

# MULTI-MESSENGER EMISSION FROM MAGNETISED CORE-COLLAPSE SUPERNOVAE

Matteo Bugli<sup>1,2</sup>

Collaborators: J. Guilet<sup>2</sup>, T. Foglizzo<sup>2</sup>, R. Raynaud<sup>2</sup>, A. Reboul-Salze<sup>2</sup>,  
M. Obergaulinger<sup>3</sup>, M. Reichert<sup>3</sup>

<sup>1</sup>Physics Department - UniTo, Turin, Italy

<sup>2</sup>Astrophysics Department - IRFU/CEA-Saclay, Gif-sur-Yvette, Paris

<sup>3</sup>Departamento de Astronomía y Astrofísica, Universitat de València, Burjassot, Spain

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DI TORINO



# Outline of talk

- 1 Introduction
- 2 GW from standard CCSN
- 3 GW driven by rotation
- 4 Magneto-rotational explosions
- 5 Numerical models
- 6 Conclusions

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# Core-collapse Supernovae

- **Gravitational collapse** of a massive star (unstable iron core)
- **Shock formation** when nuclear densities are reached (stalling)  $\Rightarrow$  Proto Neutron Star
- **Shock expansion** and ejection of unbound material (explosion)

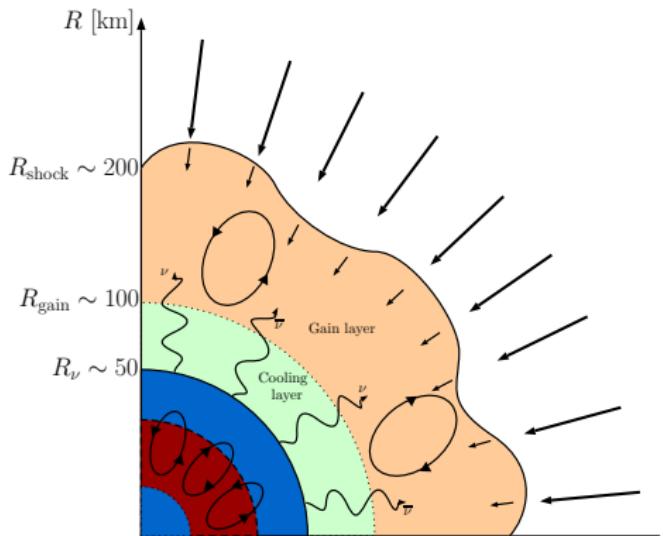


Credit: NASA/JPL-Caltech

Where does the binding energy ( $\sim 10^{53}$  erg) end up?

- Neutrino emission ( $\sim 99\%$ )
  - Ejecta ( $\sim 1\%$ )
- Gravitational waves ( $\sim 10^{-8}$ )

# Standard neutrino-driven CCSN



- PNS contraction  $\Rightarrow$  higher  $\nu$  energies
- $\nu$ -cooling rate drops faster than  $\nu$ -heating  $\Rightarrow$  **Gain radius**
- **Energy deposition** by  $\nu_e$  and  $\bar{\nu}_e$  absorption in gain layer
- **Multi-D hydrodynamic instabilities** aid the explosion
- Post-shock convection; Standing Accretion Shock Instability)

Neutrinos and GW directly probe the explosion mechanism

# Numerical models: (M)HD + nuclear EoS + neutrinos

## Uncertain initial conditions

- Progenitor thermodynamic profiles:  $\rho, s, P$
- Non-spherical perturbations

(Müller et al., 2017)

## Explodability

- Very compact cores resist to shock revival (O'Connor and Ott, 2011);
- Combination of mass accretion and entropy profiles

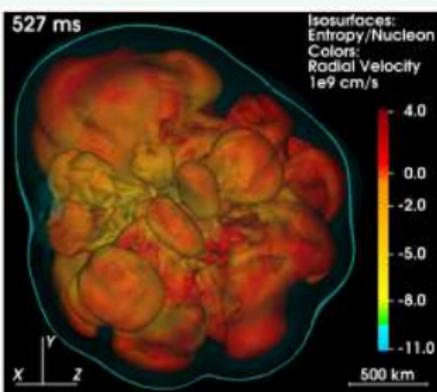
Ertl et al. (2016)

## PNS proper motions

- Asymmetries and fallback accretion  $\Rightarrow$  PNS kick velocity and spin (Janka et al., 2021)

## Hydrodynamic instabilities

- Post-shock convection ( $\nu$  energy deposition) and SASI
- 3D crucial
- Longer dwelling in gain region  
 $\Rightarrow$  more efficient heating



Janka et al. (2016)

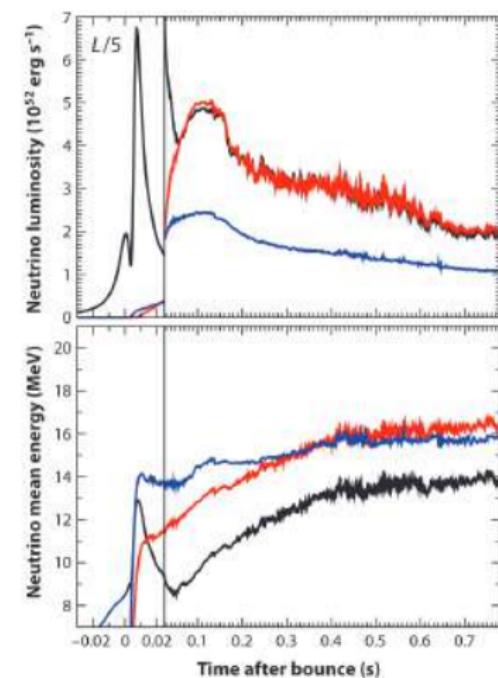
# Neutrino emission

## CCSN models

- **Onset of collapse:**  $\nu_e$  released from the core, then trapped
- **Neutronization burst:**  $\nu_e$  set free once the shock reaches low enough densities
- **Accretion phase:** high fluxes of  $\nu_e$  and  $\bar{\nu}_e$  in addition to the core luminosity

## Late PNS models

- **Cooling phase:** residual deleptonization and loss of binding energy



Janka (2012)

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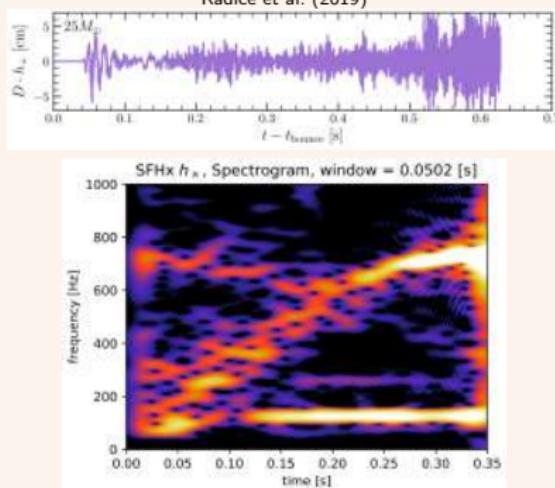
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# GW signals from standard CCSN

## Main features

- Perturbations induced in the PNS
- Highly stochastic
- g/f modes and SASI

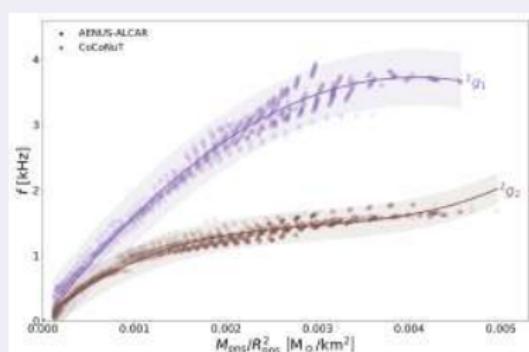
Radice et al. (2019)



Kawahara et al. (2018)

## Asteroseismology

- **Universal relations** between g/f modes freq. and  $M_{PNS}$ ,  $R_{PNS}$
- Same in 3D models?
- Other r modes?



Torres-Forné et al. (2019)

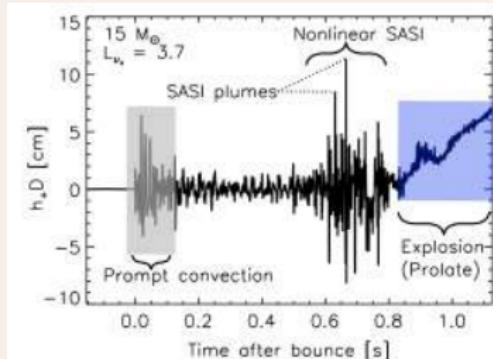
# Secondary features

## Prompt convection

- Onset due to shock propagation and  $\nu_e$  burst
- 50-100 Hz

## Memory

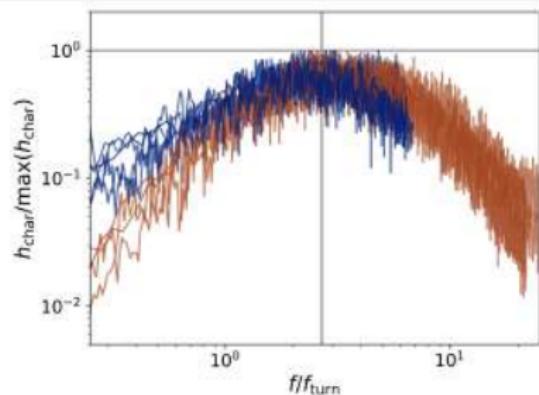
- 1-10 Hz (asymmetric explosions)



Murphy et al. (2009)

## Long-term convection

- Lepton-gradient driven PNS convection
- 100-1000 Hz



Raynaud et al. (2022)

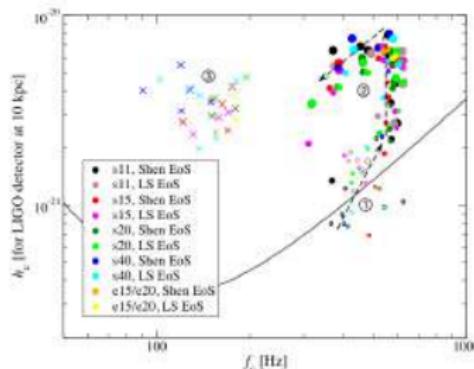
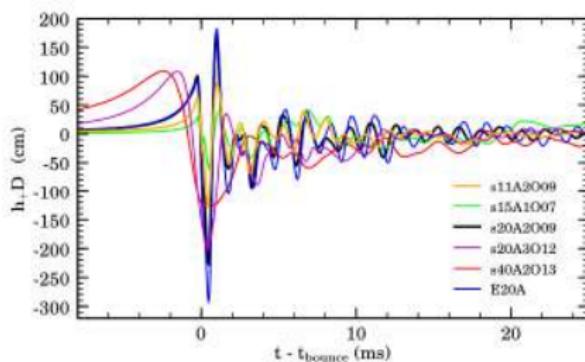
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# The impact of rotation

## Bounce signal

- Precollapse rotation  $\Rightarrow$  time-varying  $I = 2$  deformation of bouncing core
- Most favourable for moderate/rapid rotation ( $\Omega_c \in [1 - 10]$  rad/s)

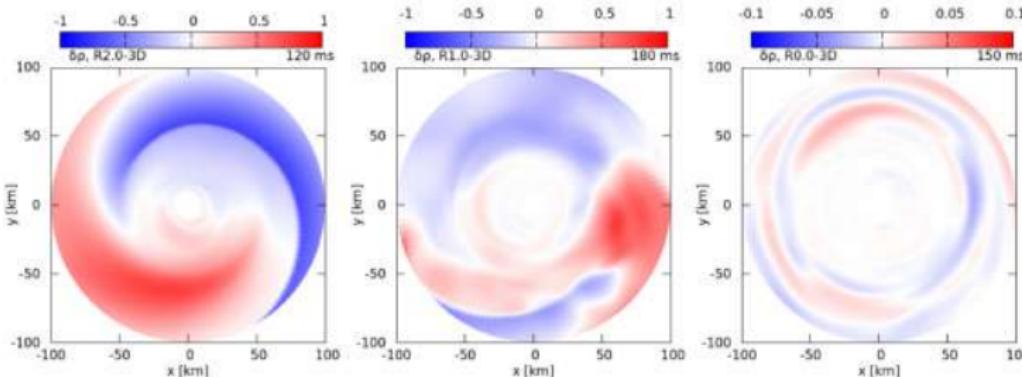
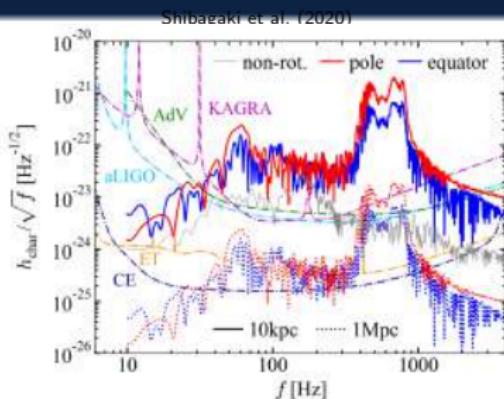


Ott (2009)

# Corotational instabilities

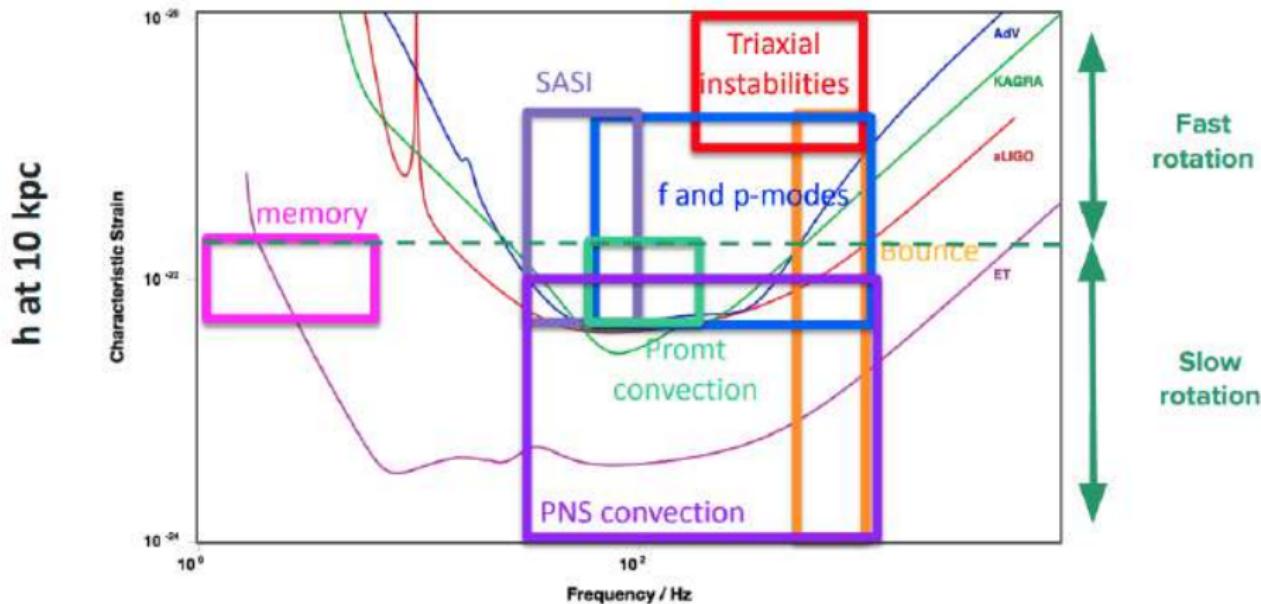
- Growing non-axisymmetric large-scale modes with fast rotation
- Low  $T/|W|$  instability associated to GW emission

(Shibagaki et al., 2020; Takiwaki et al., 2021).



Takiwaki et al. (2021)

# Summary of physical sources of GW



Credit: Pablo Cerdà-Durán

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# Outstanding explosions and magnetic fields

## Explosion kinetic energy

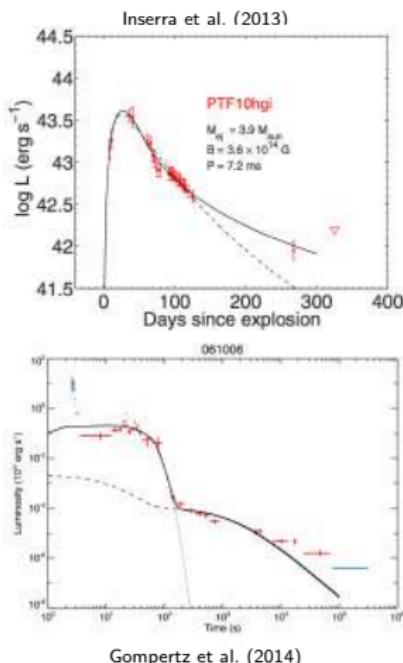
- Typical supernova:  $10^{51}$  erg
- Rare hypernovae and GRBs:  $10^{52}$  erg

## Total luminosity

- Typical supernova:  $10^{49}$  erg
- Superluminous SN:  $10^{51}$  erg

## Lightcurves and X-ray plateaus

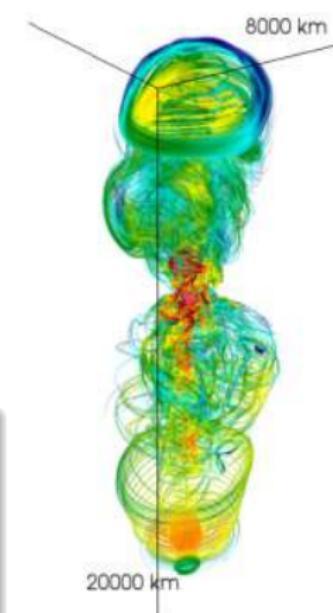
- Strong dipolar magnetic field:  
 $B \sim 10^{14} - 10^{15}$  G
- Fast rotation:  $P \sim 1 - 10$  ms
- Kasen and Bildsten (2010); Dessart et al. (2012); Nicholl et al. (2013);  
Zhang and Mészáros (2001); Metzger et al. (2008); Lü et al. (2015); Gao et al. (2016)



# Magneto-rotational explosions

## Core mechanism

- **Rotation**  $\Rightarrow$  energy reservoir
- **Magnetic fields**  $\Rightarrow$  means to extract that energy through magnetic stresses
- **Powerful jet-driven explosions** (Shibata et al., 2006; Burrows et al., 2007; Dessart et al., 2008; Takiwaki et al., 2009; Kuroda and Umeda, 2010; Winteler et al., 2012; Obergaulinger and Aloy, 2017)

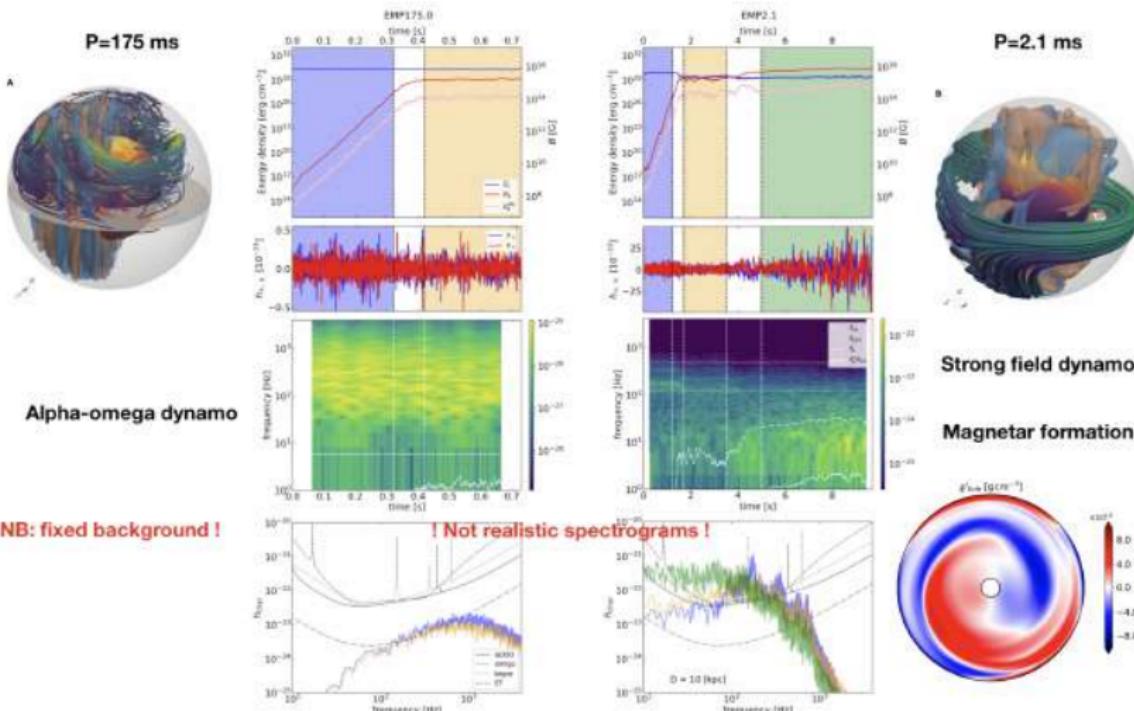


## Origin of the magnetic field

- **Progenitor** (Woosley and Heger, 2006; Aguilera-Díaz et al., 2020)
- **Stellar mergers** (Schneider et al., 2019)
- **PNS dynamo:**
  - **Convection** (Raynaud et al., 2020)
  - **Magnetorotational Instability** (Reboul-Salze et al., 2021, 2022)
- **Taylor-Spruit** (Barrère et al., 2022)

Obergaulinger and Aloy (2021)

# Convective dynamo in PNS



Raynaud et al. (2022)

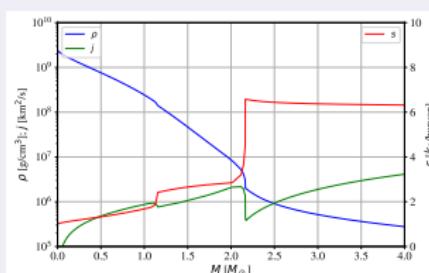
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# 3D MHD explosion models

(Bugli et al., 2021)

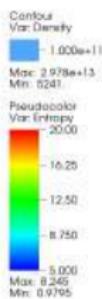
- 35OC: massive, fast rotating stellar progenitor (Woosley and Heger, 2006)
- Rotation profile from stellar evolution model
- Different magnetic configurations: dipole (aligned and equatorial) or quadrupole (motivated by PNS dynamos; Raynaud et al. (2020); Reboul-Salze et al. (2021, 2022))



## Multipolar poloidal field

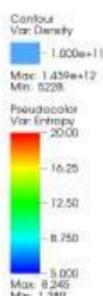
$$A_{\phi,I} = r B_0 \frac{\sqrt{I}}{2I+1} \frac{r_0^3}{r^3 + r_0^3} \frac{P_{I-1}(\cos \theta) - P_{I+1}(\cos \theta)}{\sin \theta}$$

# Hydrodynamic model



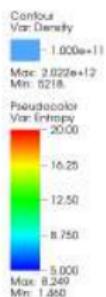
Time = 0 ms p.b.

# Aligned dipole



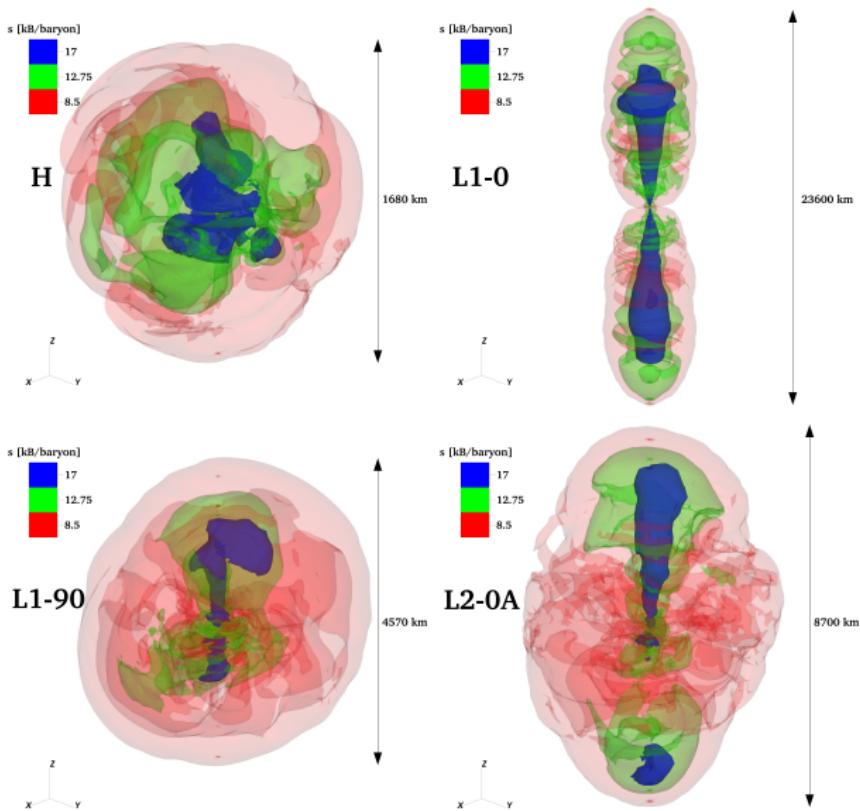
Time = 0 ms p.b.

# Equatorial dipole



Time = -17 ms p.b.

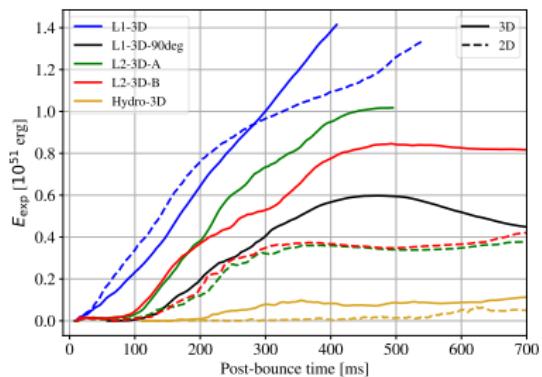
# Explosion Morphology



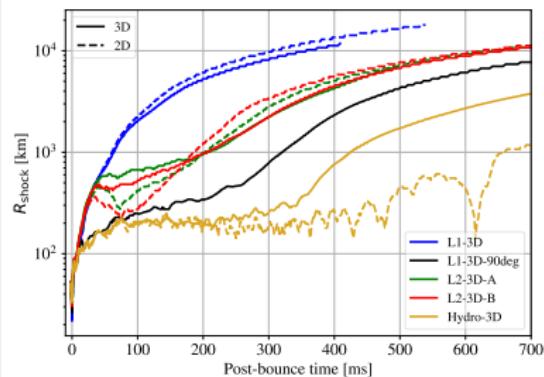
# Explosion dynamics

(Bugli et al., 2021)

## Ejecta energy



## Shock expansion

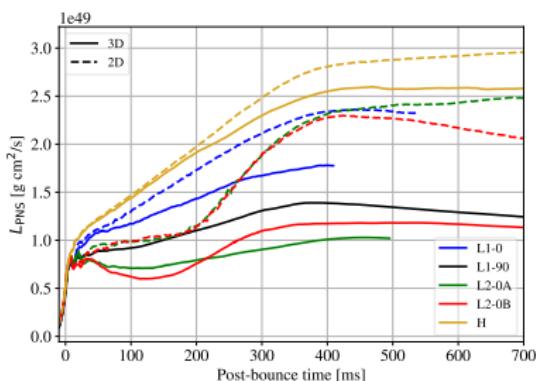


- Stronger explosions for lower multipoles and aligned configurations
- 3D generally more energetic

- Faster shock expansion for stronger explosions
- 2D faster than 3D in magnetized models

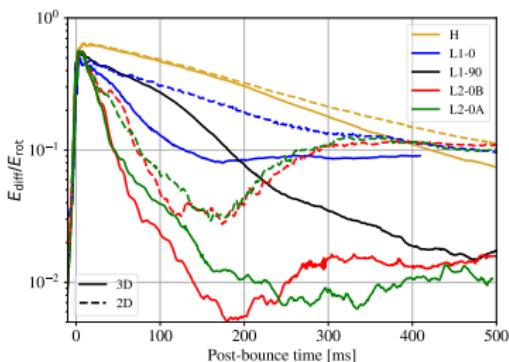
# Angular momentum transport

## PNS angular momentum



- Magnetic stresses slow down the PNS

## PNS differential rotation



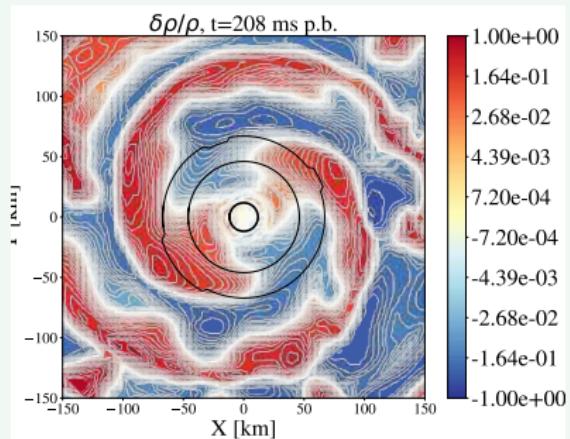
- Fast redistribution of differential rotation in magnetized models

- Quadrupolar fields more efficient than dipolar ones
  - 3D more efficient than 2D

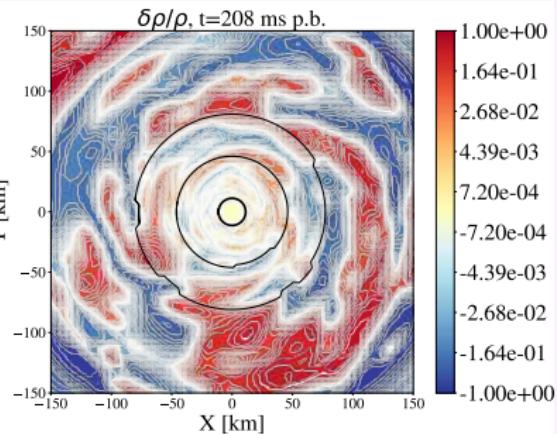
# The low $T/|W|$ instability

(Bugli et al., sub. to MNRAS)

Hydrodynamic case



Magnetized case

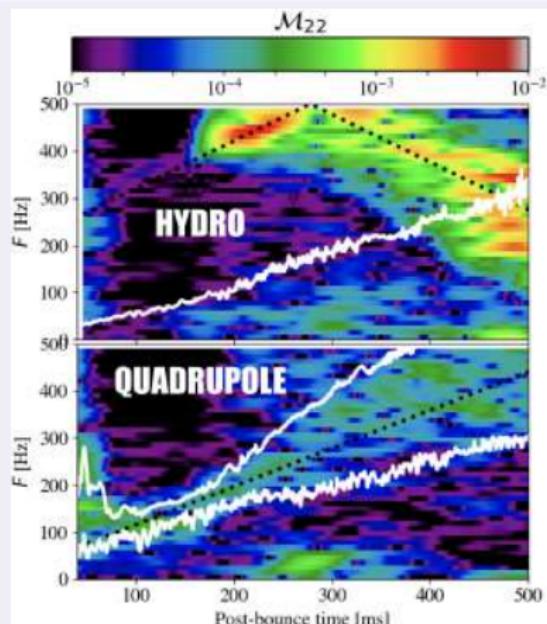
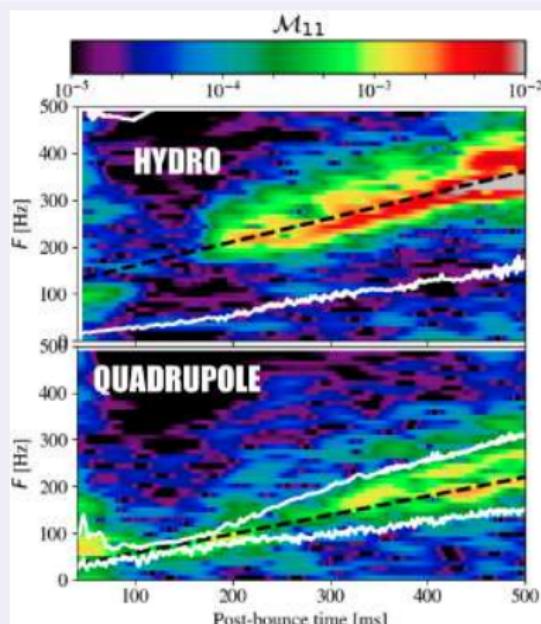


- Spiral structures forming at  $\sim 200$  ms p.b.
- Observed for different progenitors/rotation profiles (Takiwaki et al., 2016, 2021)

- No spiral structures
- Smaller-scale density perturbations
- Weak dependence on magnetic field

# PNS oscillation modes

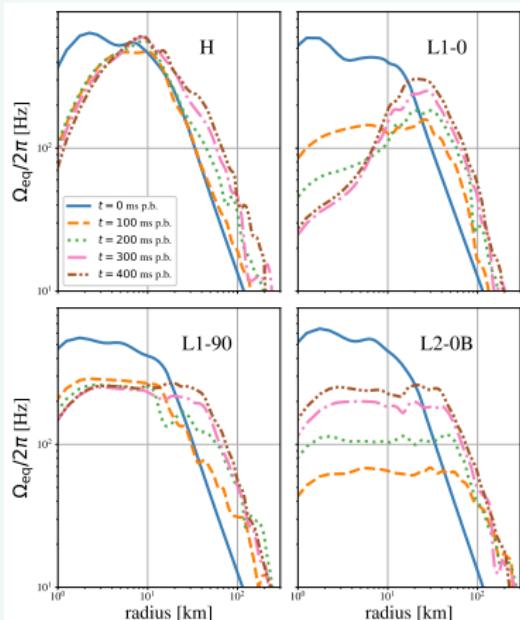
Density modes at 30 km ( $\{l, m\} = \{1, 1\}$  and  $\{2, 2\}$ )



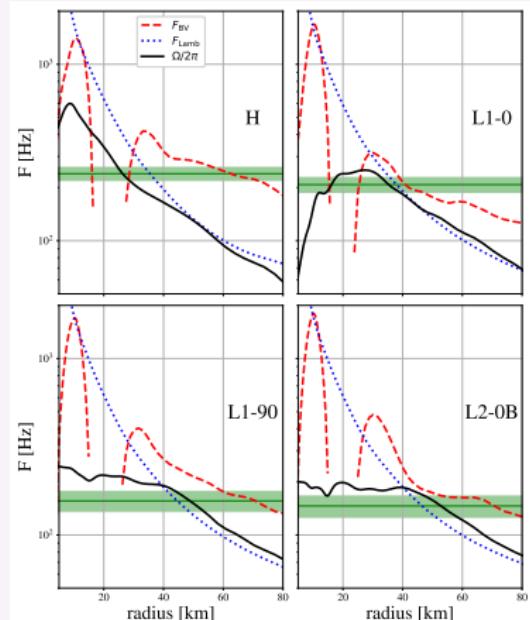
- Strong  $l = 1, 2$  non-axisymmetric modes in the hydrodynamic case
- Weaker modes in magnetized models

# Magnetic transport of angular momentum

Rotation profile evolution



Mode's frequency

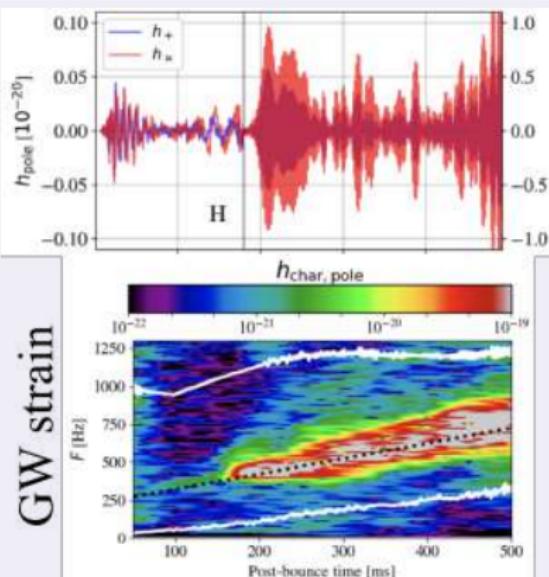


- Distinctive dynamics for each model
- Strongest flattening for quadrupolar fields

- Corotation radius outside the convective zone  $\Rightarrow$  stable against low  $T/\|W\|$  (Takiwaki et al., 2021)

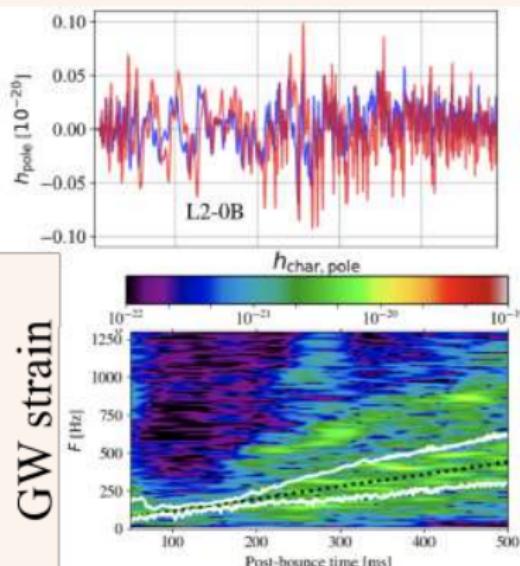
# GW emission

Hydrodynamic case



GW strain

Magnetized case (quadrupole)



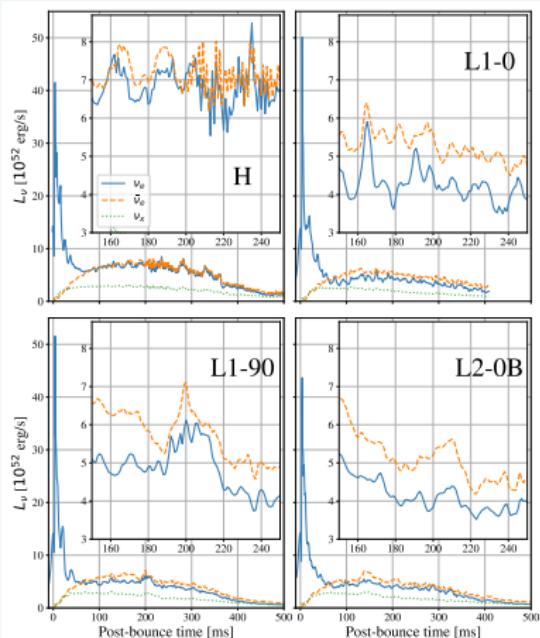
GW strain

- 400 Hz emission at 200 ms
- $h \sim 10^{-20}$  for  $D = 10$  kpc
- Strong correlation with PNS modes

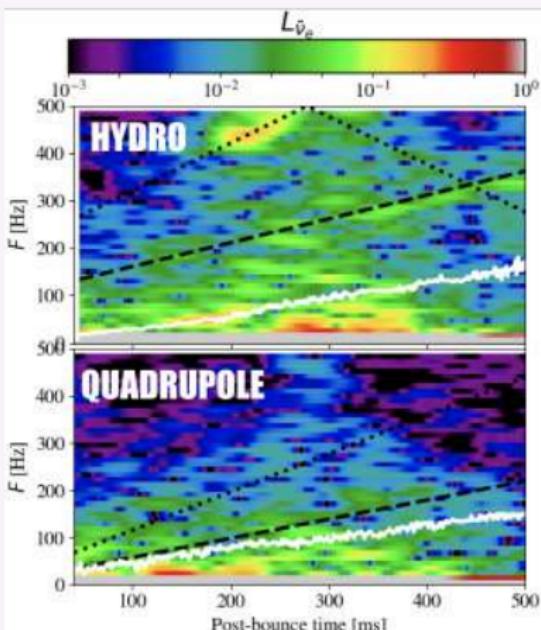
- No low  $T/|W|$  signal burst
- $h \sim 5 \times 10^{-22}$  for  $D = 10$  kpc
- Strong transport of AM

# Neutrino emission

## Lightcurves (equator)



## PNS modes signatures

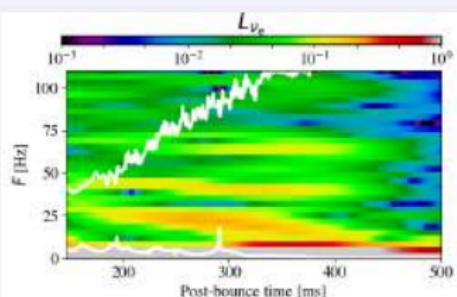
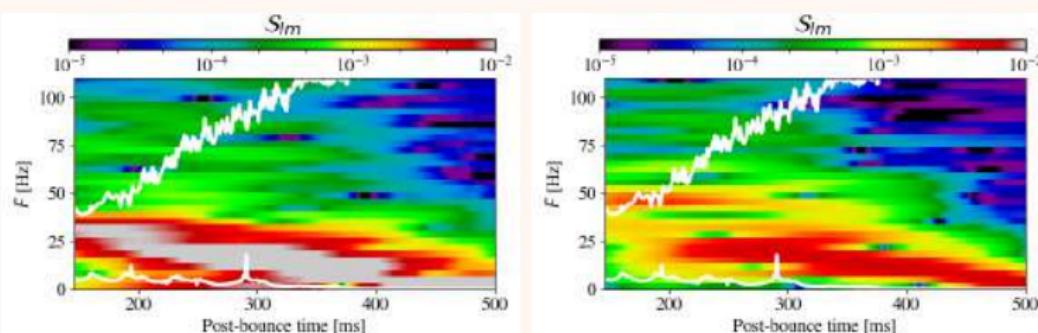


- Lower luminosity in MHD
- $\nu_e - \bar{\nu}_e$  asymmetry

- low  $T/|W|$  and SASI signatures

# Neutrino SASI signature

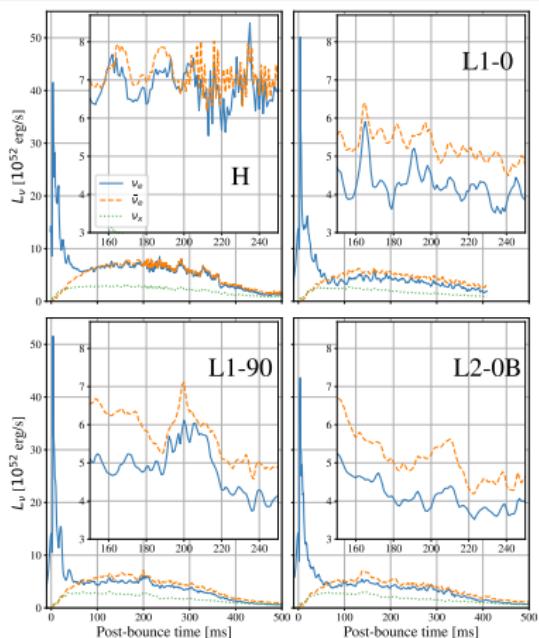
Shock's surface modes: (1,1), (2,2)



- Low-frequency signature of **spiral SASI modes**  $\sim 20 - 30$  Hz
- **Decreasing frequency and short duration** for exploding models

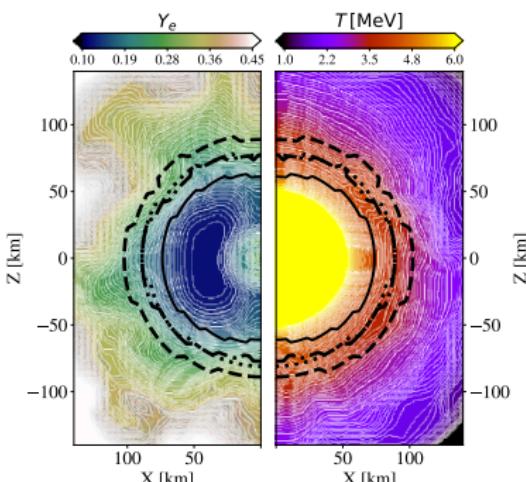
# Electron fraction distribution

## Lightcurves (equator)



- Lower luminosity in MHD
- $\nu_e$ - $\bar{\nu}_e$  asymmetry

## $Y_e$ distribution

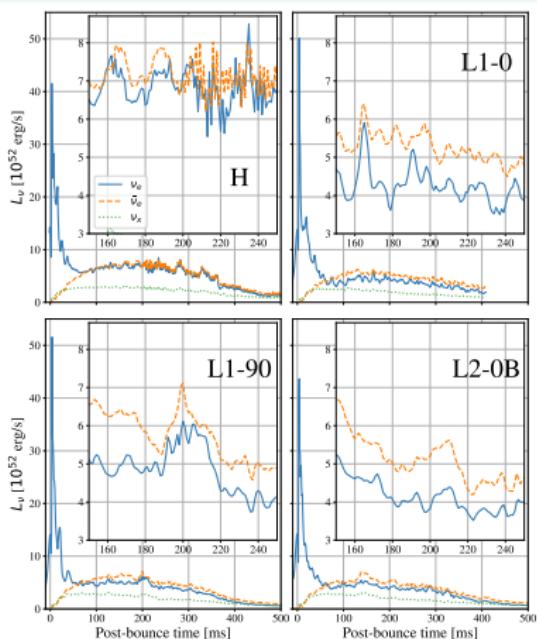


Hydrodynamic model

- More compact PNS  $\Rightarrow$  higher mean energies

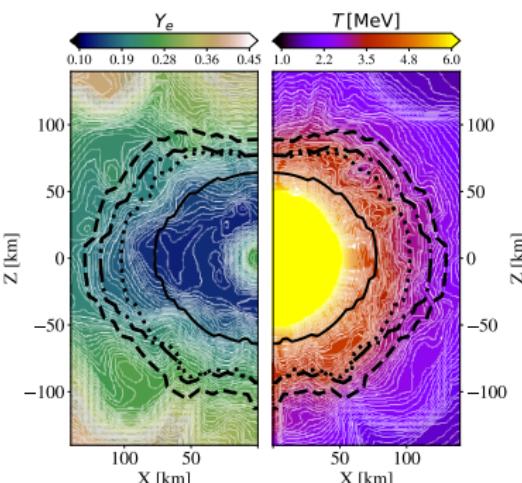
# Electron fraction distribution

Lightcurves (equator)



- Lower luminosity in MHD
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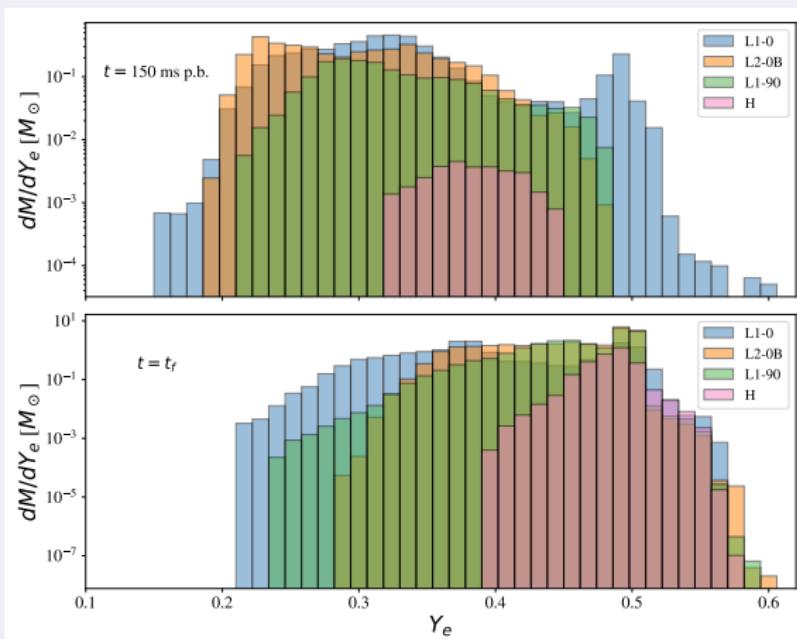
$Y_e$  distribution



Quadrupolar model

- Outward transport of a.m.  $\Rightarrow$  lower  $Y_e$

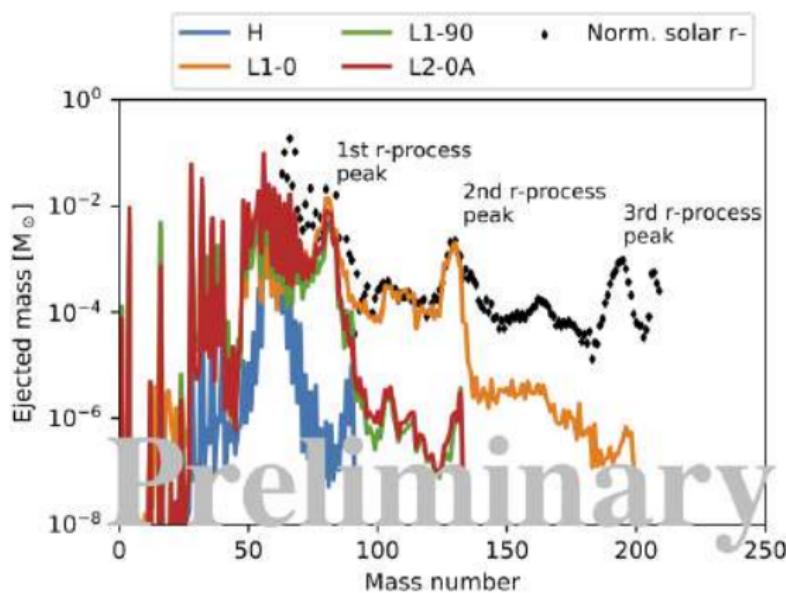
# Nuclear composition of the ejecta



- More neutron-rich material for magnetized models
  - Lowest  $Y_e$  for dipolar fields
- Longer simulations required to reduce uncertainties

# Explosive nucleosynthesis

(Reichert et al., in prep.)



- All magnetized models produce **1st r-process peak elements**
  - **2nd peak** only for the aligned dipole
- **No 3rd peak**, consistent with recent 3d models (Reichert et al., 2022) and in contrast to 2d models (Reichert et al., 2021).
- Crucial estimates for **chemical evolution models** (Dvorkin et al., 2020)

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## Conclusions

- GW open a **unique window** on the central engine dynamics
  - Signatures from **fluid instabilities** (convection, SASI, low  $T/|W|$ )
  - Both **rotation** and **magnetic fields** deeply affects the GW emission
  - **Low  $T/|W|$**  produces high amplitude GW, but quenched by strong magnetic fields
    - Important **correlations** between GW and neutrinos

### Future goals

- Impact of weaker magnetic fields
  - Dependence on the rotation profile
  - Fundamental physical mechanism behind low  $T/|W|$ 
    - Impact on explosive nucleosynthesis

## Join Movember!



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Introduction  
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GW from standard CCSN  
ooo

GW driven by rotation  
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Magneto-rotational explosions  
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Numerical models  
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# BACKUP SLIDES

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