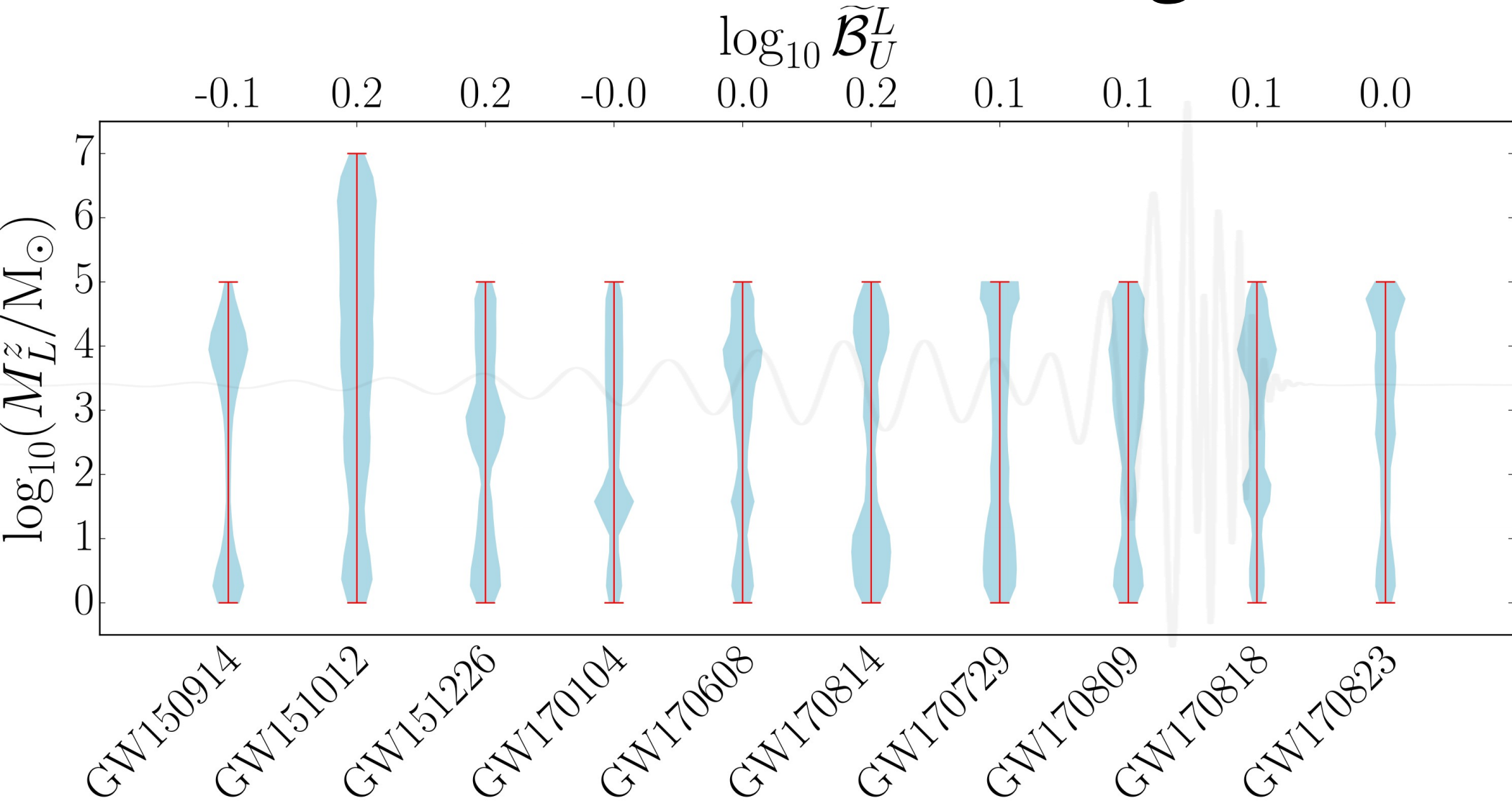
# Microlensing: intermediate-mass black holes

Above 100 solar masses

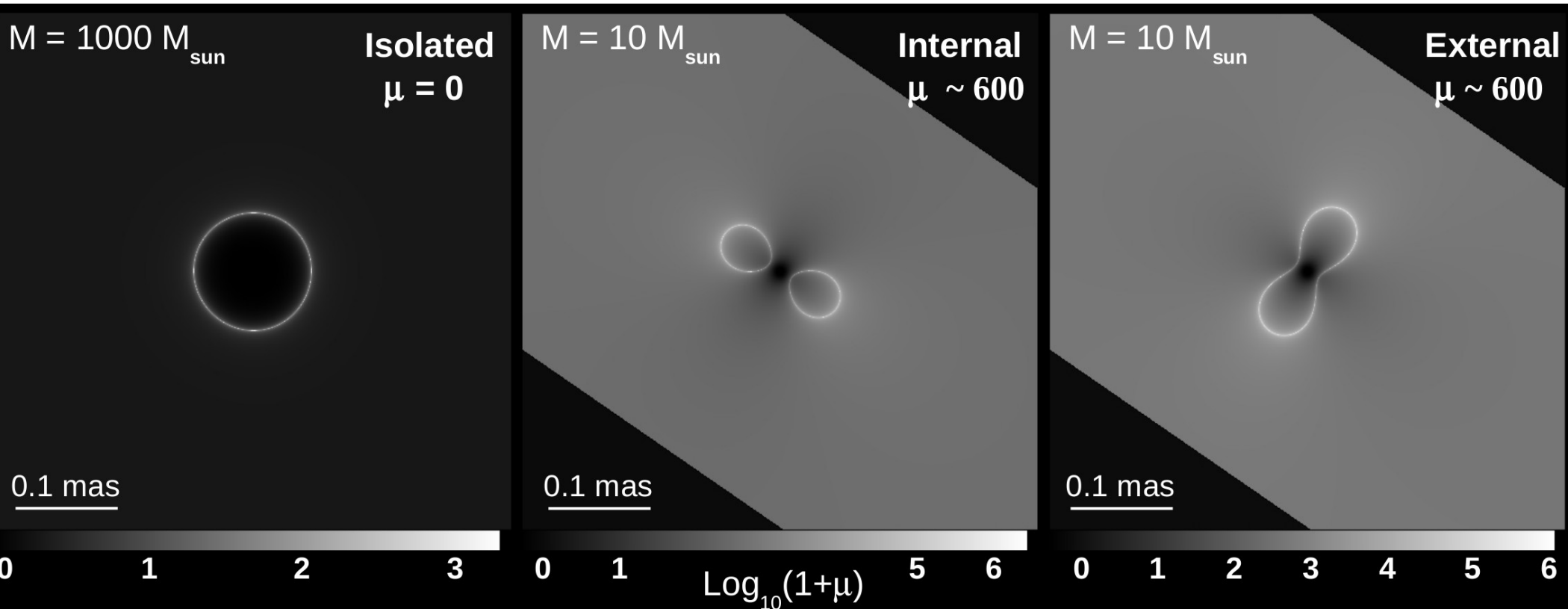


Implementation  
within LSC-developed  
LALSuite

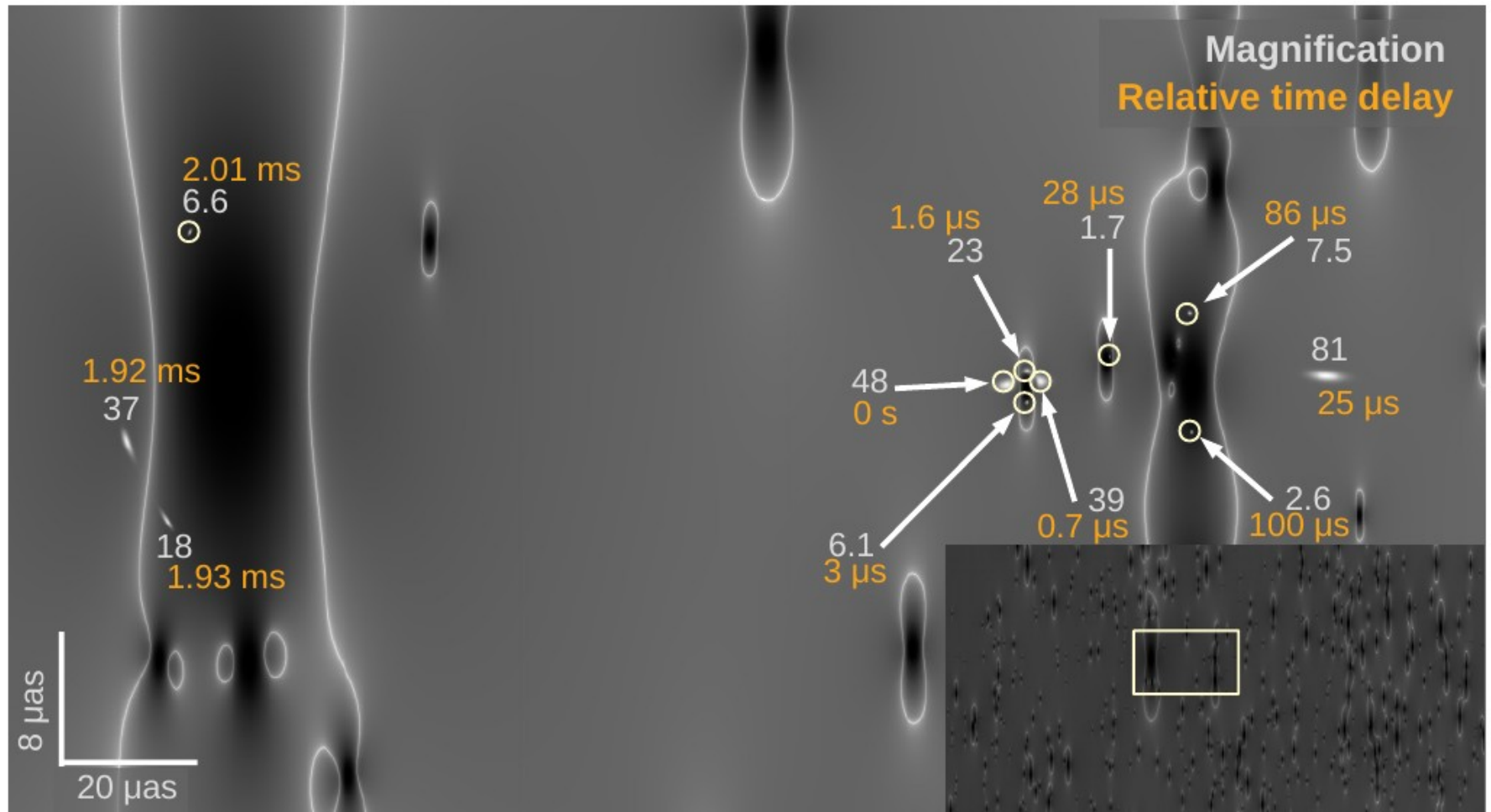
# GWTC-1: Microlensing



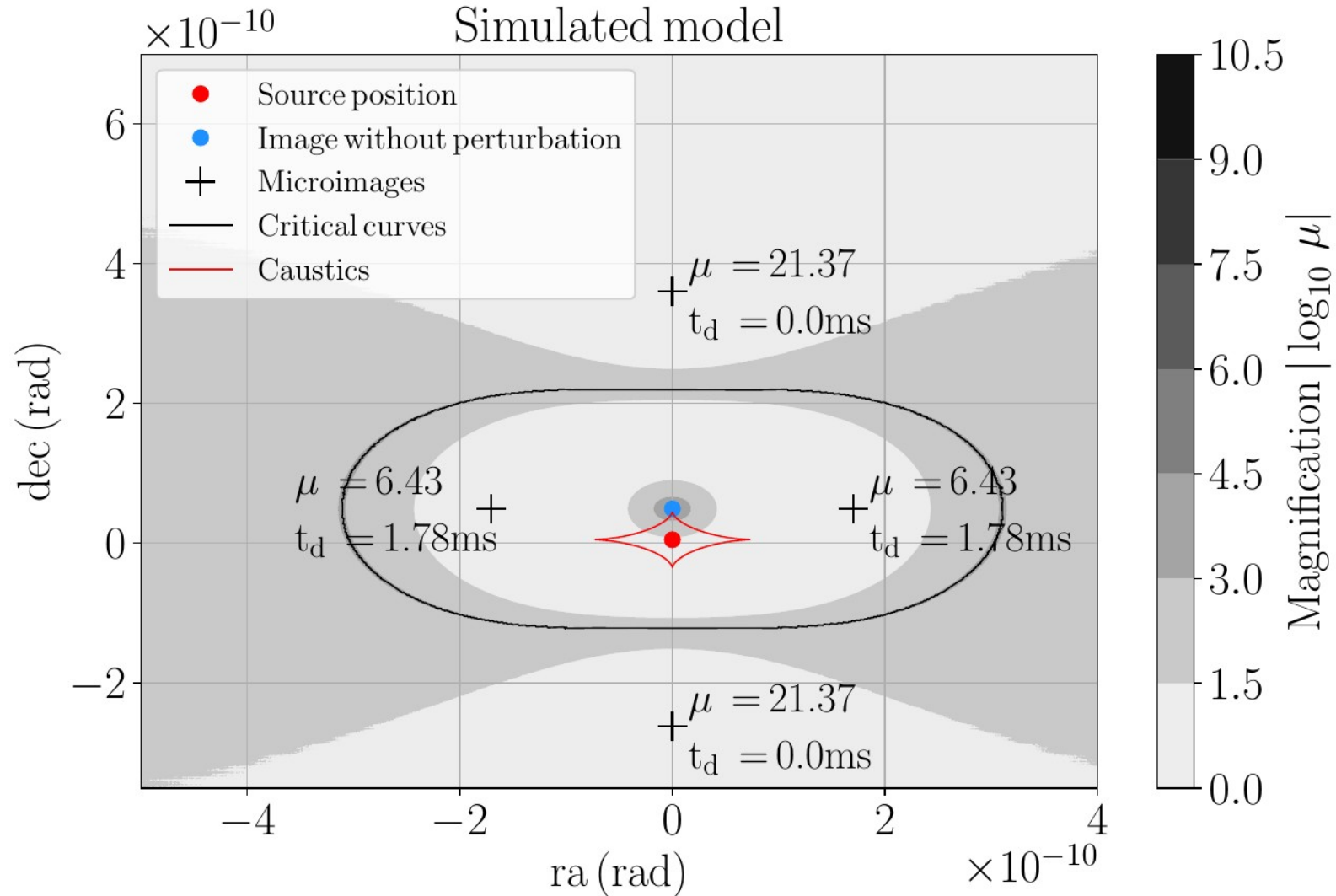
# Microlensing: Macromodels



# Microlensing: Macromodels



# Microlensing: Outlook

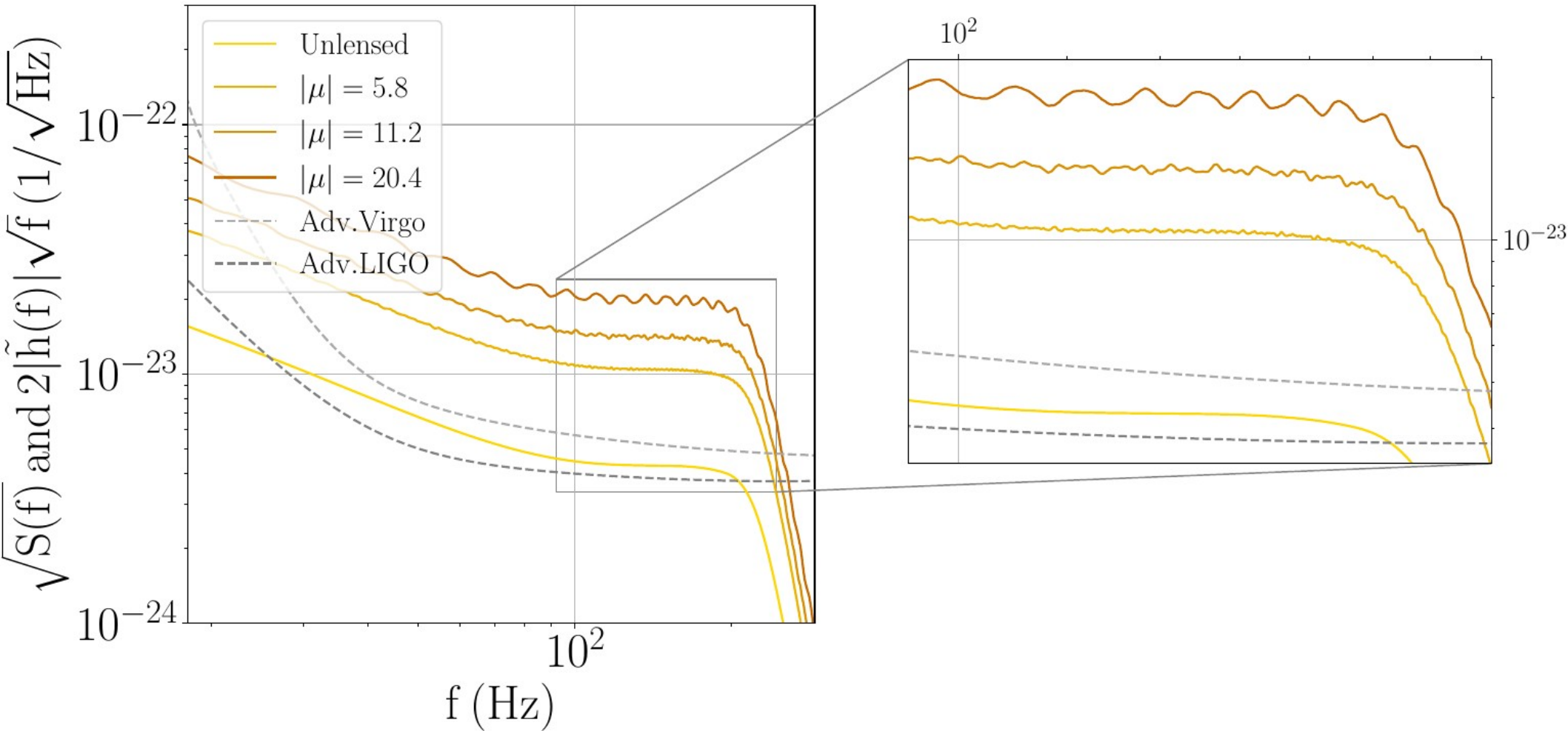


- Framework for generic microlensing configurations

Pagano et al., in prep.

- Waveform generation and analysis by lensingGW

# Microlensing: Outlook



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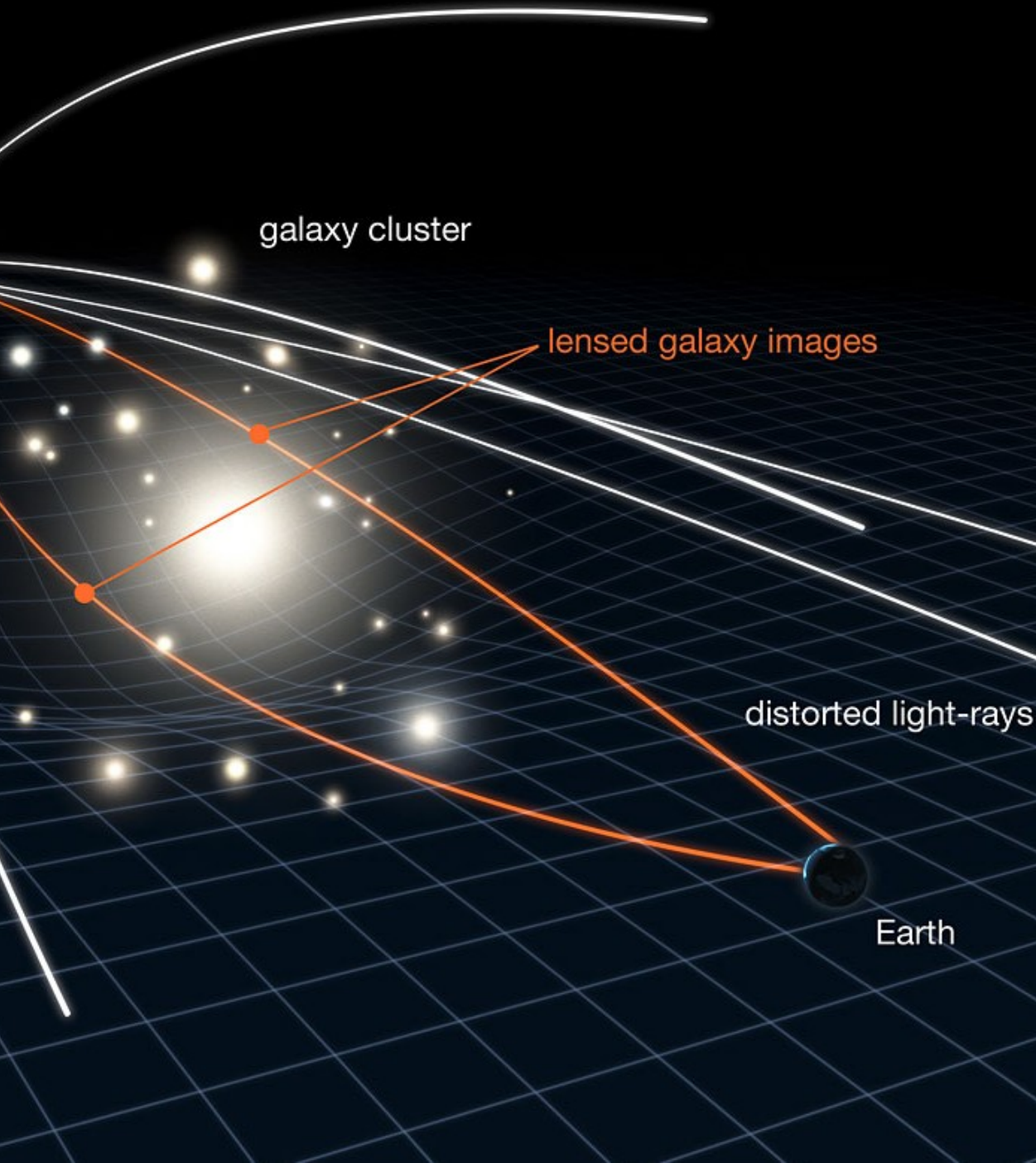


# Why study microlensing?

Example work:

- Study primordial black hole dark matter (Jung et al., 2019)
- Search for intermediate-mass black holes (Lai et al., 2017)
- Possibly smoking-gun evidence of strong lensing (Diego et al., 2019)
- Gravitational waves could allow for study of wave diffraction effects

# Gravitational-wave lensing



- Gravitational waves, like light, can be gravitationally lensed
- Strong lensing would cause the signal to be magnified and split into multiple images
- If the wave travels through substructures, it could experience microlensing
- Thus far, we have not found compelling evidence of Gravitational-wave lensing
- However, future analyses and detector upgrades allow for better sensitivity and improved searches