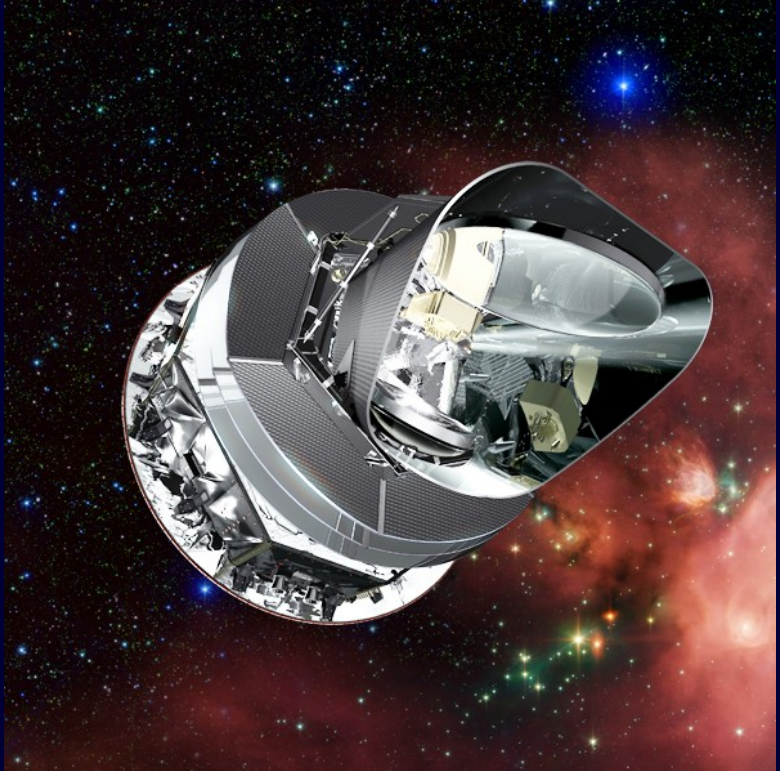


Cosmic Beginnings and Cosmic Fate

ou: La révolution non-Gaussienne

Benjamin D. Wandelt
Institut d'Astrophysique de Paris
Université Pierre et Marie Curie



Why cosmology?

The big questions are:

“How did the Universe begin
(if it did)?”

“Whence the laws of Nature?”

Why cosmology?

The big questions are:

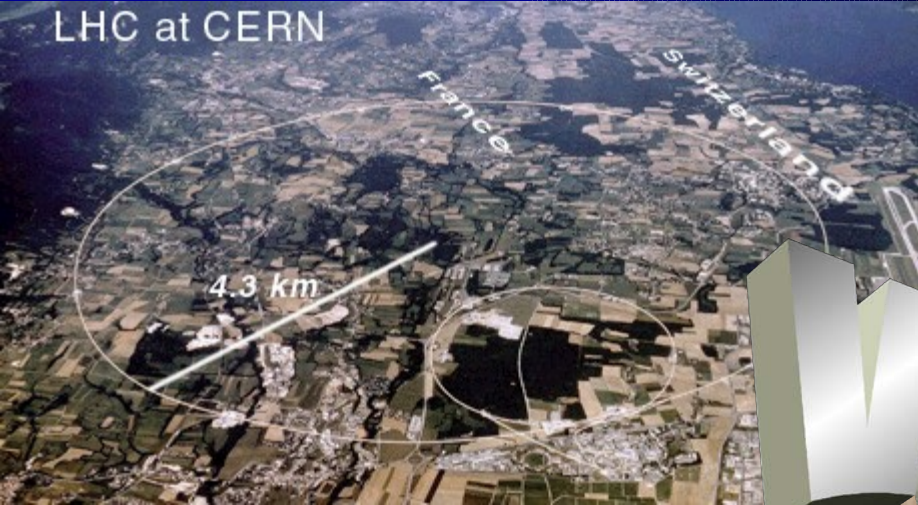
“What happened at $t = 0$?”

“What is the fundamental theory,
valid at the highest energies?”

How do we study what happens at the highest energy scales and at the shortest time scales?

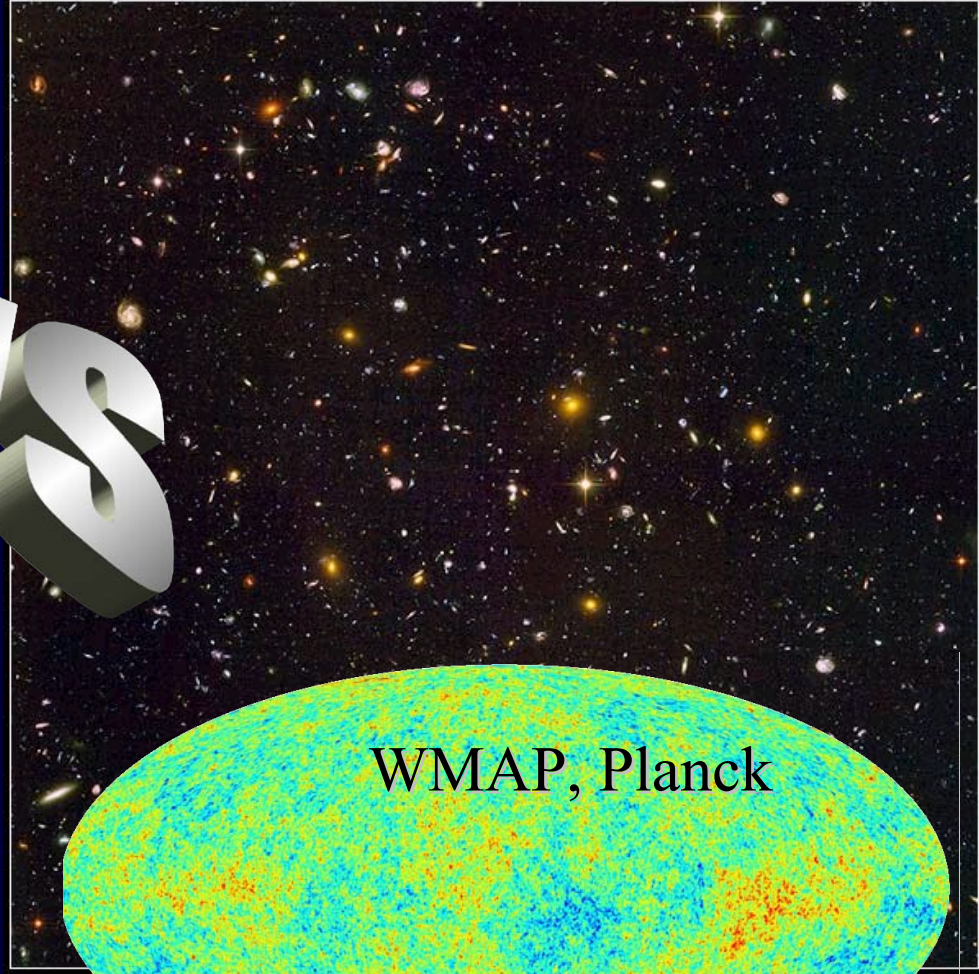
Showdown

LHC at CERN

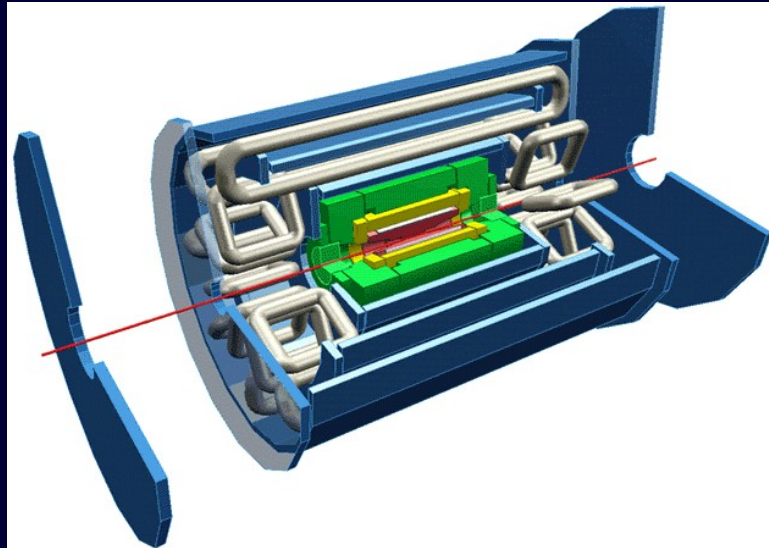


Hubble Ultra Deep Field

HST • ACS



vs



WMAP, Planck

NASA, ESA

04-07a

-0.00046 0.00046

Energy and Time scales



Planck energy

(Quantum Gravity)

Unification of forces

CERN

...

Everyday energies

Low energies

Planck time 10^{-42} s

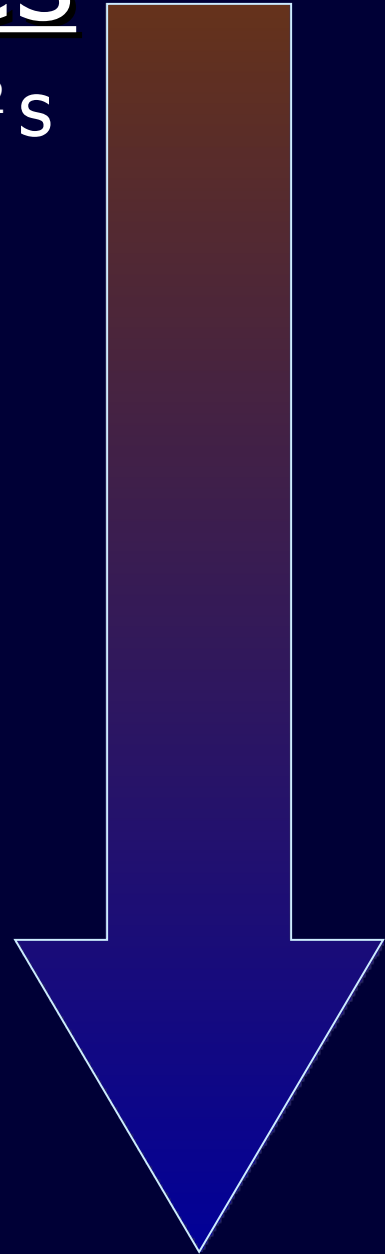
...

...

10^{-22} s

nanoseconds

seconds



Will accelerators work?

Planck energy

Planck time 10^{-42} s

(Quantum Gravity)

...

Unification of forces

Hard technological limit:

10^{-22} s

CERN

...

Everyday energies

nanoseconds

Low energies

seconds

Accelerators are very useful

But: basically, trying to study physics at the very highest energies in a particle accelerator is **too ambitious**.

It's brute force.

It involves creating early Universe conditions in the lab.

“Can Astronomy do better
than accelerators?”

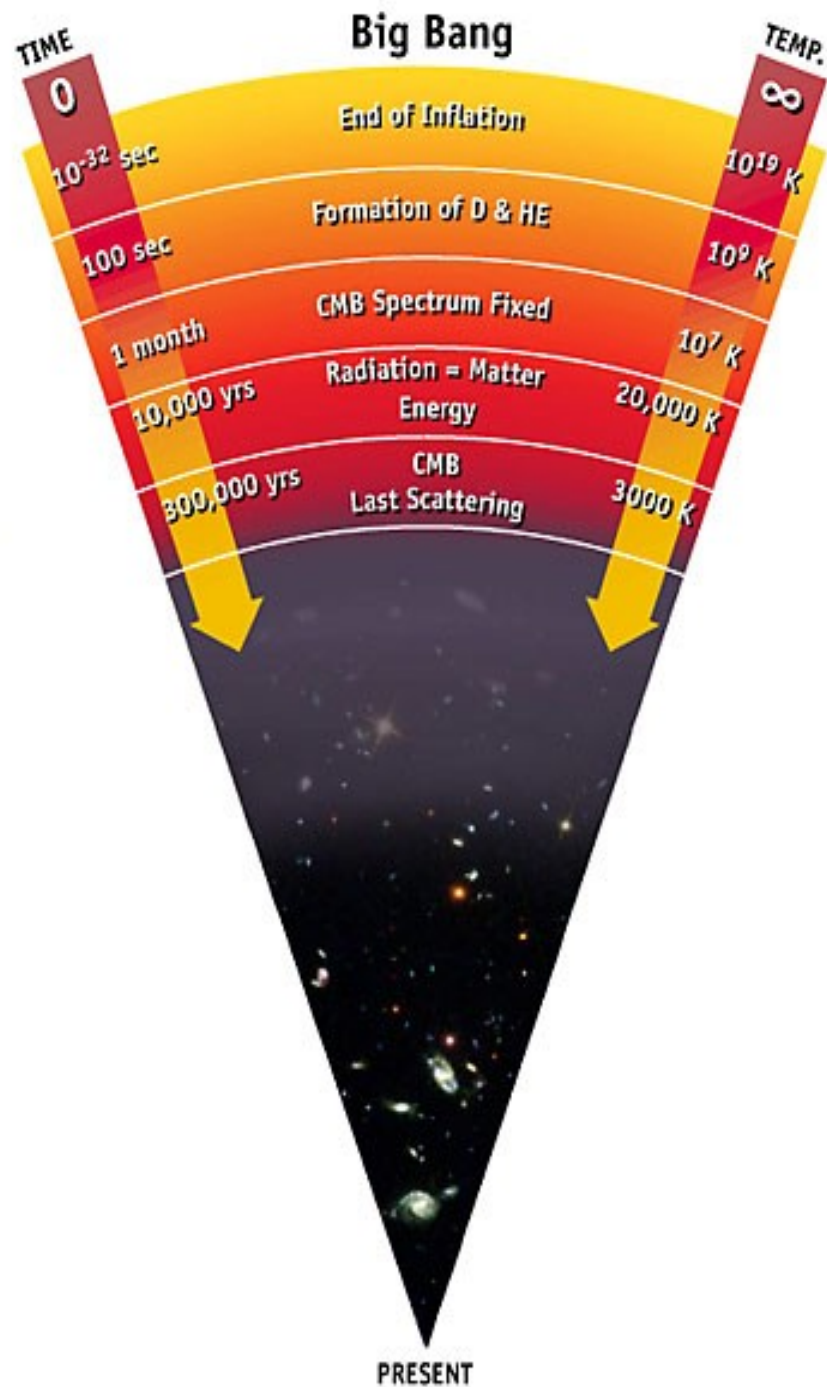


Enter: the Cosmic Microwave Background (CMB)

What is the Cosmic Microwave Background?

Before the Universe turned $\sim 380,000$ years old, it was hot and dense, a plasma opaque to photons.

When it cooled to 3000 Kelvin, electrons and protons combined into neutral H atoms and the Universe became transparent (**decoupling**).



What is the CMB?

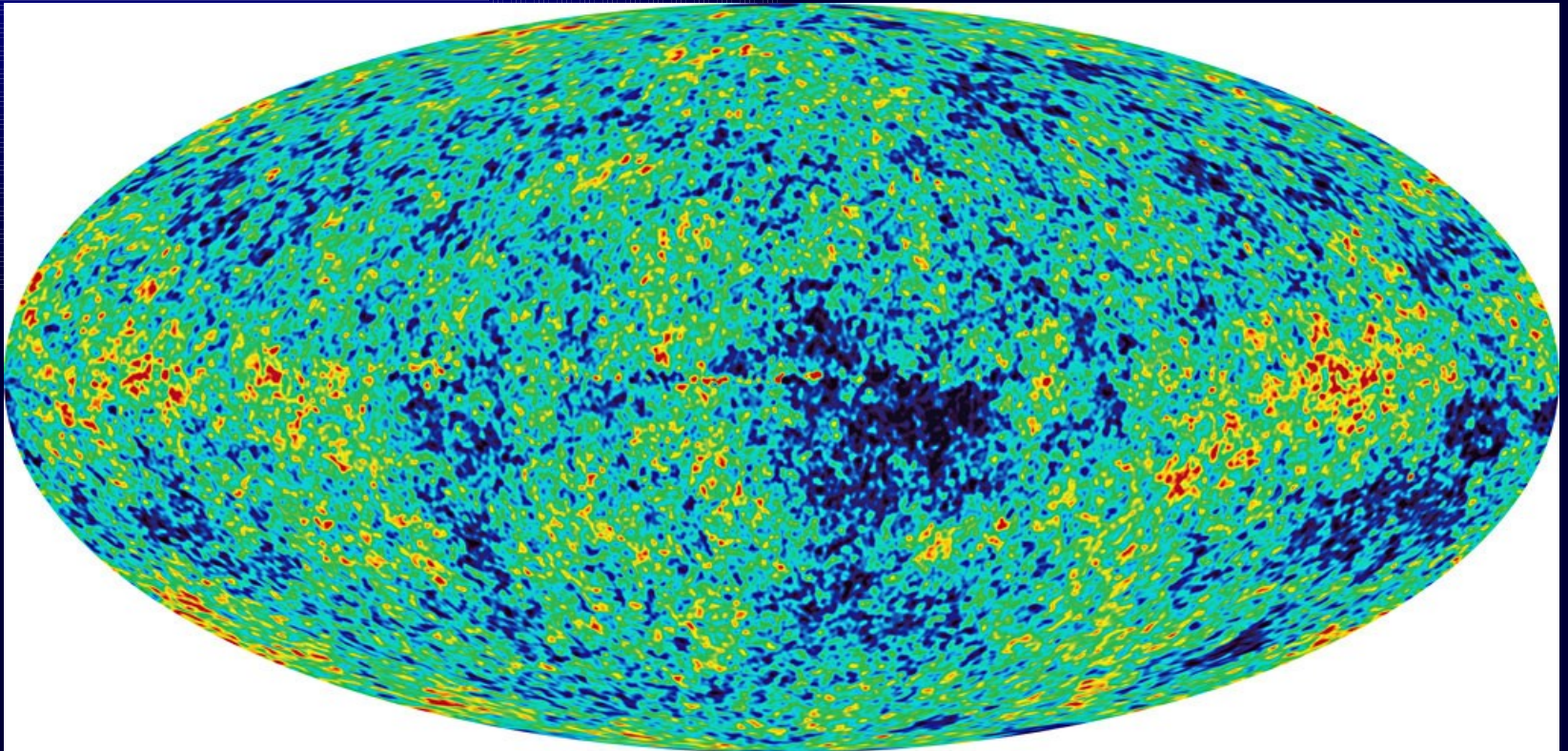
Photons we see today which interacted with matter last at **decoupling** make up the Cosmic Microwave Background (CMB).

Gravitational potential perturbations in the infant universe cause anisotropies in the CMB.

So the CMB is the ultimate
time-capsule

The Universe conveniently
sent us a baby picture of
itself!

And here it is

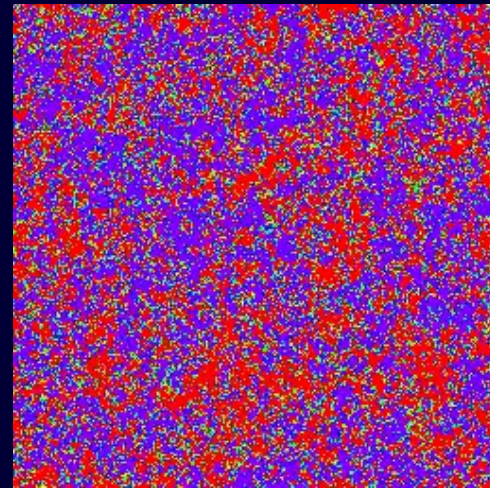


credit: WMAP

We'd like to probe structure formation

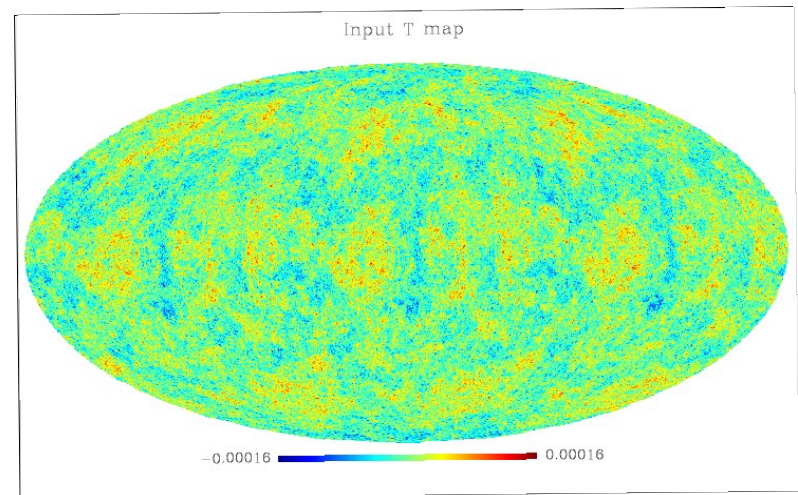
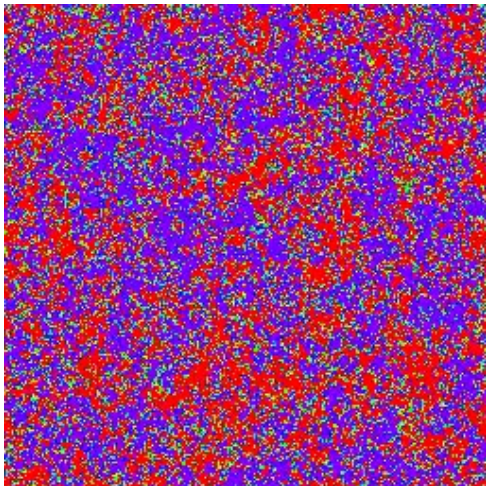
Some quantum mechanical fluctuations, e.g. during inflation, seed potential **perturbations** in a huge, smooth Universe

How do we get back to these very early times (fractions of a second)?



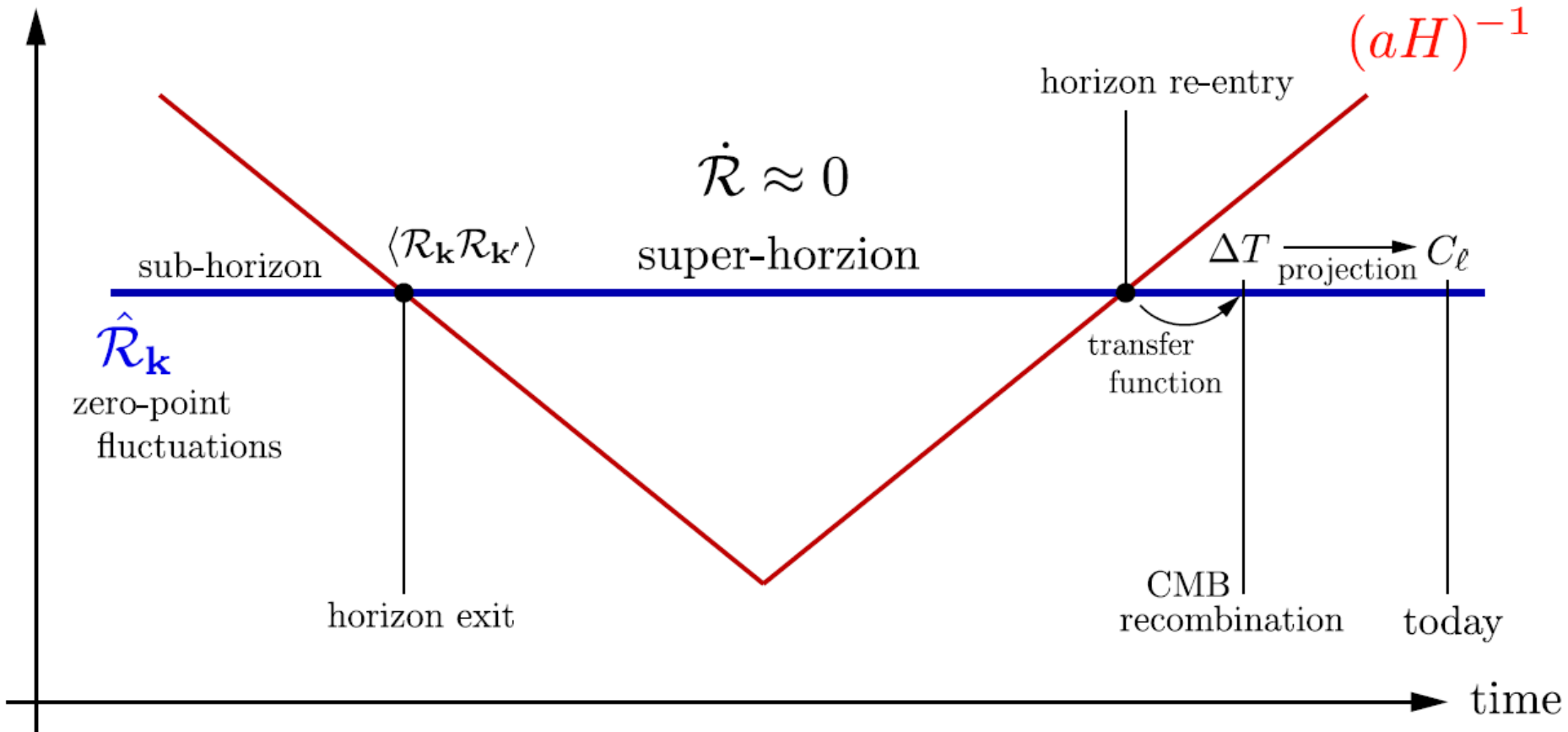
Part II of the time machine:

Calculating back from the Cosmic Microwave Background to the primordial perturbations



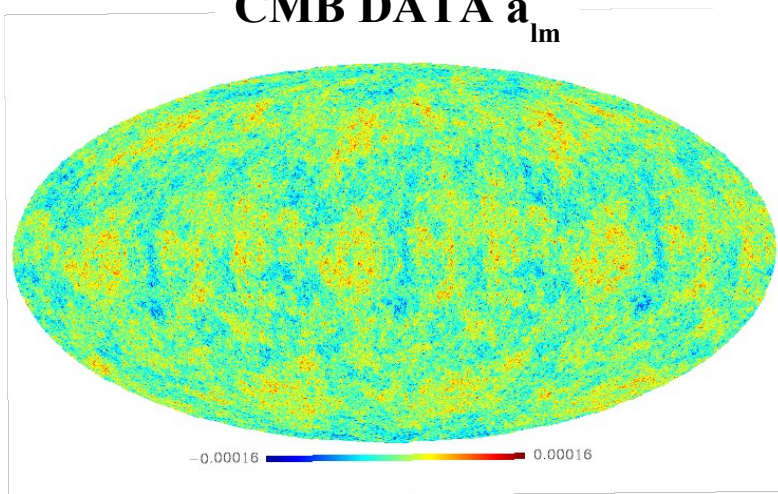
Imprinting primordial perturbations

comoving scales



Reconstructing Primordial Perturbations

CMB DATA a_{lm}



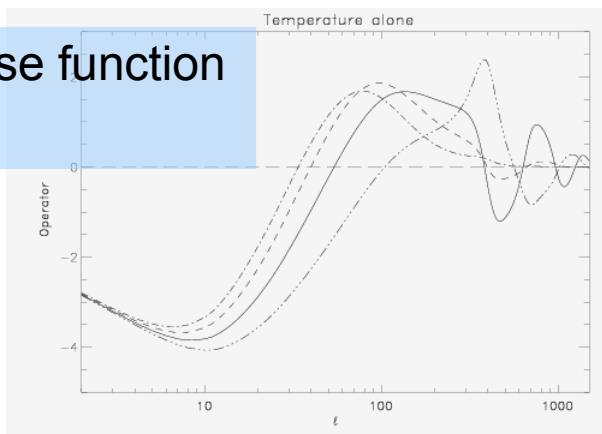
$$\Phi_{lm} = O_l a_{lm}$$

SW limit

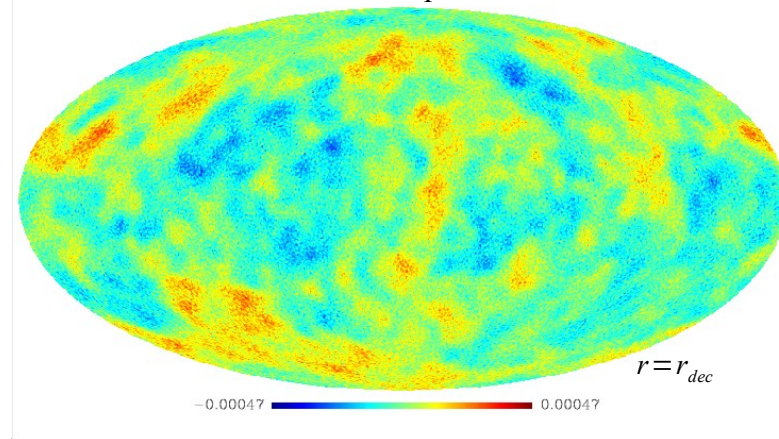
$$\frac{\delta \phi}{\phi} = -3 \frac{\delta T}{T}$$

Response function

$$O_l = \beta / C_l$$



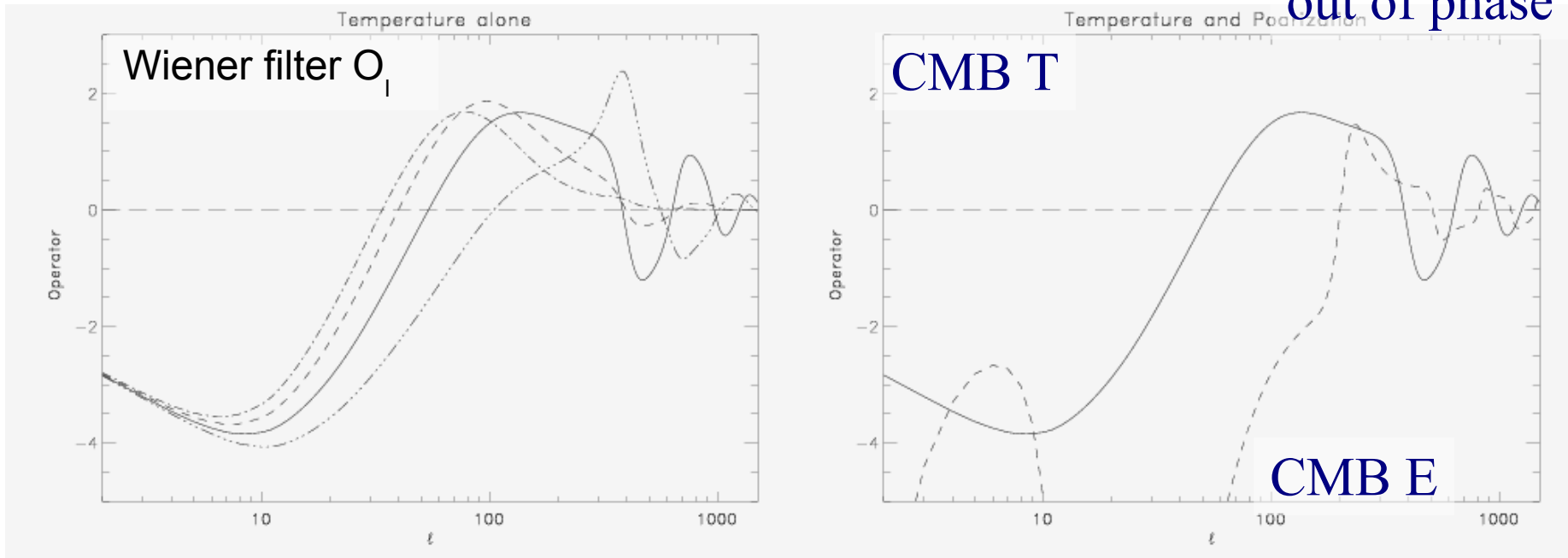
Reconstructed Primordial perturbations with T alone



$$\beta_\ell^i(r) = \frac{2b_\ell^i}{\pi} \int k^2 dk P_\phi(k) g_\ell^i(k) j_\ell(kr).$$

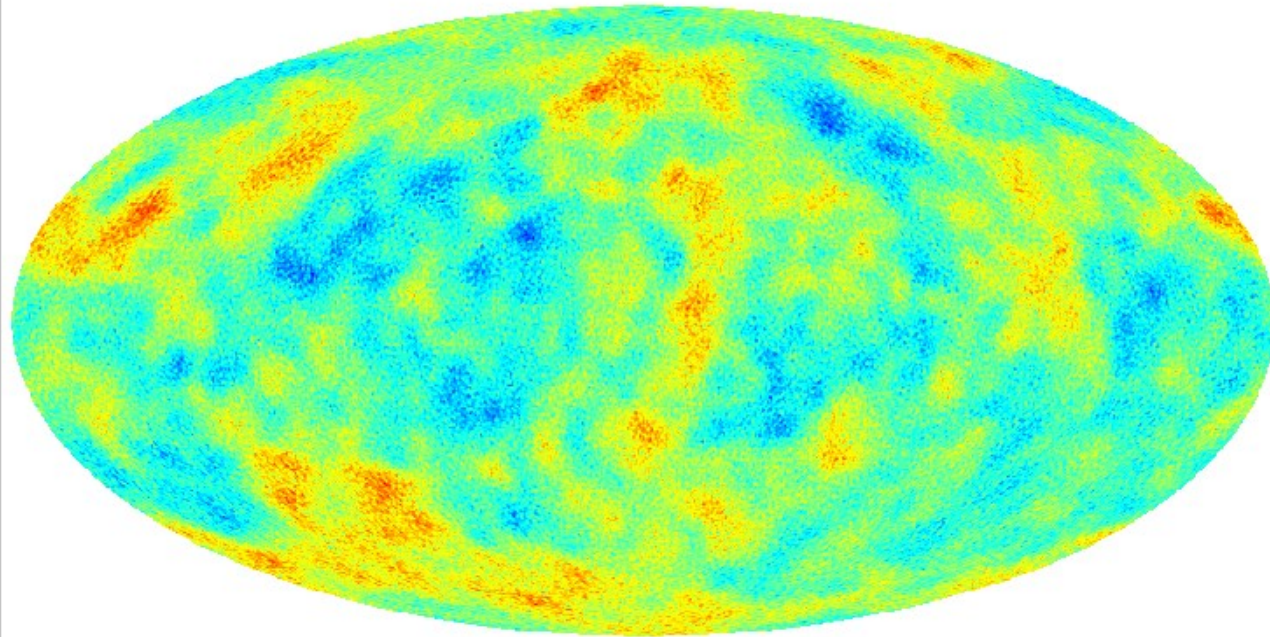
The curvature perturbation leaves a unique signature also in the polarization anisotropies

- Note negative response on large scales T and E are out of phase



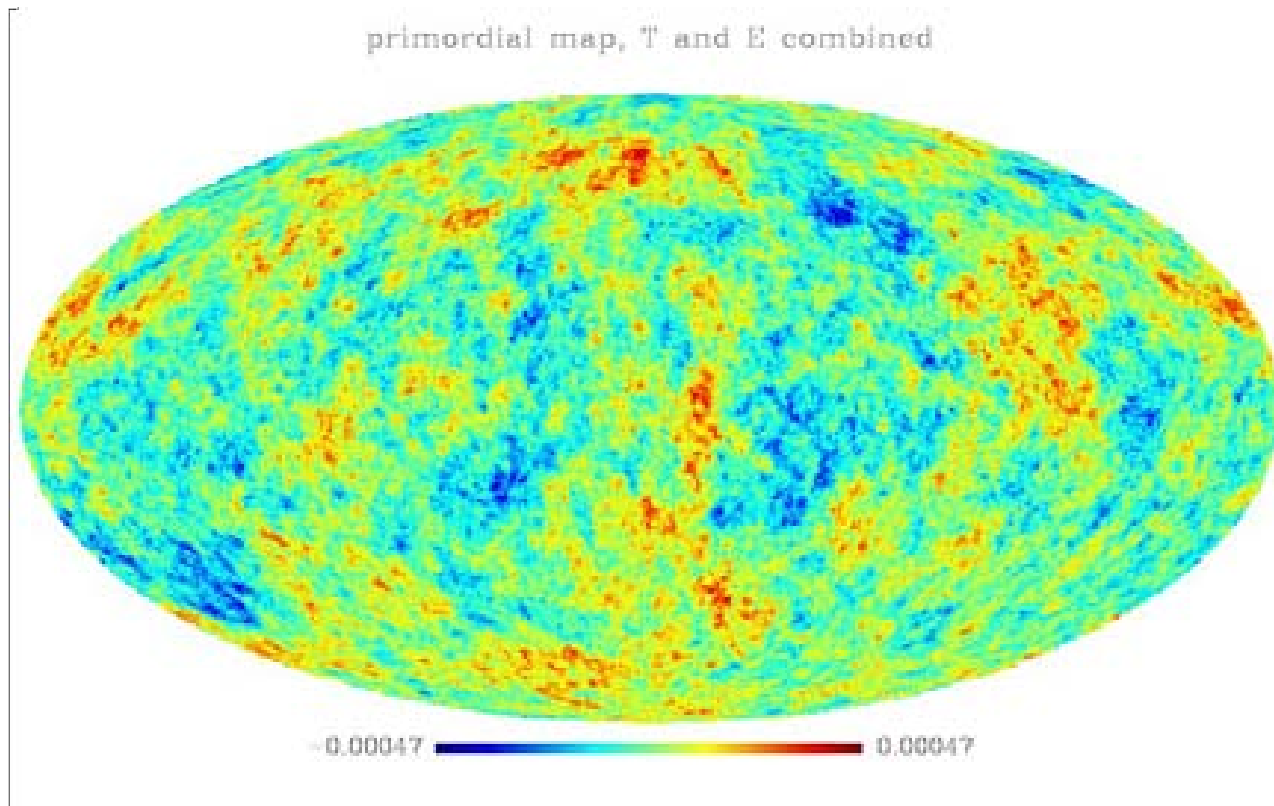
Yadav, and Wandelt, PRD (2005)

primordial map, using T alone



-0.00047 0.00047

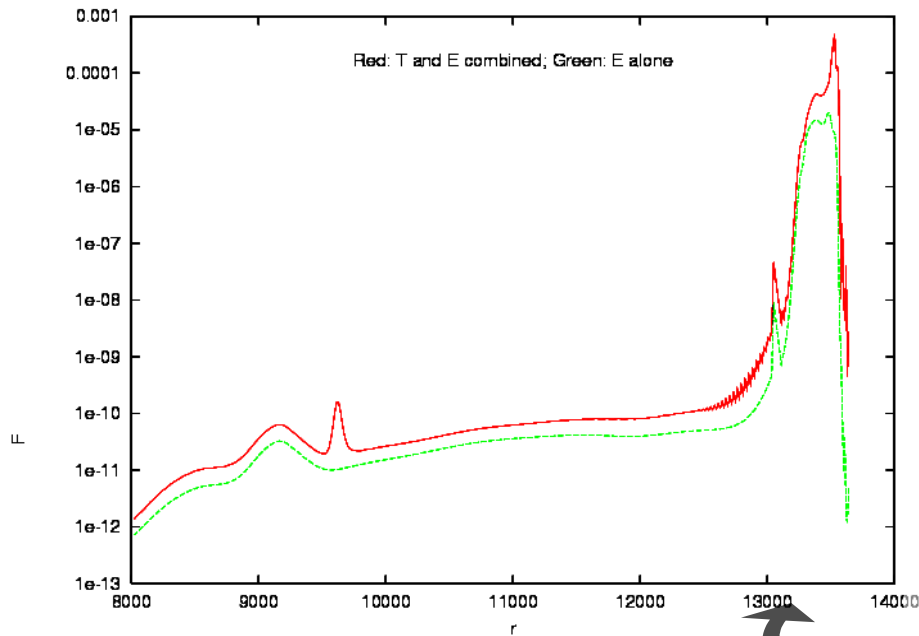
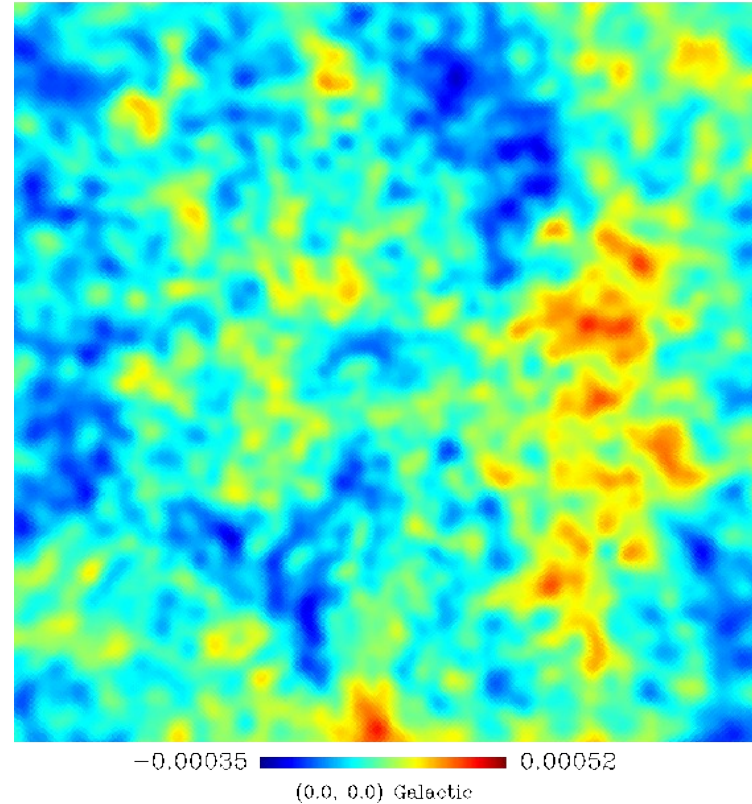
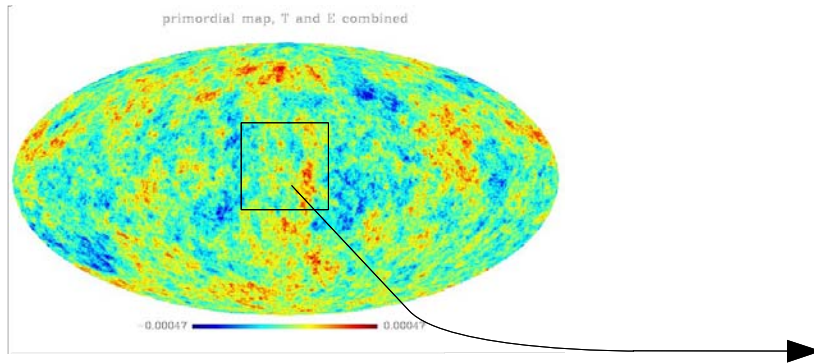
Yadav, and Wandelt, PRD (2005)



Yadav, and Wandelt, PRD (2005)

Curvature perturbations at different r

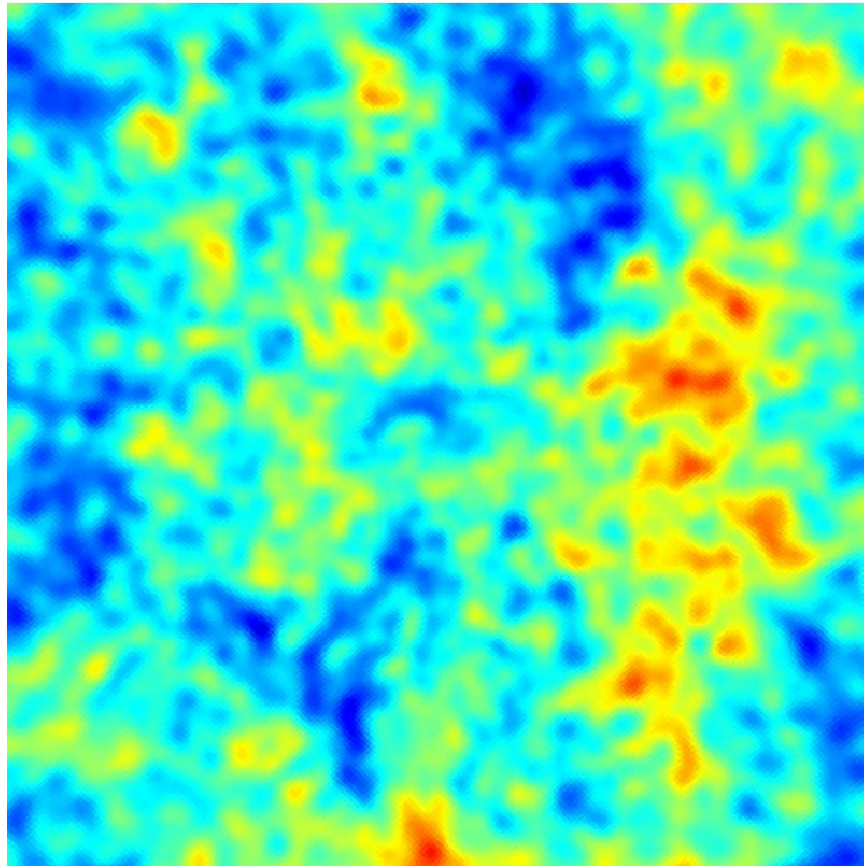
Curvature perturbations




Yadav, and Wandelt, PRD (2005)

Tomographic reconstruction of inflationary curvature perturbations from CMB temperature and polarization.

Curvature perturbations



-0.00035  0.00052
(0.0, 0.0) Galactic

One can invert the linear radiative transport generating the primordial curvature perturbations .

They contain all the information about the initial scalar seed perturbations in the CMB T&E.

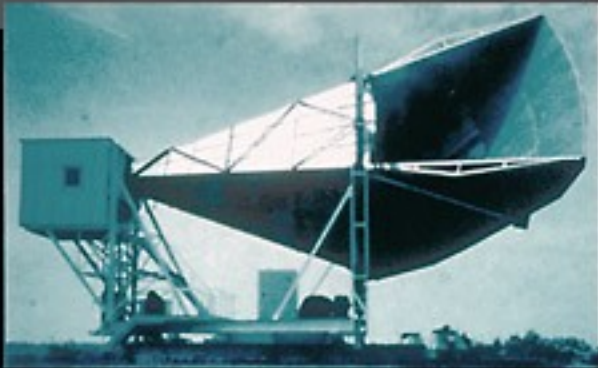
Yadav and Wandelt 2006

Observational Status and Prospects for the CMB

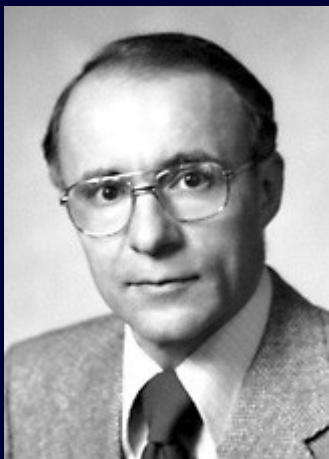
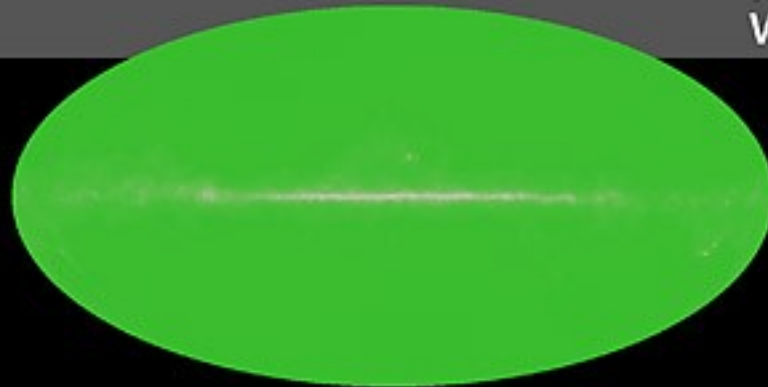
A major international effort is under way to make high quality observations of the microwave sky using ground-based, balloon borne and space missions.

Observing the CMB

1965



Penzias and
Wilson

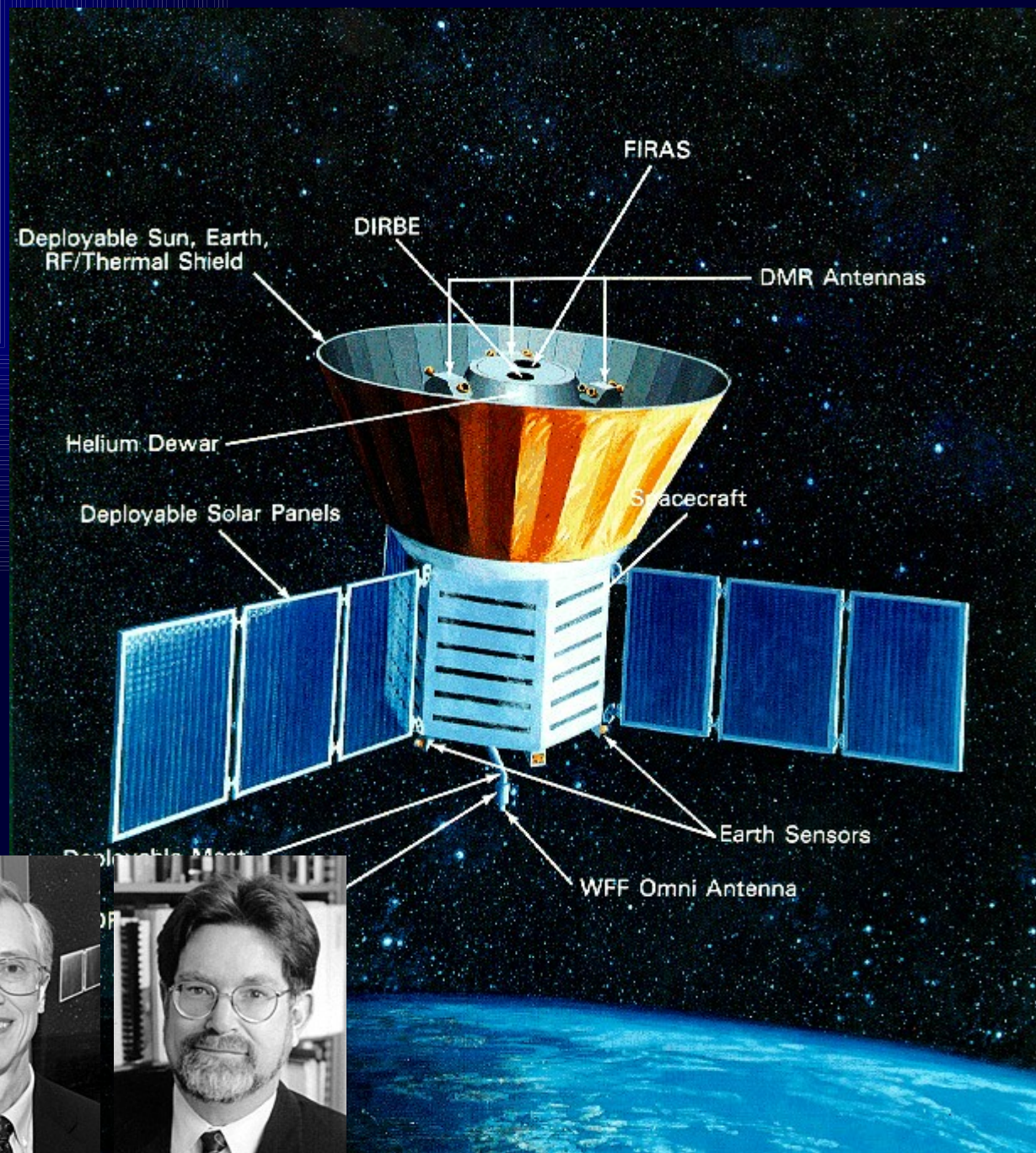


Penzias and Wilson, Nobel Prize Physics 1978

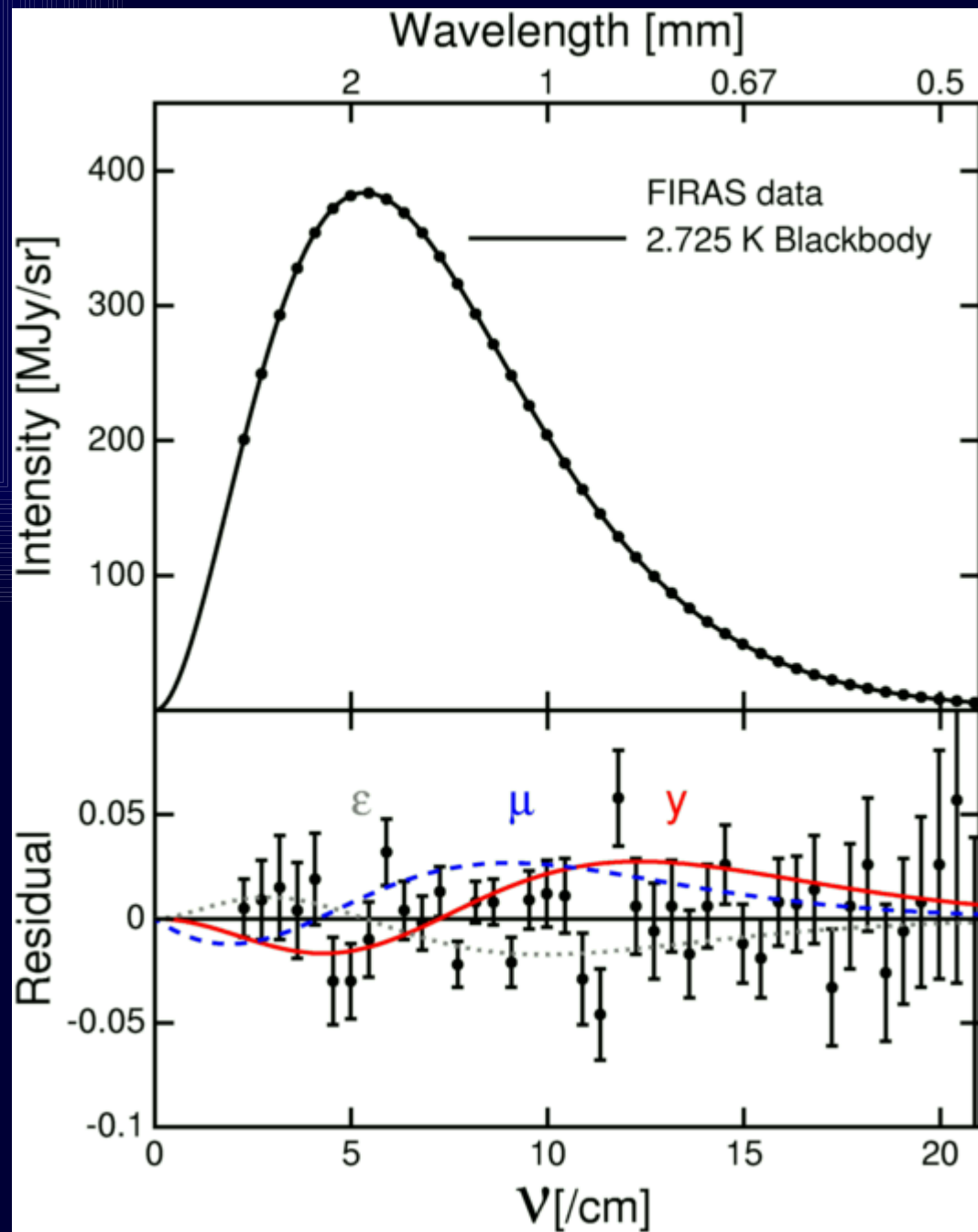
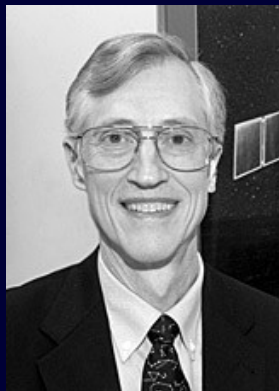
1990's: COBE- DMR

The discovery
of primordial
fluctuations and
the blackbody
nature of the
CMB

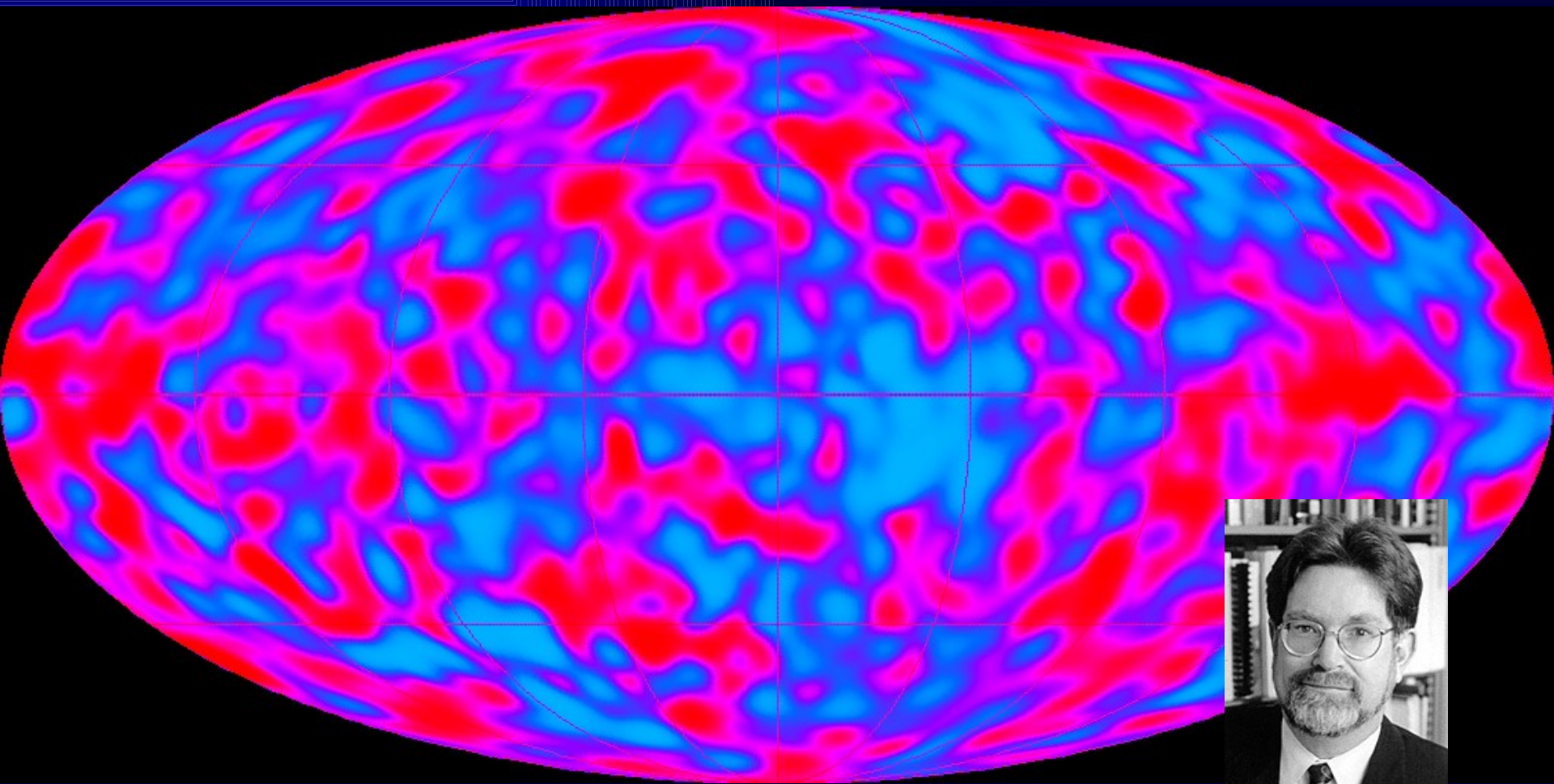
Nobel Prize
Physics 2006:
Mather and
Smoot



The cosmic microwave background is blackbody radiation



CMB *anisotropies* as observed by COBE-DMR



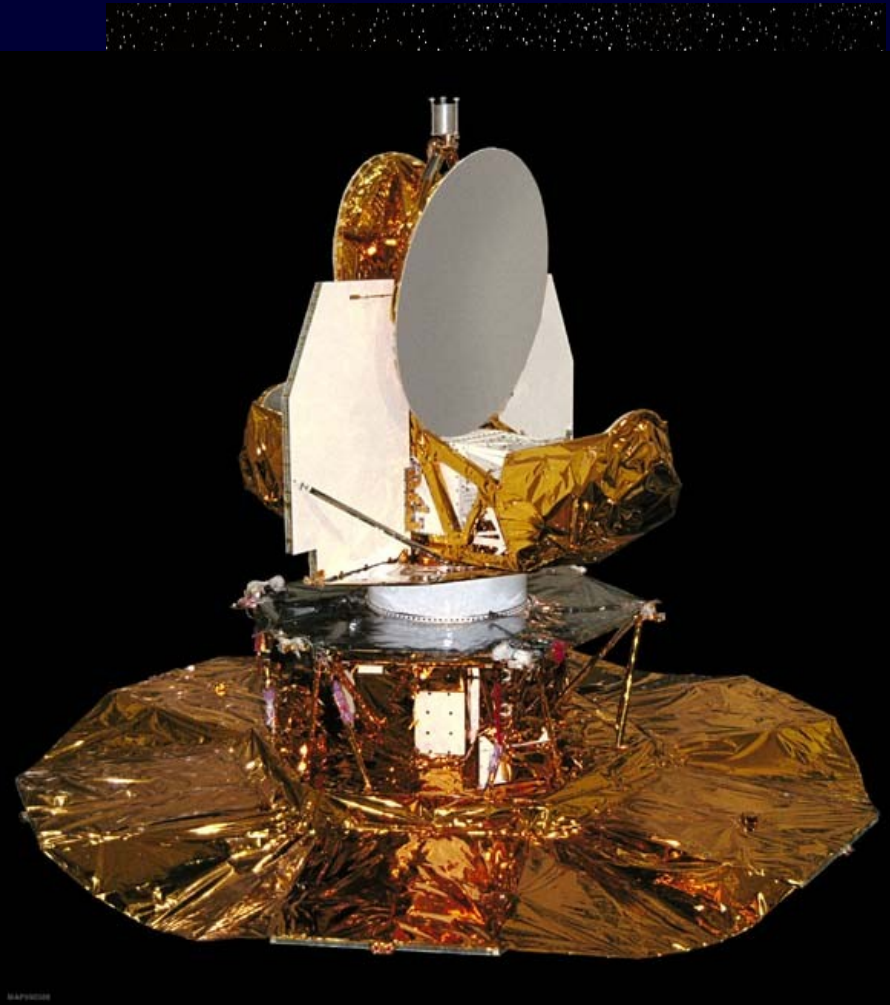
The Wilkinson Microwave Anisotropy Probe

NASA MIDEX mission

Currently in Operation

- Reached observing location (L2) in 2001
- YR1 data released in early 2003
- YR3 data released in 2006
- YR5 data released in 2008

Harbinger of precision cosmology

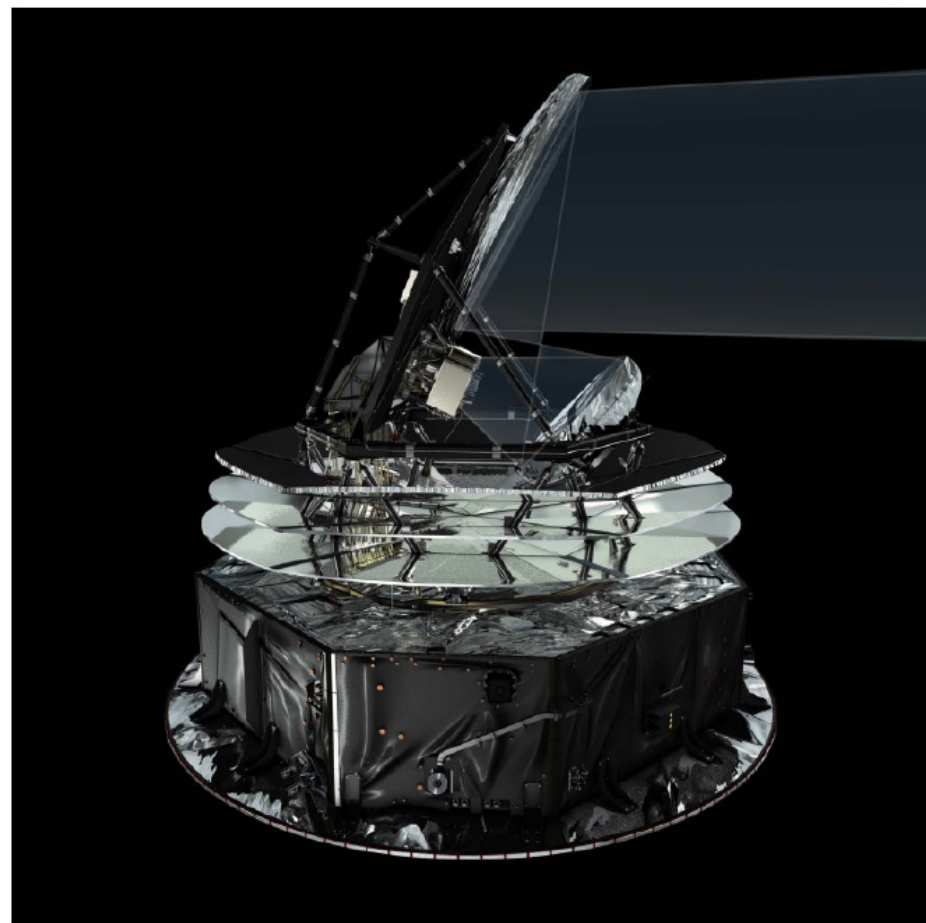




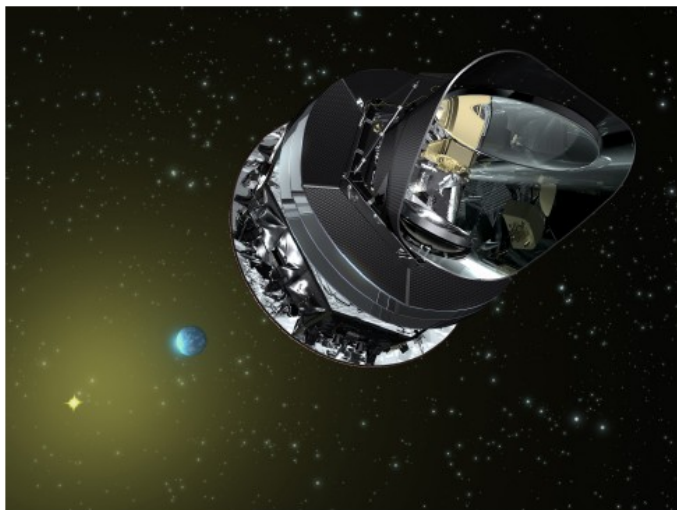
The Planck mission



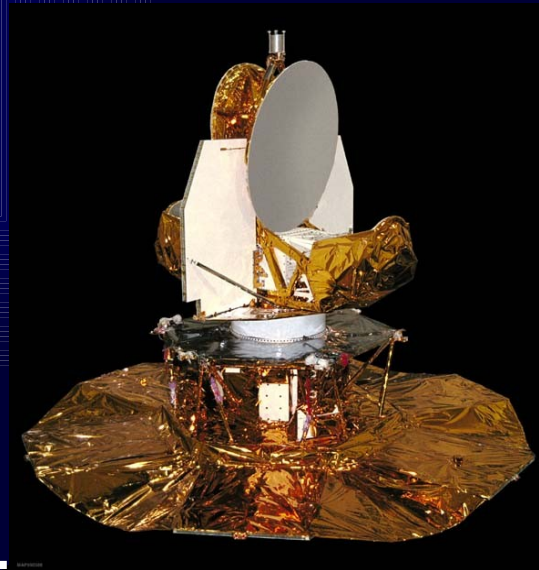
- Planck is a major joint ESA/NASA mission to **L2**.
- Principal scientific goal:
 - to make definitive all-sky maps of CMB temperature anisotropy down to 5' resolution.
- Two instruments:
 - Low Frequency Instrument (PI: Reno Mandolesi)
 - High Frequency Instrument (PI: Jean-Loup Puget)
- Temperature measurement at 9 frequencies
 - 30, 44, 70, 100, 143, 217, 353, 545, 857 GHz
- Polarization measurement at 7 frequencies
 - 30, 44, 70, 100, 143, 217, 353 GHz
- Detailed Planck Science Case in the “Blue Book:”



- Planck launch date: May 14, 2009.
- Dual launch with Herschel on an Ariane 5 rocket
- Then cruise to L2



So where do we stand?



What do we find when we analyze the WMAP, suborbital CMB, and other astronomical data? And what can we expect from Planck?

We now have a Standard Model of Cosmology!

- Bad news for theorists:

We now know the basic global properties of the Universe.

- Good news for theorists:

We don't understand most of the constituents of the Universe.

We don't know how it began

Observer's recipe for Universe pie



One delicious universe:

3 cups dark energy
1 cup dark matter
a pinch of baryonic matter for flavor

microwave at 2.7 K

Razzle Dazzle Recipes

Theorist's recipe for Universe pie



One inflationary universe:
Use recipe below to make 4-D effective field theory.

Start with smooth patch + GR.

Let the field with the largest potential energy inflate patch while cooling. Reheat.

OR: set up parallel
colliding branes. OR...

One 4-D effective theory:

Strings? 10 to 11 space-time dimensions.

Compactify to 4 or 5 "large" dimensions, to taste.

How many branes in the Calabi-Yau? Where?

What causes inflation? Find effective 4-D description...

Theorist's recipe for Universe pie

Dark matter recipes:

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Theorist's recipe for Universe pie

Dark energy recipes:

Dark matter recipes:

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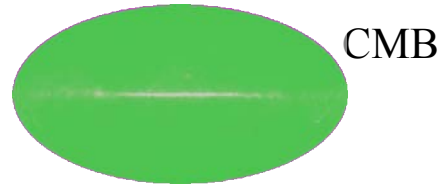
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colliding branes. OR...

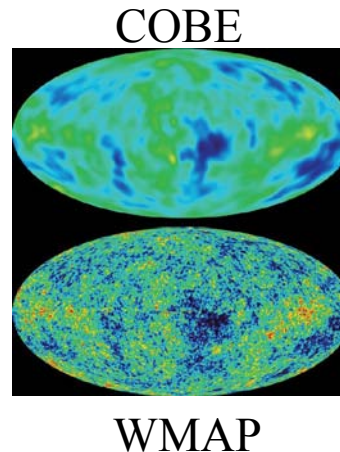
The Physics of the Beginning

- Why Homogeneity and Isotropy?



- Why Flatness?

- Whence the seed perturbations?



1978 Nobel Prize
in Physics



Robert Wilson and Arno Penzias



2006 Nobel Prize
in Physics

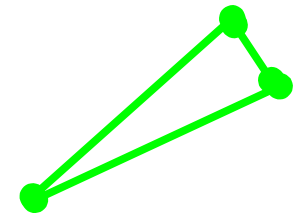


George Smoot John C. Mather
Paris, March 19, 2010

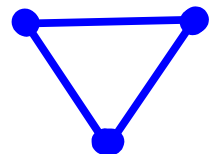
The CMB and the Beginning

Test	Std. Inflation	Ekpyrosis	Obs
• Is observable universe flat?	• Yes.	• Built in.	• Yes, to ~2%
• Do the fluctuations have the predicted correlations (nearly scale independent)?	• Yes.	• Yes.	• Yes, to few %
• Are fluctuation adiabatic?	• Yes.	• ?	• Yes, to ~10%
• primordial gravitational waves	• Maybe	• No	• ?
• Are fluctuations nearly Gaussian?	• Yes: predicted to be true at 0.001%!	• Much higher deviations from Gaussianity	• ~2σ hints of deviation from Gaussianity from WMAP data

Primordial perturbations and Gaussianity



- Slow-roll \rightarrow shallow potential \rightarrow nearly free field; has Gaussian quantum perturbations (field modes in S.H.O. potential). Theorem for single field.
- If multi-field (or ekpyrosis), can have isocurvature perturbations convert into non-Gaussian curvature pert. outside horizon \rightarrow local bispectrum
- Non-standard kinetic term: can inflate in spite of steep potential \rightarrow equilateral bispectrum
- Vacuum state – can get flattened triangle contributions if not Bunch-Davies.



Non-Gaussianity – a new frontier

- In addition to the information to be gained from 2-point correlations, non-Gaussianity opens a new and much richer window on the Physics of the Beginning
- What is the research program?
 - Reliable theoretical prediction of non-Gaussianity from models of the early Universe
 - Characterization of non-Gaussian confusion effects
 - Development of efficient and practical statistical methods to draw inferences about non-Gaussianity from the data.

f_{NL} – a specific parameterization of non-Gaussianity

$$\Phi(x) = \Phi_G(x) + f_{NL} \Phi_G^2(x)$$

Salopek & Bond 1990
Komatsu & Spergel 2001

Characterizes the amplitude of non-Gaussianity

- This non-Gaussianity creates a bispectrum signature (as well as higher order moments)

$$\langle \Phi(k_1) \Phi(k_2) \Phi(k_3) \rangle = 2(2\pi)^3 f_{NL} \delta(k_1 + k_2 + k_3) P(k_1) P(k_2),$$

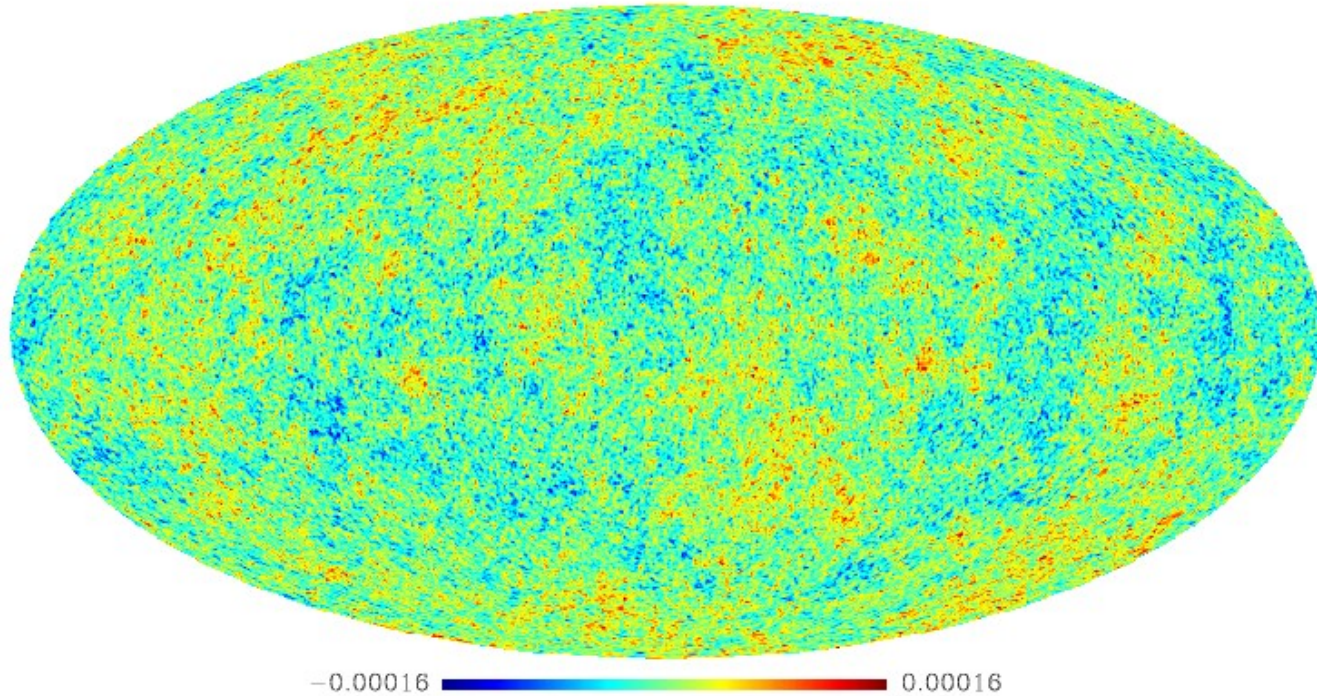
where $(2\pi)^3 \delta(k_1 + k_2) P(k_1) = \langle \Phi(k_1) \Phi(k_2) \rangle$

- This translates into a bispectrum signature in the CMB through

$$a_{lm} = 4\pi(-i)^l \int \frac{d^3\mathbf{k}}{(2\pi)^3} \Phi(\mathbf{k}) g_{Tl}(k) Y_{lm}^*(\hat{\mathbf{k}})$$

$$f_{NL} = 0$$

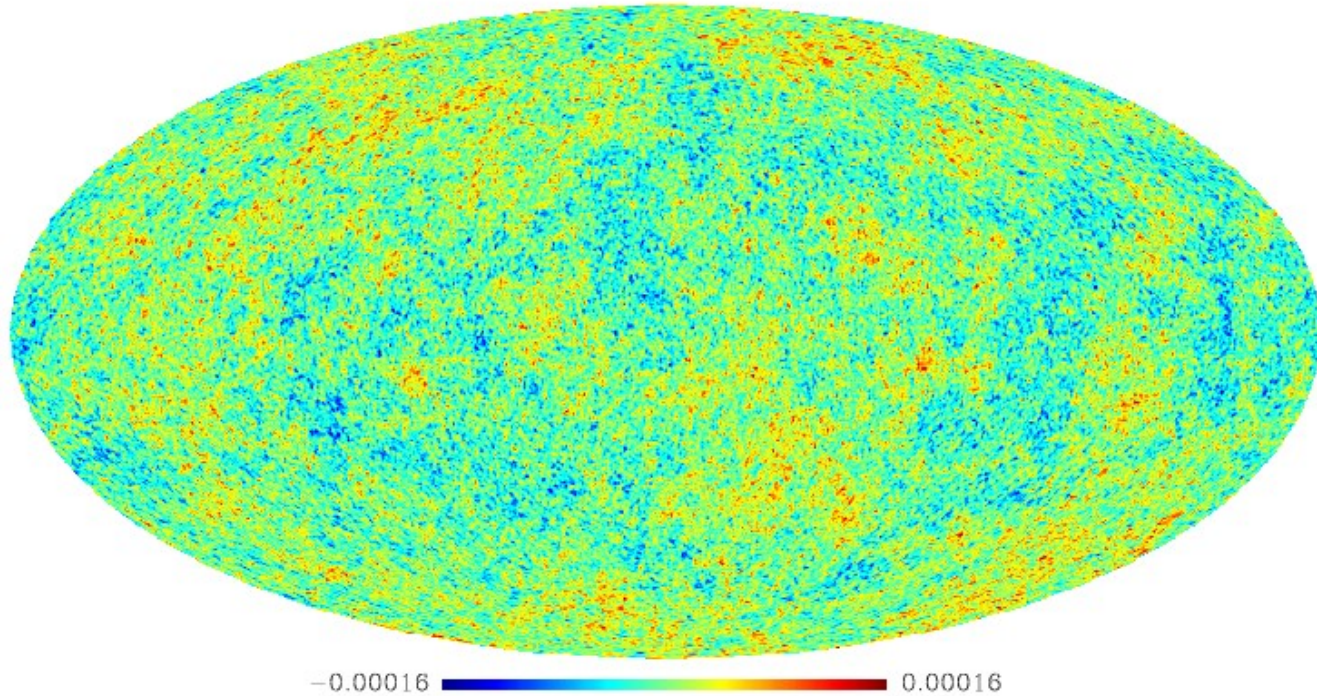
Temperature ($f_{NL} = 0$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^1$$

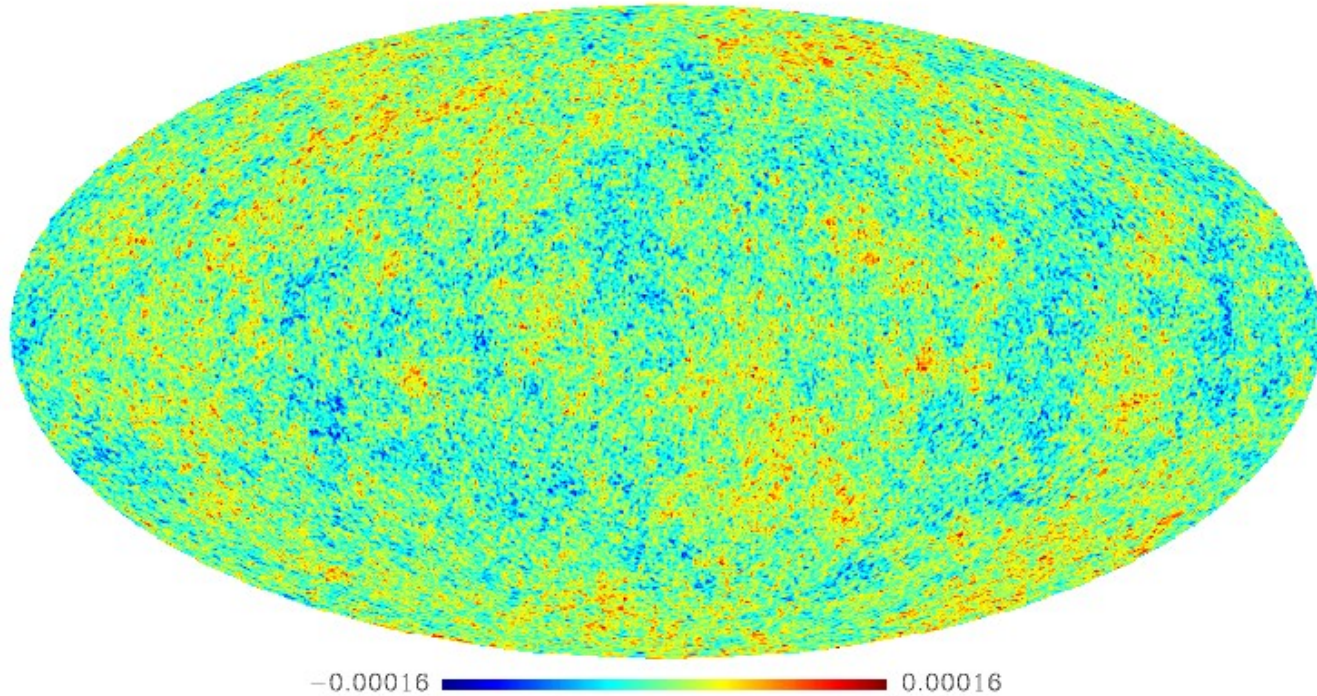
Temperature ($f_{NL} = 10$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^2$$

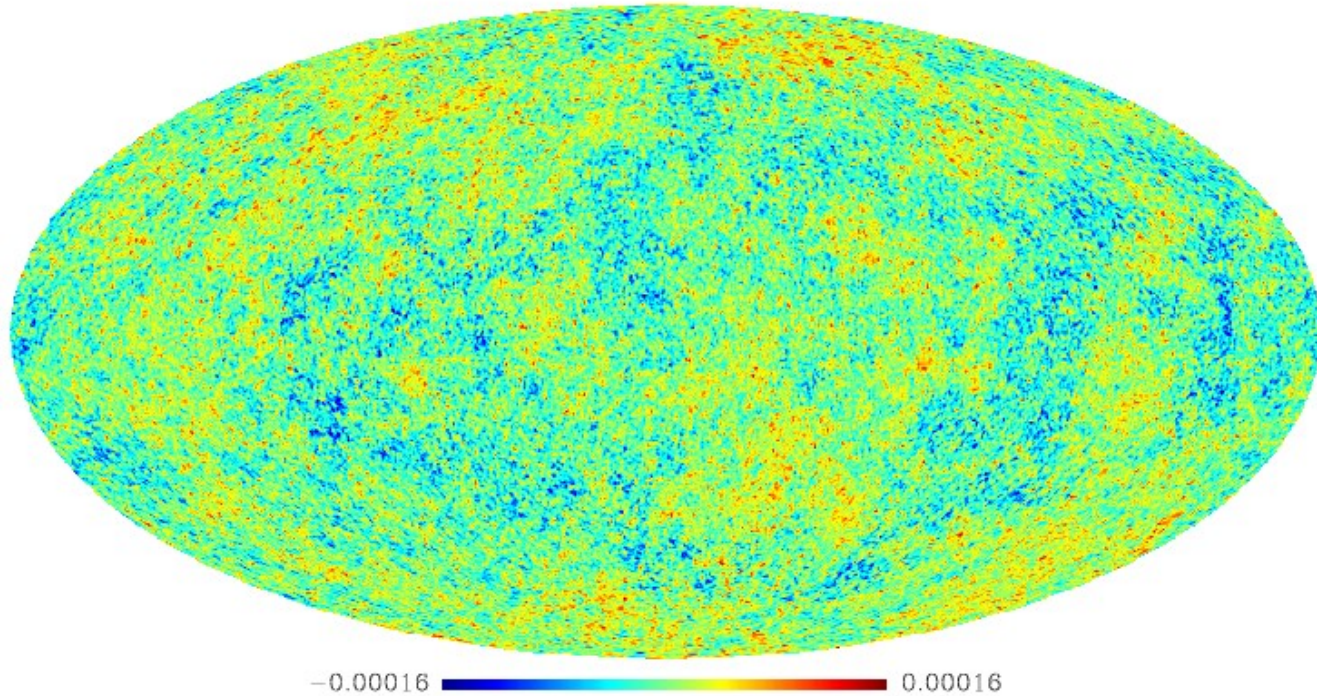
Temperature ($f_{NL} = 10^2$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^3$$

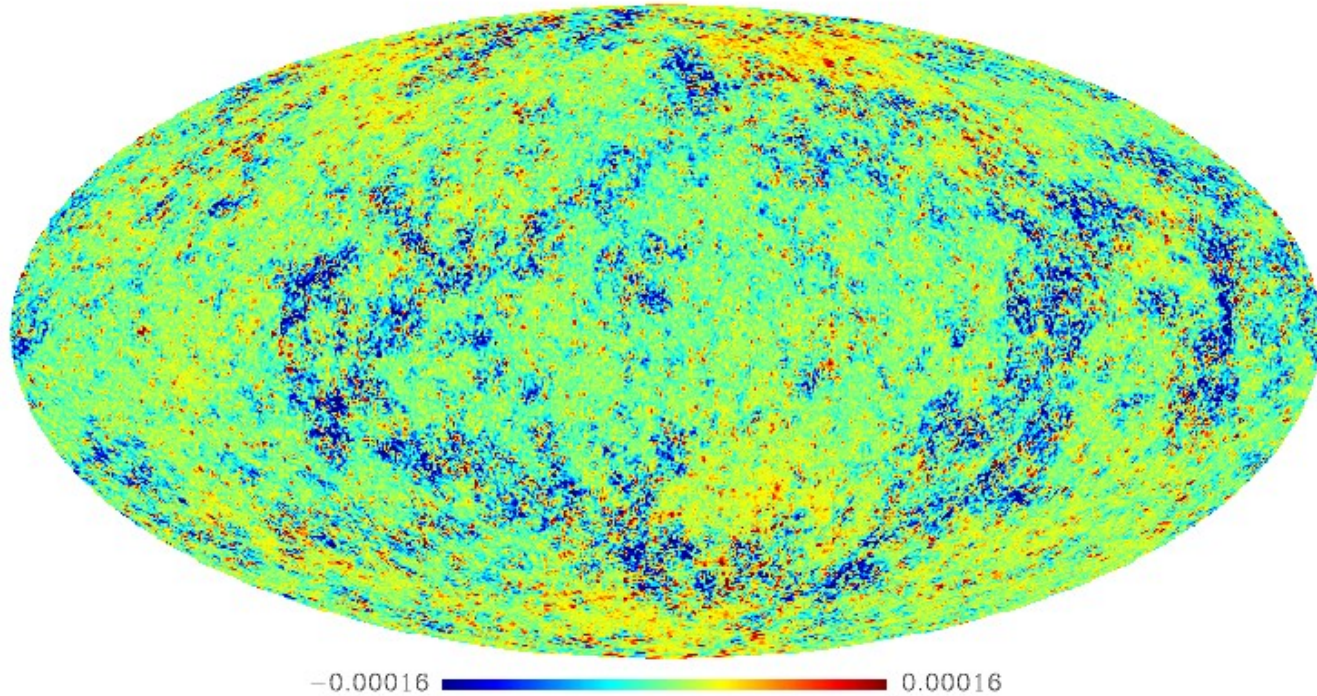
Temperature ($f_{NL} = 10^3$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^4$$

Temperature ($f_{NL} = 10^4$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

Estimating non-Gaussianity

Fast Cubic Statistic:

$$\hat{S}_{prim} = \frac{1}{f_{sky}} \int r^2 dr \int d^2\hat{n} B(\hat{n}, r) B(\hat{n}, r) A(\hat{n}, r) \quad \text{Komatsu, Spergel and Wandelt 2005}$$

$$B(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{lm}^i \beta_\ell^p(r) Y_{lm}(\hat{n})$$

B(r) is a map of reconstructed primordial perturbations

$$A(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{lm}^i \alpha_\ell^p(r) Y_{lm}(\hat{n}).$$

A(r) picks out relevant configurations of the bispectrum

S_{prim} combines all bispectrum configurations nearly optimally for “local” primordial non-Gaussianity f_{NL} while avoiding brute force computation of the bispectrum.

f_{NL} phenomenology from the CMB bispectrum

Komatsu & Spergel 2001 – CMB bispectrum from f_{NL}

Verde et al. 2002

Komatsu, Wandelt, Spergel, Banday, Gorski 2001 – f_{NL} from COBE

Komatsu Spergel & Wandelt 2003 – fast f_{NL} estimator

Komatsu et al (WMAP team) 2003 – WMAP1 analysis using KSW

Babich and Zaldarriaga 2004 – temperature + polarization

Creminelli, Nicolis, Senatore, Tegmark, Zaldarriaga 2006 – introduce linear term to improve KSW estimator

Spergel et al (WMAP team) 2006 – WMAP3 analysis using KSW

Creminelli, Senatore, Tegmark, Zaldarriaga 2006 – apply cubic + linear term to WMAP3 data

Yadav & Wandelt 2005 – tomography of the curvature perturbations

Yadav Komatsu & Wandelt 2007 – KSW generalized to T+P

Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007 – calibrate YKW estimator against non-Gaussian simulations

Yadav, Komatsu, Wandelt, Liguori, Hansen, Matarrese 2007 – Creminelli et al. corrected and generalized to T+P

Yadav & Wandelt 2007 – application of YKWLHM07 to WMAP3

Komatsu et al 2008 – application of YKWLHM07 to WMAP5

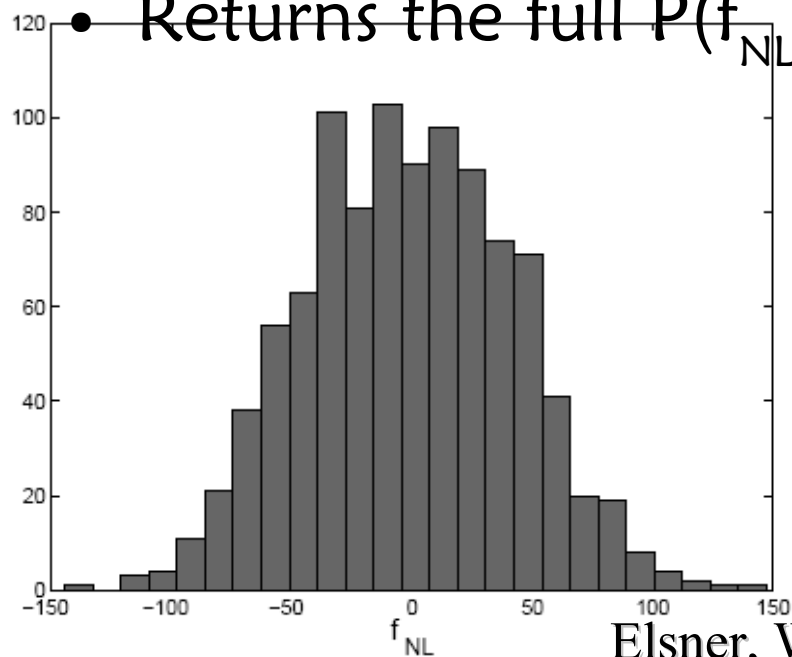
Smith, Senatore, Zaldarriaga 2009 – least squares bispectrum estimator, WMAP5

[...]

Fully Bayesian non-Gaussianity analysis

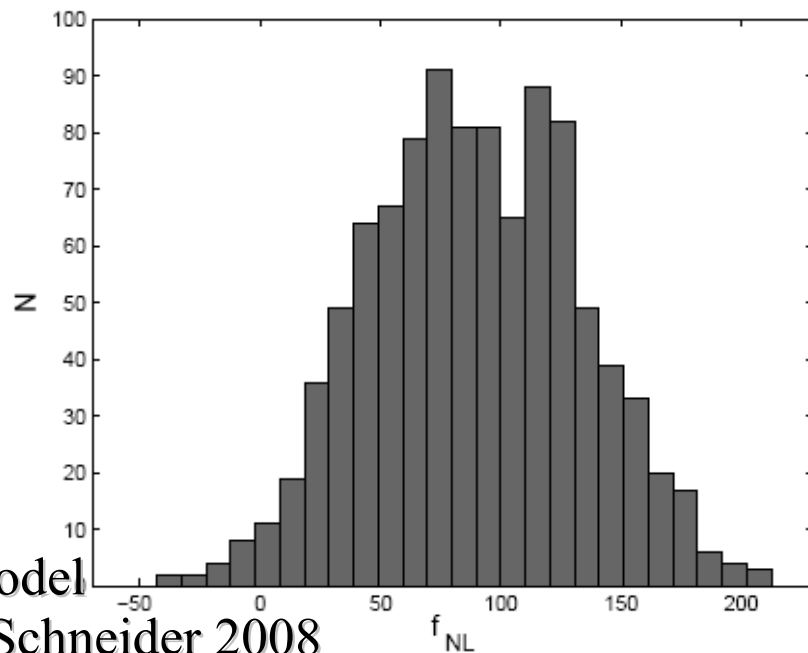
- Instead of going via the bispectrum, build full statistical model of the data, including general local non-Gaussianity, (including cubic perturbation predicted by ekpyrotic model) and a detailed model of the observations

- Returns the full $P(f_{NL} | \text{data})$

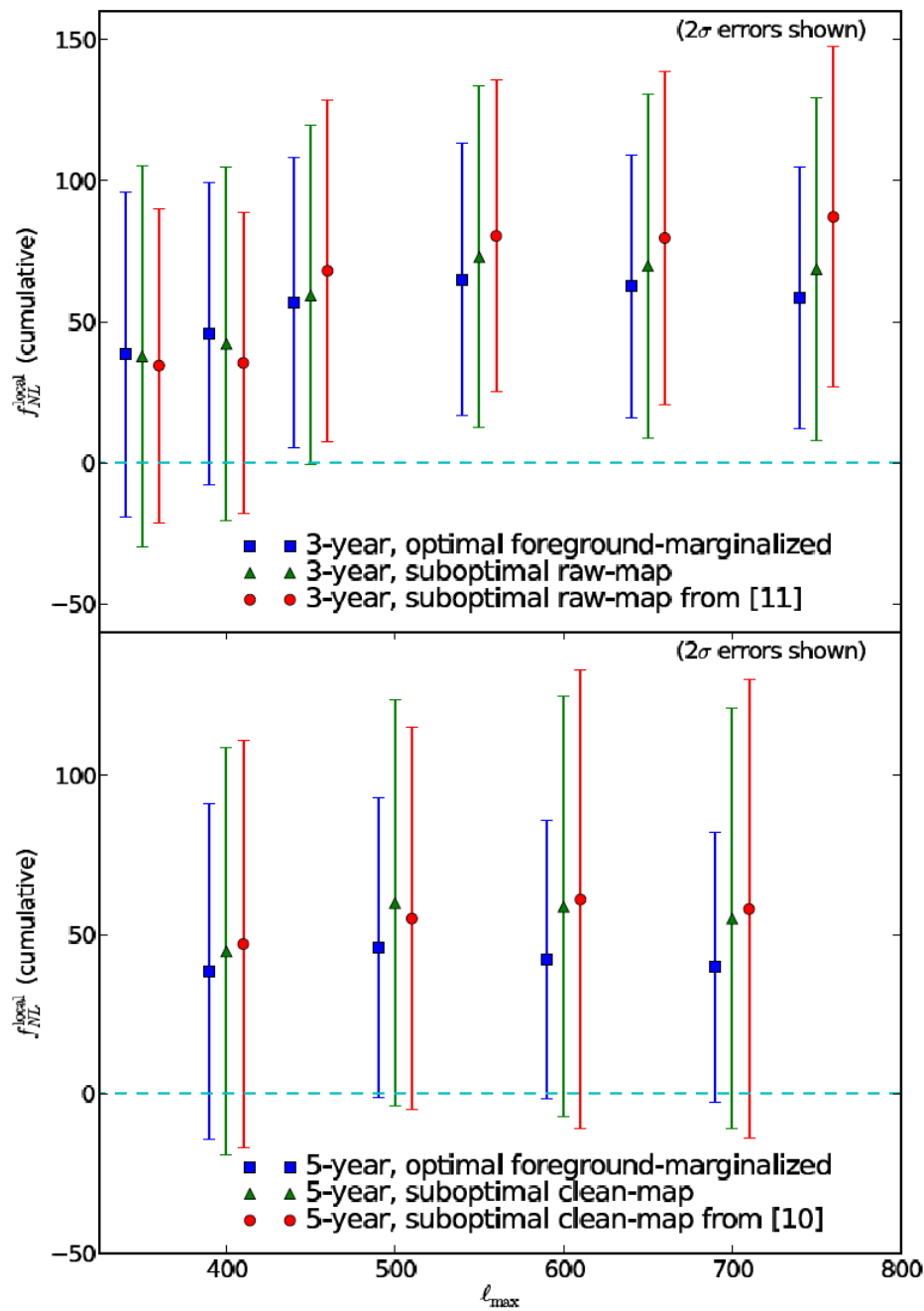


Elsner, Wandelt, Schneider 2008

Toy model



f_{NL}



- Overview of current observational status

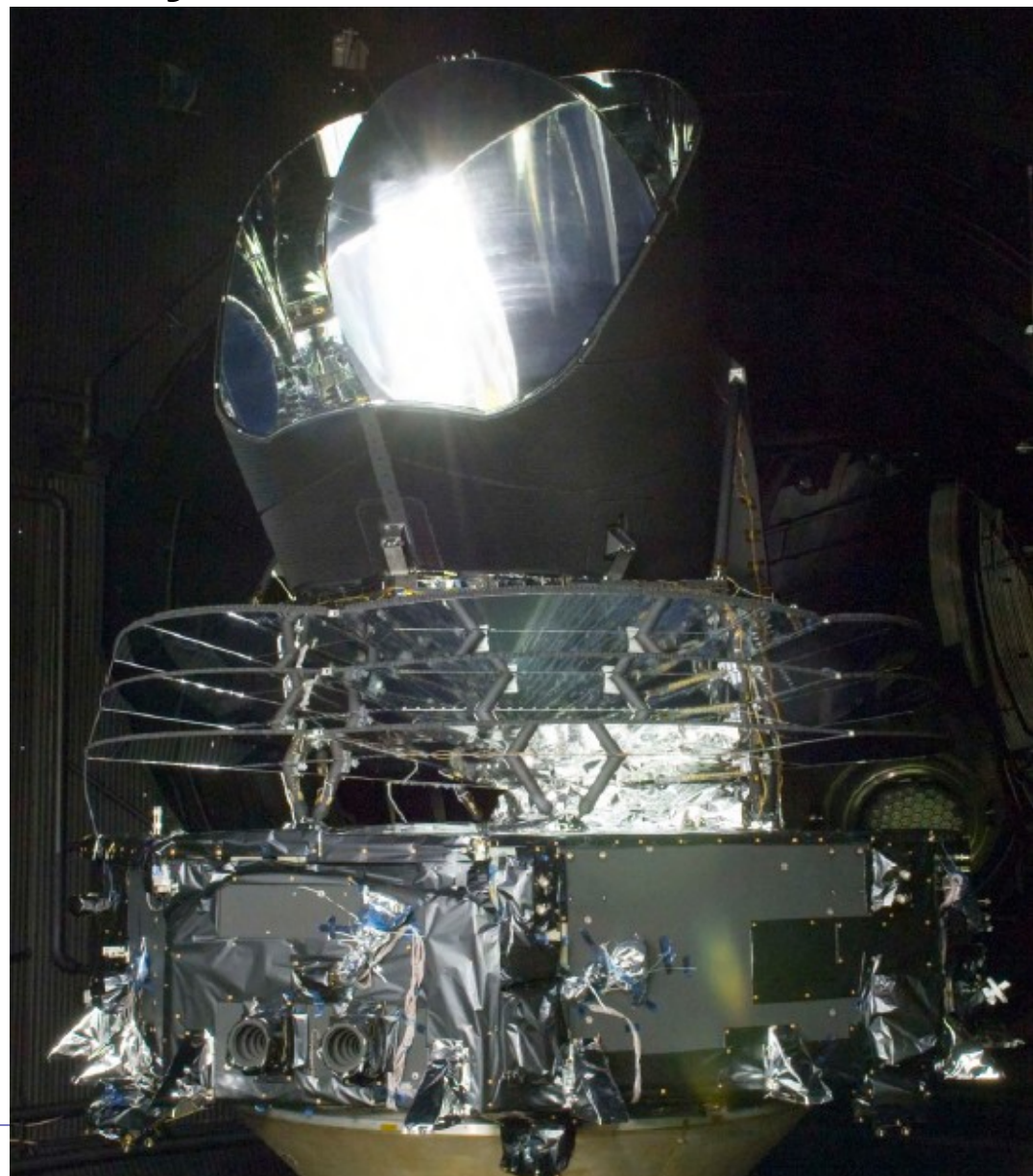
Non-Gaussianity and Planck

- Non-Gaussianity with Planck will be a new window on the early Universe, complementary to the wealth of information in the two-point function.
- Different early Universe models have distinct predictions for the type and amount of non-Gaussianity expected.
- Ekpyrotic/Cyclic models generically predict non-Gaussianity at detectable levels for Planck $-50 < f_{\text{NL}} < 200$ (Leners&Steinhardt 2008)
- New ekpyrotic models are already being hit by current constraints.
- The search for non-Gaussianity is complementary to the search for primordial gravitational waves
 - Primordial B-modes are the “smoking gun” of inflation
 - Finding primordial non-Gaussianity would rule out all single-field models of slow-roll inflation
- Planck will improve WMAP f_{NL} error bars by a factor 4.

Non-Gaussianity and Planck

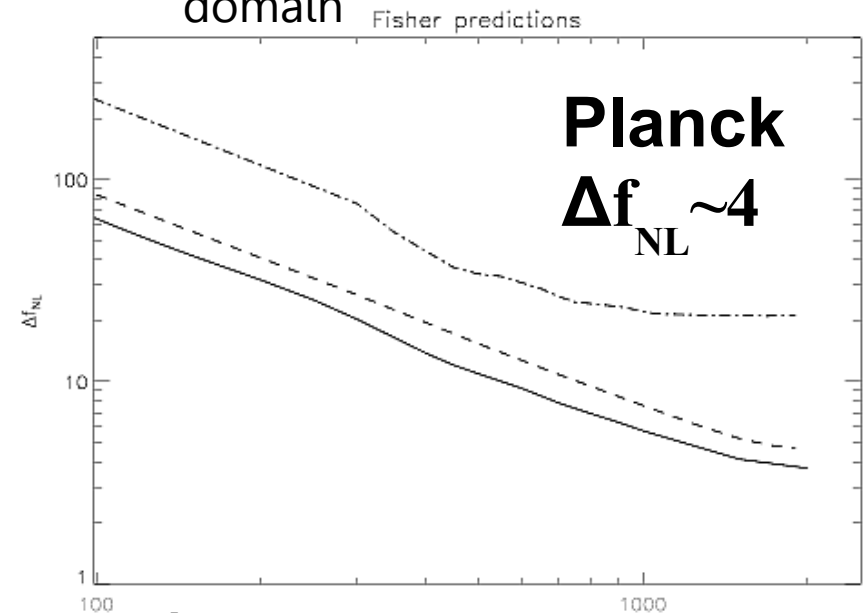
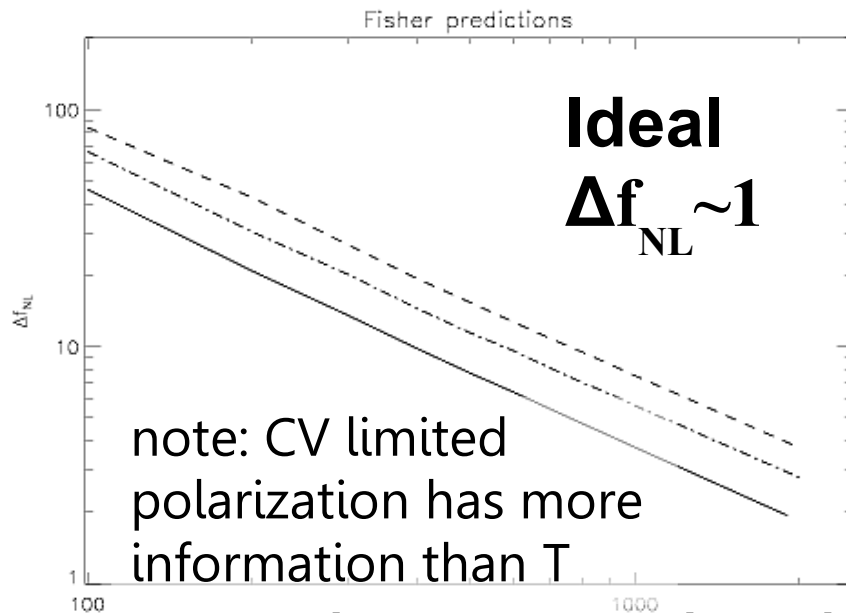
One of the lasting impacts of Yadav and Wandelt 2008: search for primordial NG using bispectrum templates is *much more robust* to systematic error than was previously realized.

- Even though non-Gaussianity is small, the radiation transfer functions give the bispectrum of primordial non-Gaussianity a very different signature from late time secondary effects, foregrounds, or non-Gaussian instrument systematics
- Temperature and Polarization are complementary and can give independent and combined constraints.
- Expect that this robustness will enable the study of primordial non-Gaussianity with Planck.



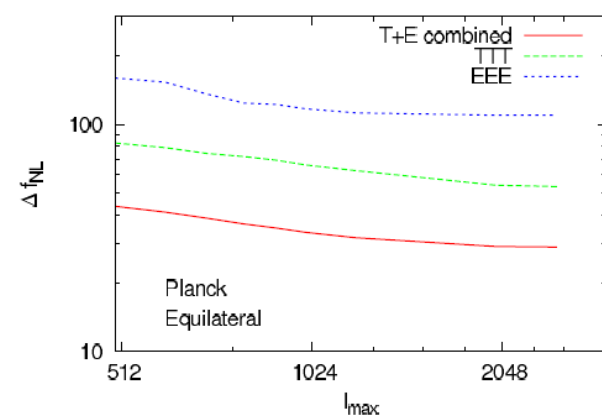
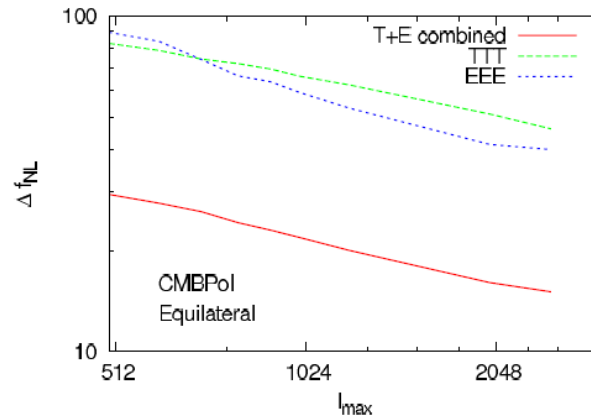
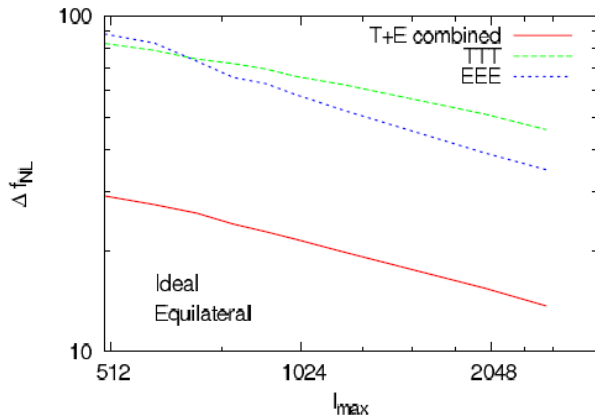
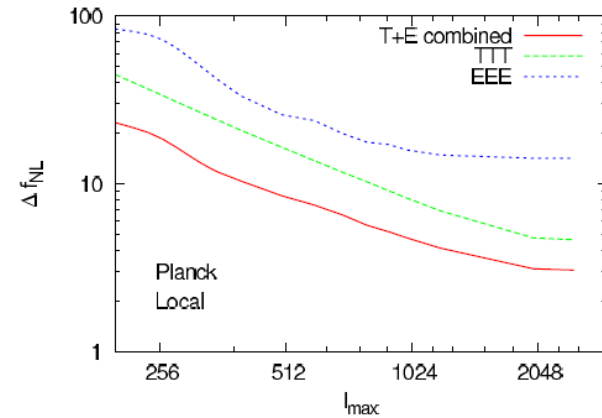
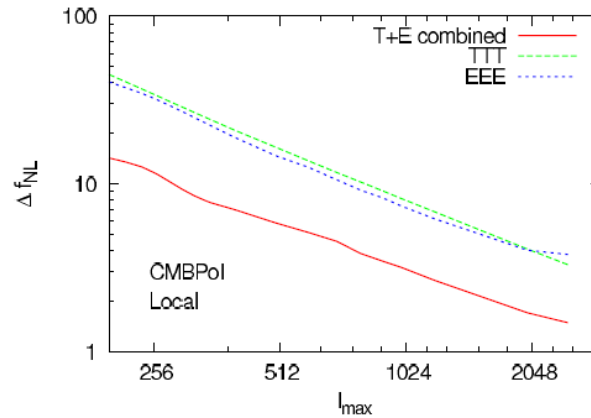
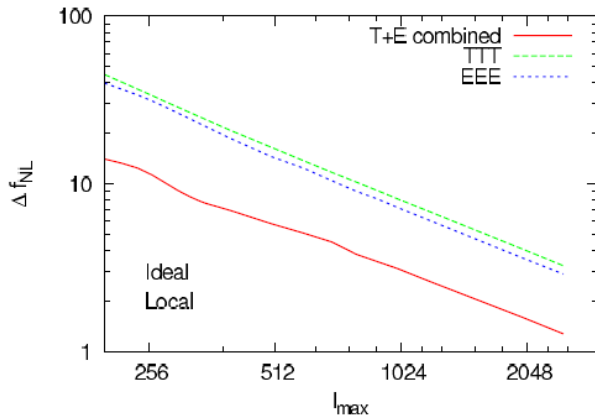
Planck's promise for Non-Gaussianity

- Many modes
 - large sky coverage
 - high resolution
- Frequency coverage
 - foreground removal
- Polarization
 - complementary to T
 - adds a great deal of information
- Multiple sky coverages
 - control of systematics in time-domain



Yadav, Komatsu and Wandelt, astro-ph/0701921, ApJ (2007)

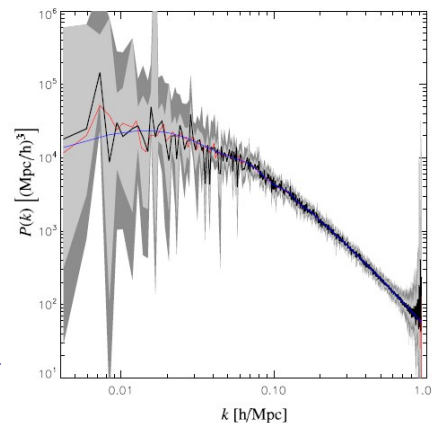
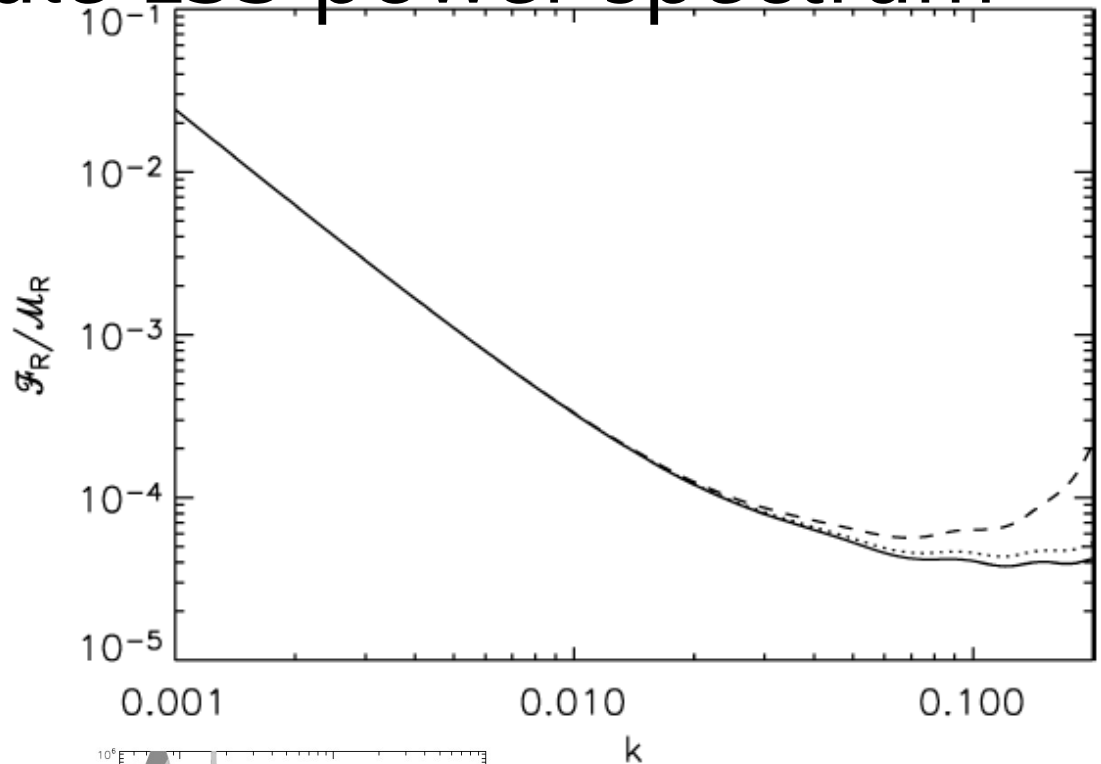
The future



$\Delta f_{NL} \sim 1$ is within reach!

Fully independent probe of local NG from large scale LSS power spectrum

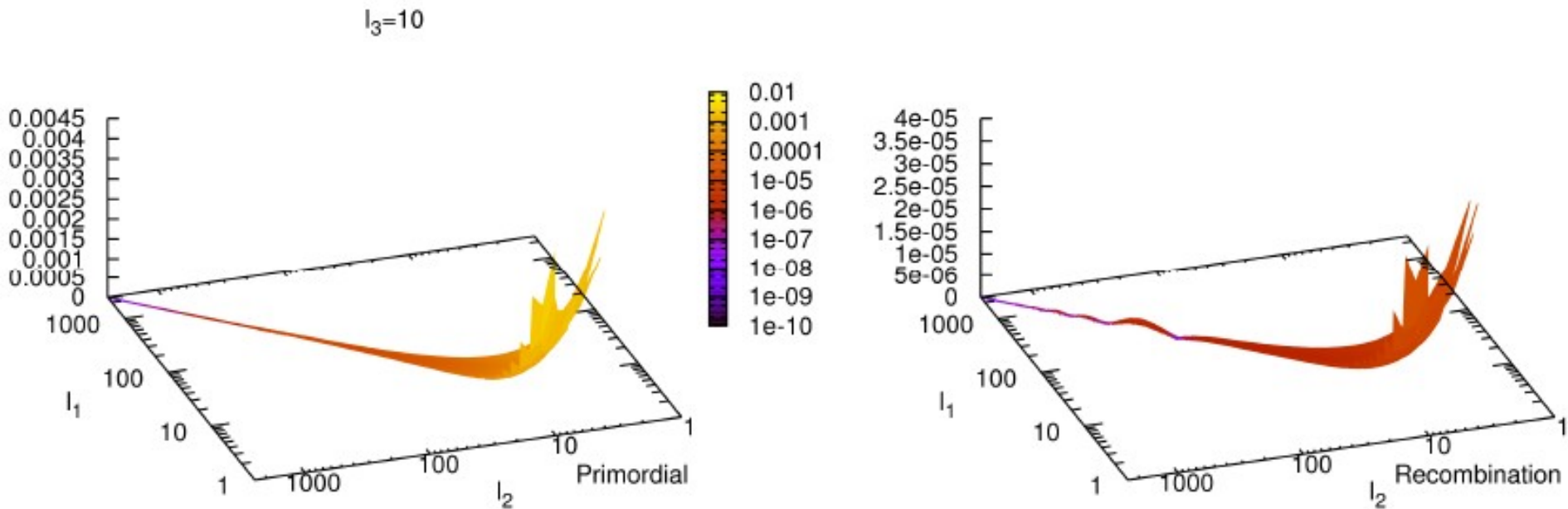
- local non-linear transformation of the potential leaves imprint on large scale correlations of collapsed structures (Dalal et al. 2008, Verde&Matarrese 2008, Slosar et al 2008)
- promises $\Delta f_{\text{NL}} \sim 1$ with future very large scale redshift surveys
- requires very careful power spectrum analysis (Jasche, Kitaura Wandelt Ensslin 2009)



Non-Gaussianity due to “crinkles” in the surface of last scattering

- The electron density is not homogeneous – recombination occurs at slightly different times in different places
 - **crinkles in the surface of last scattering**
- Perturbations in the free electron density (ionization fraction) can be larger than perturbations in the baryon density by a factor of 5 (Novosyadlyj, MNRAS 2006; Senatore, Tassev, Zaldarriaga arxiv:0812.3652).
- Does this produce non-Gaussianity observable by Planck?

Crinkles vs. primordial non-Gaussianity give similar but not identical bispectrum

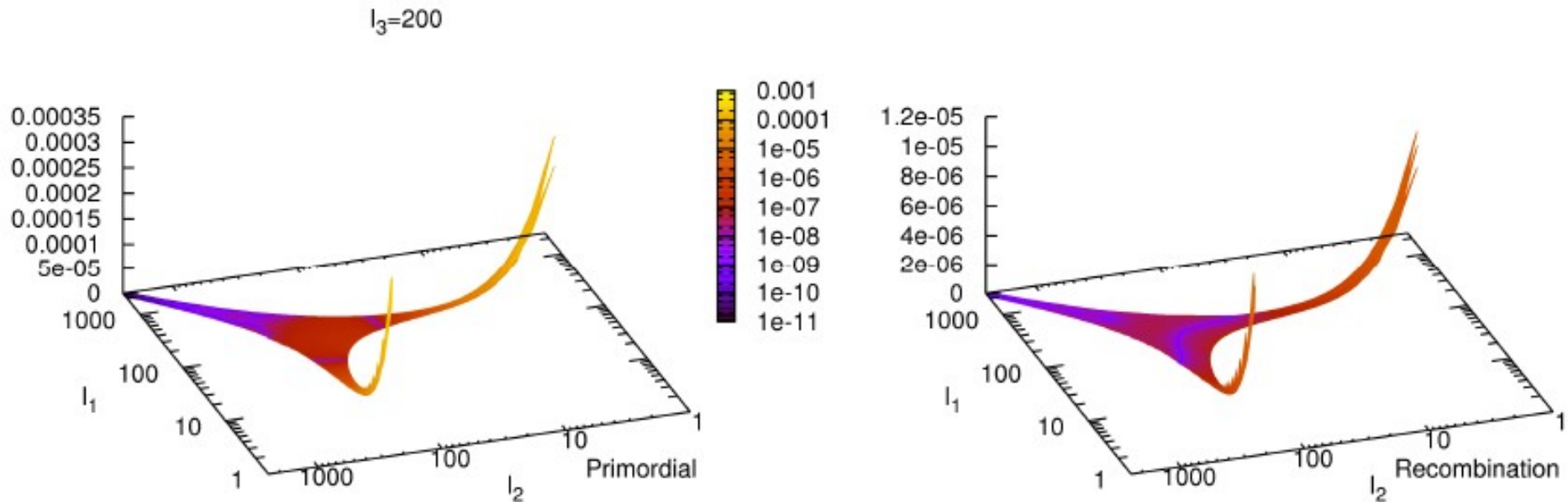


Khatri & Wandelt, PRD 2008

Khatri & Wandelt, arxiv:0903.0871

58

Crinkles vs. primordial non-Gaussianity give similar but not identical bispectrum

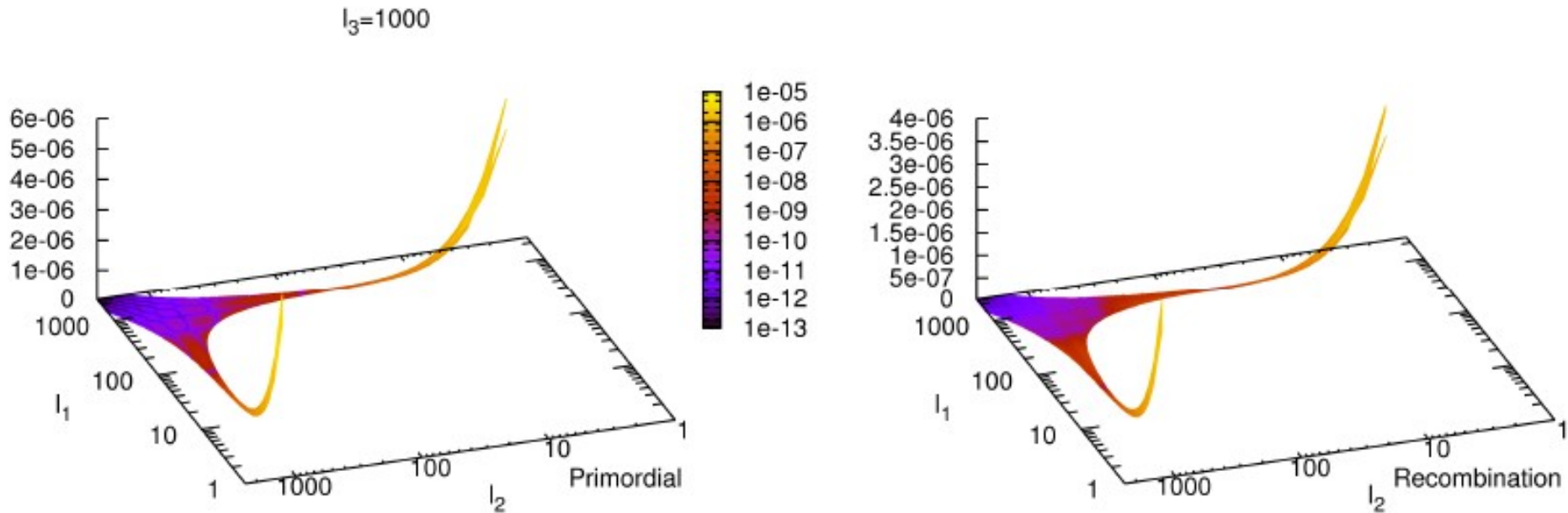


Khatri & Wandelt, PRD 2008

Khatri & Wandelt, arxiv:0903.0871

59

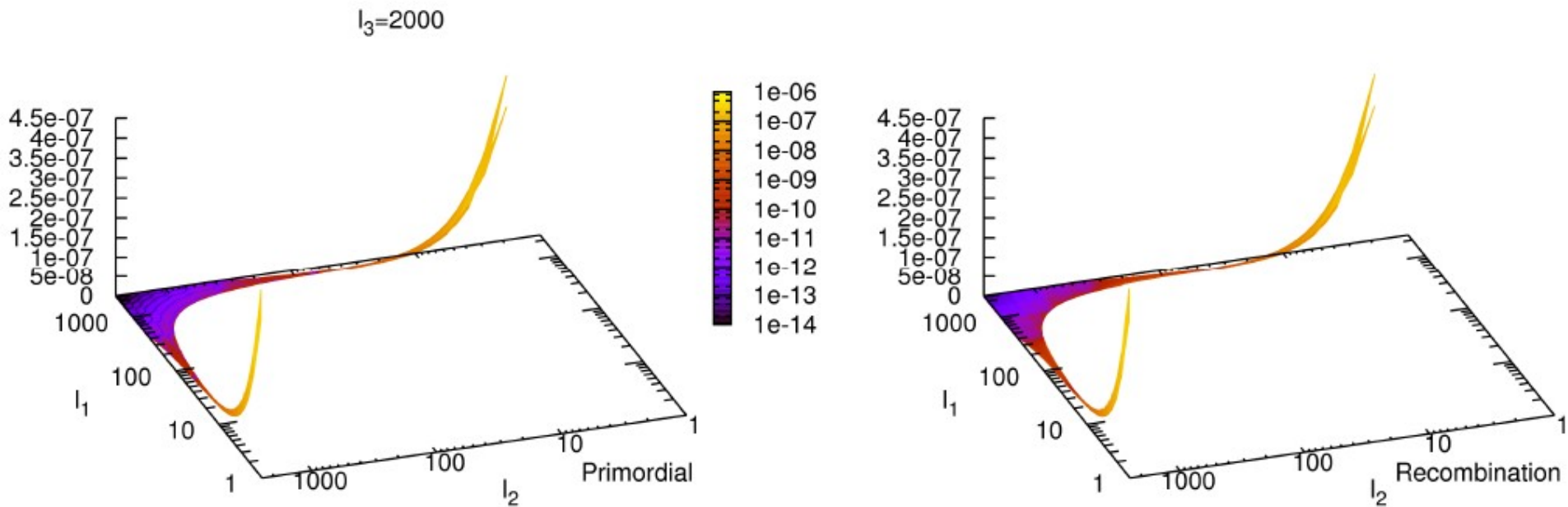
Crinkles vs. primordial non-Gaussianity give similar but not identical bispectrum



Khatri & Wandelt, PRD 2008

Khatri & Wandelt, arxiv:0903.0871

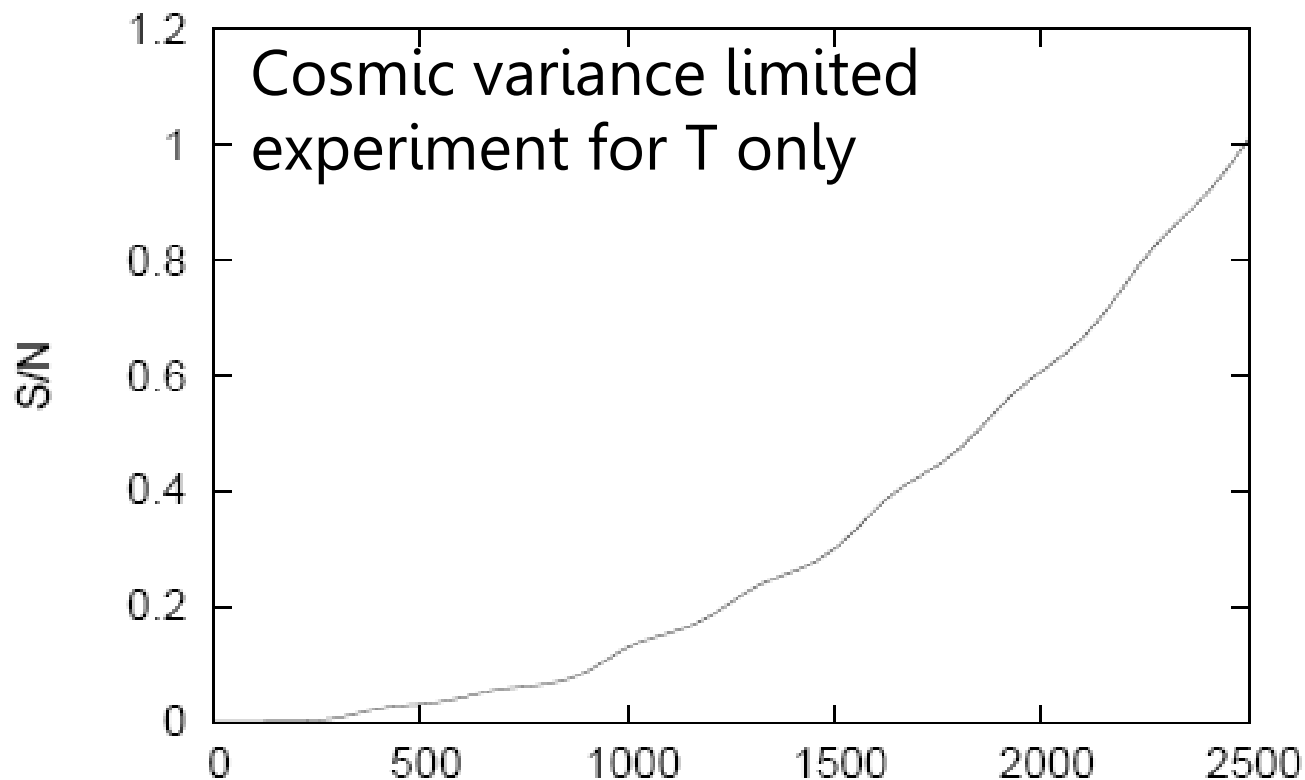
Crinkles vs. primordial non-Gaussianity give similar but not identical bispectrum



Khatri & Wandelt, PRD 2008

Khatri & Wandelt, arxiv:0903.0871

Can we see non-Gaussianity from Crinkles?

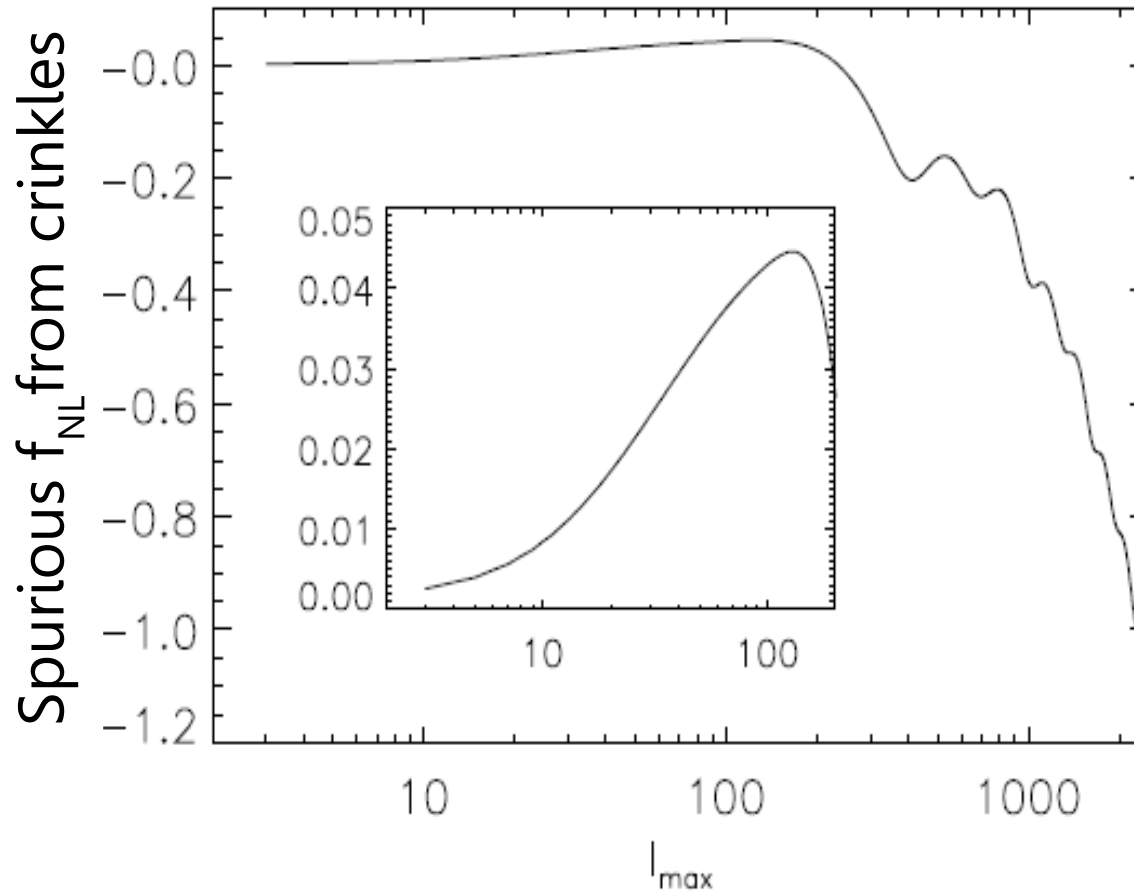


Khatri & Wandelt, PRD 2008

Senatore, Tassev, Zaldarriaga: arXiv:0812.3652/8

Khatri & Wandelt, arxiv:0903.0871

Are crinkles an important “background” for primordial f_{NL} ?



At the level of $f_{NL} \sim -1$ for Temperature

What about other second-order effects?

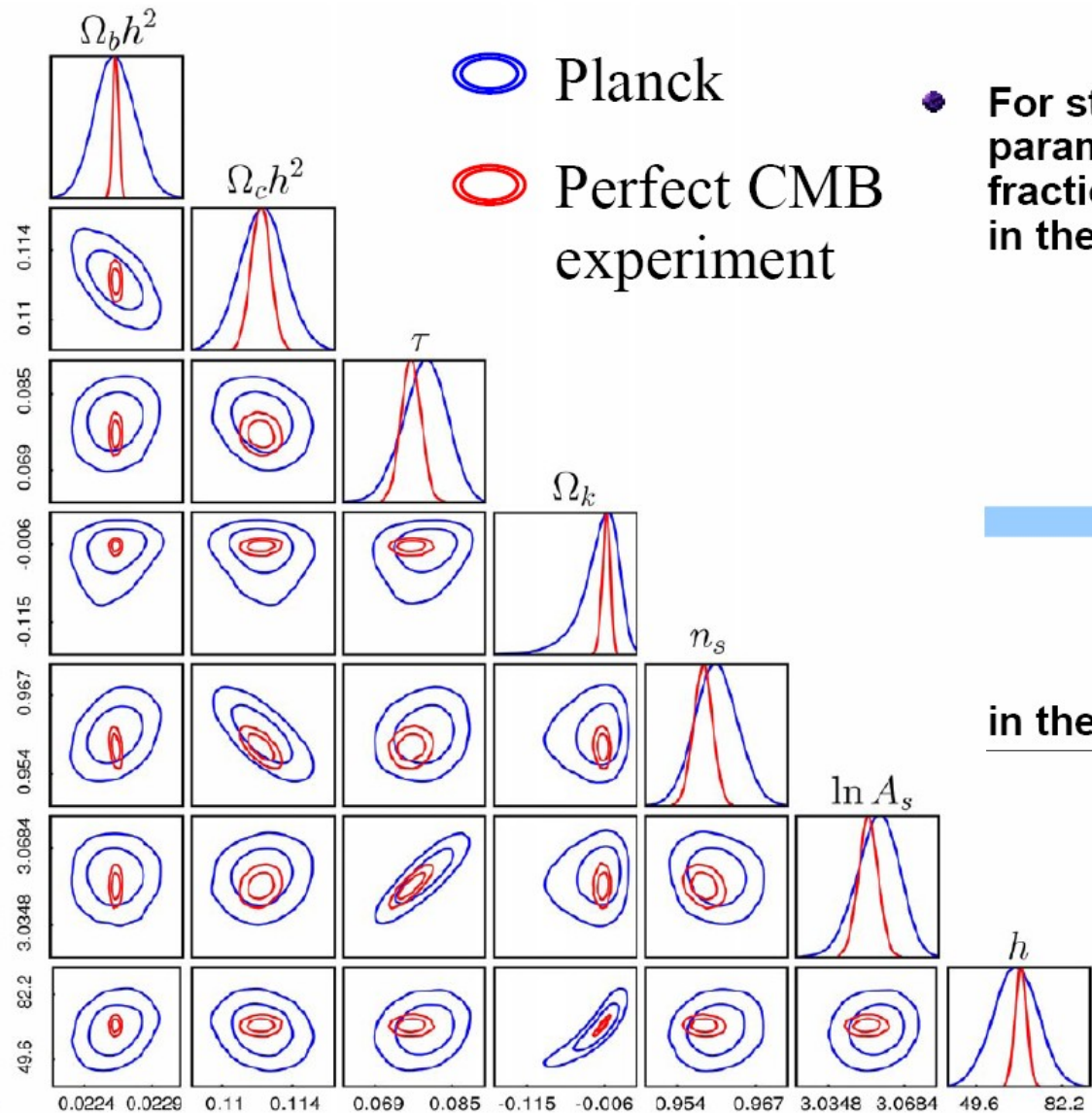
- Pitrou ,Uzan Bernadeau 2010: full second order calculation gives $f_{\text{NL}} \sim 5$ with Gaussian primordial fluctuations
- This would mean non-Gaussianity cannot be ignored in analysis of future CMB experiments ***even if the primordial perturbations are Gaussian***



The Gaussian Universe is dead!

Long live the *almost* Gaussian Universe!




The end of the line for cosmological parameters



 Planck
 Perfect CMB experiment

• For standard cosmological parameters Planck will extract a large fraction of the information contained in the cosmic microwave background!



$$\frac{\sigma_{Planck}}{\sigma_{Perfect}} = O(1)$$

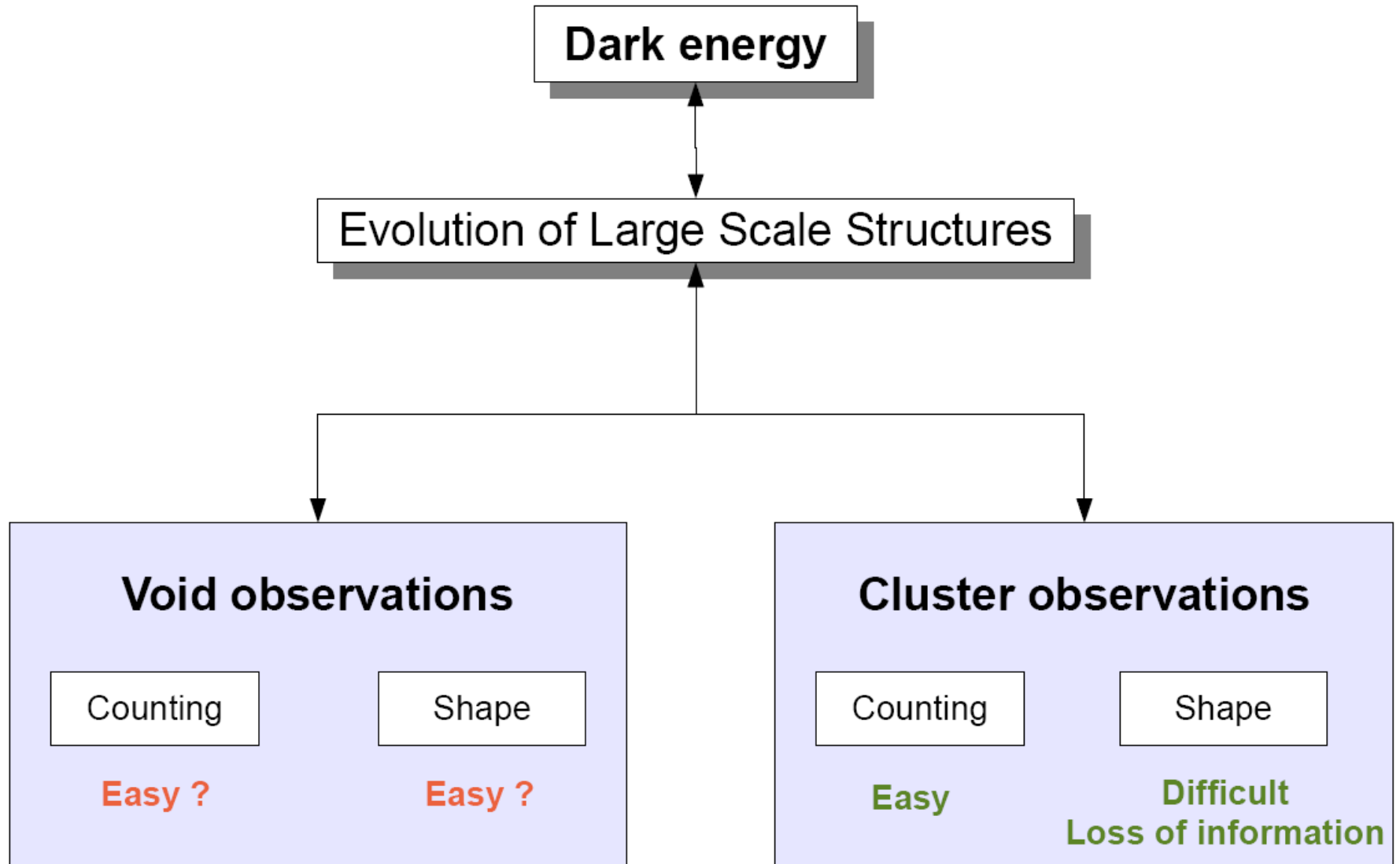
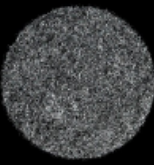
in the standard cosmological model.

The non-Gaussian revolution

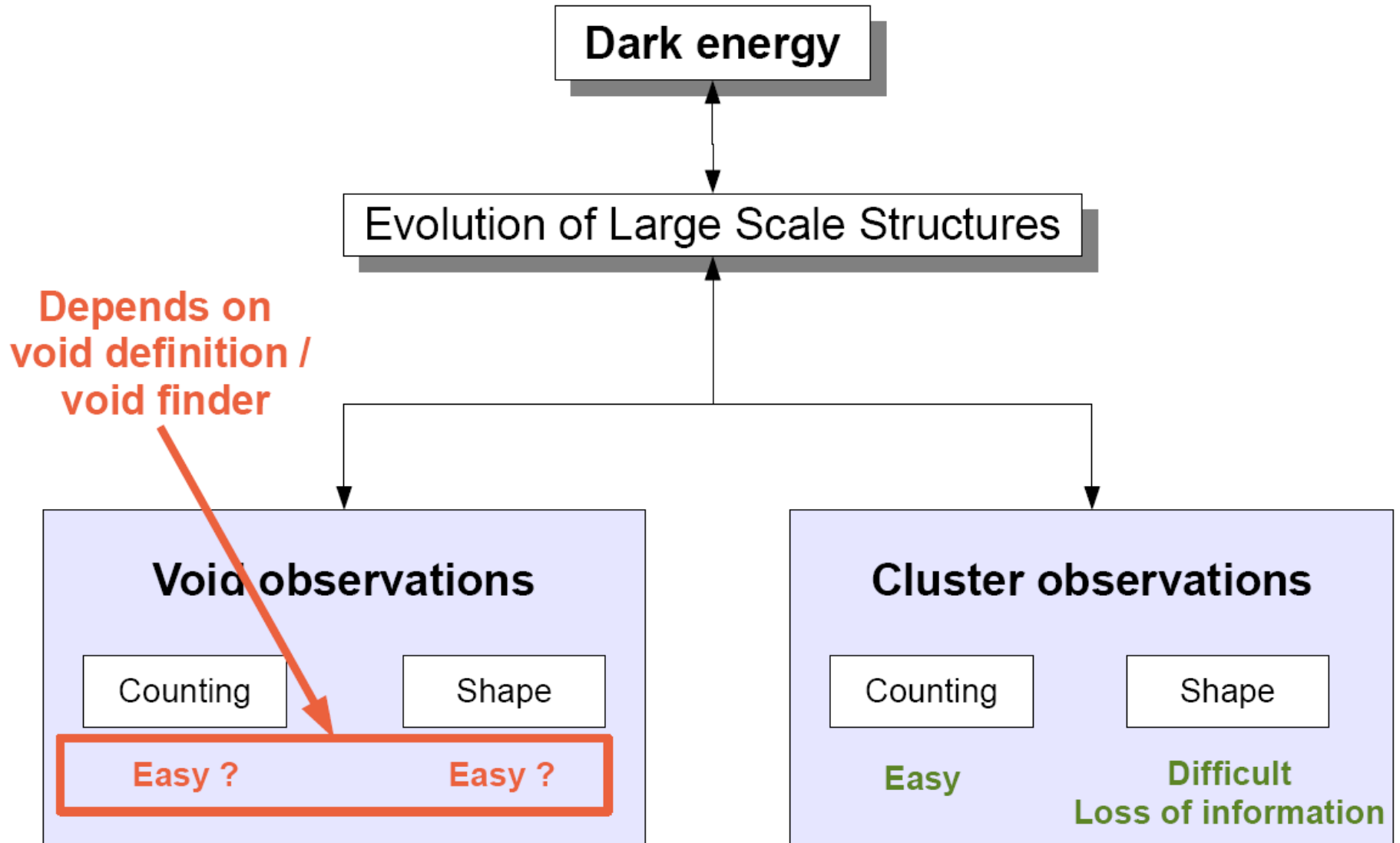
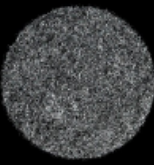
- The coming decade will be the era of extraction of information from non-Gaussian sources
 - probe of primordial non-Gaussianity
 - secondary anisotropies (lensing)
 - high precision Large Scale Structure analysis
 - dark energy
 - primordial non-Gaussianity
- This will require new ways of connecting theory with observations
- Will conclude by mentioning a few projects that have clear applications in this direction

Identification and characterization of cosmic voids

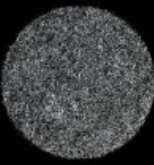
Why look at voids ?



Why look at voids ?

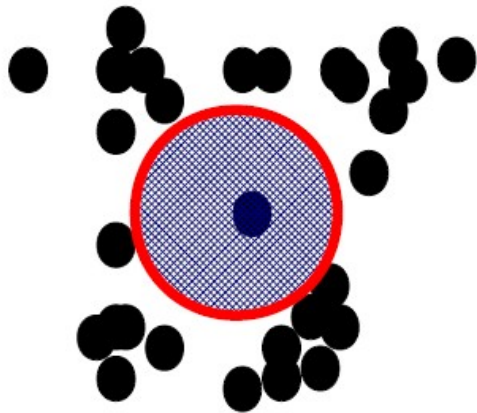


Several definition of voids

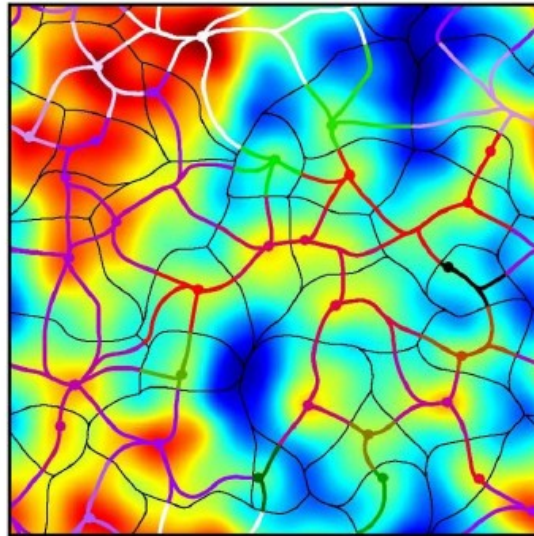


What is a void ?

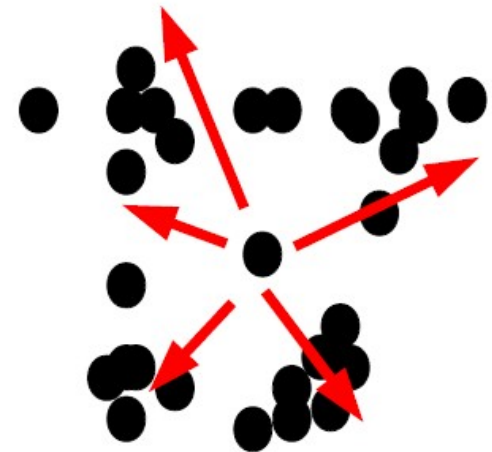
Holes in a distribution
of galaxy



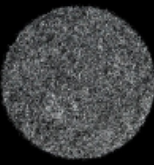
Dip in the
matter density field



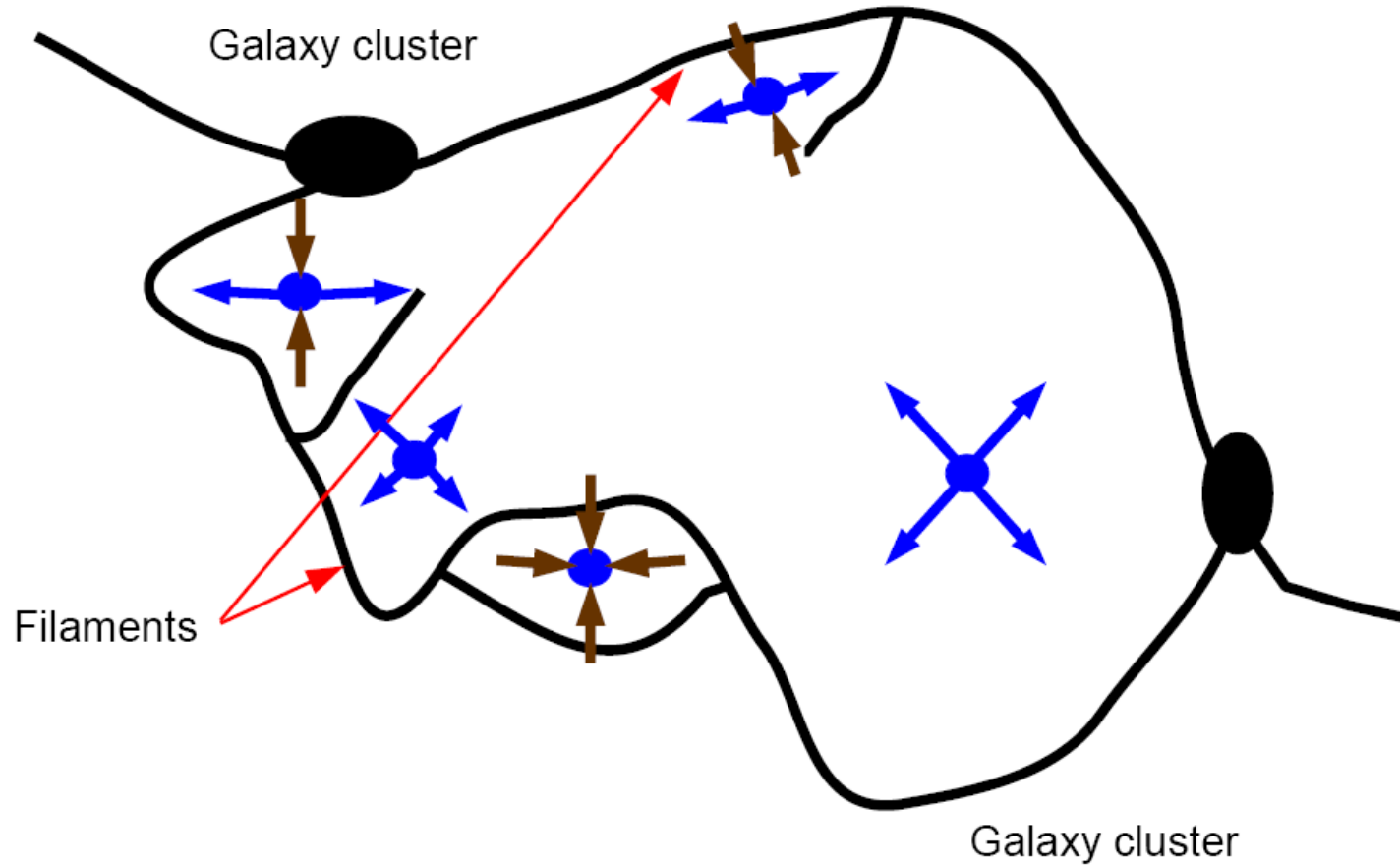
Unstable/expanding
patch of matter



A dynamical definition of voids



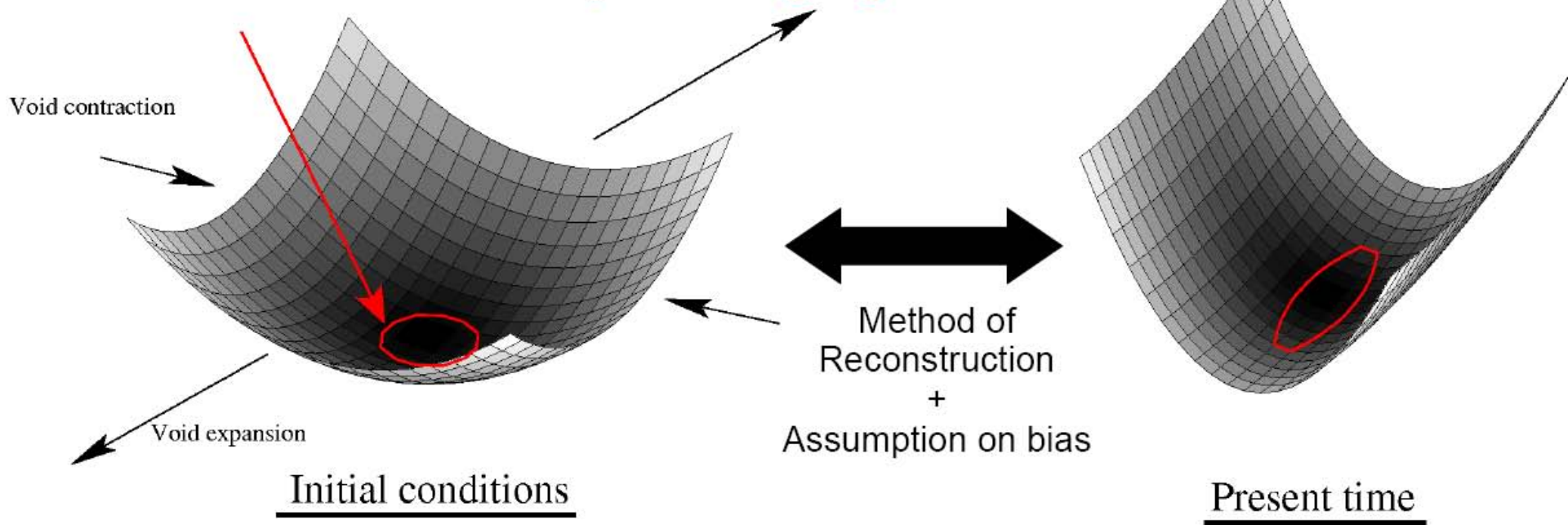
Voids in structures



A dynamical definition of voids



Void center = minima in the primordial density field
= "source" of velocity field in Lagrangian coordinates



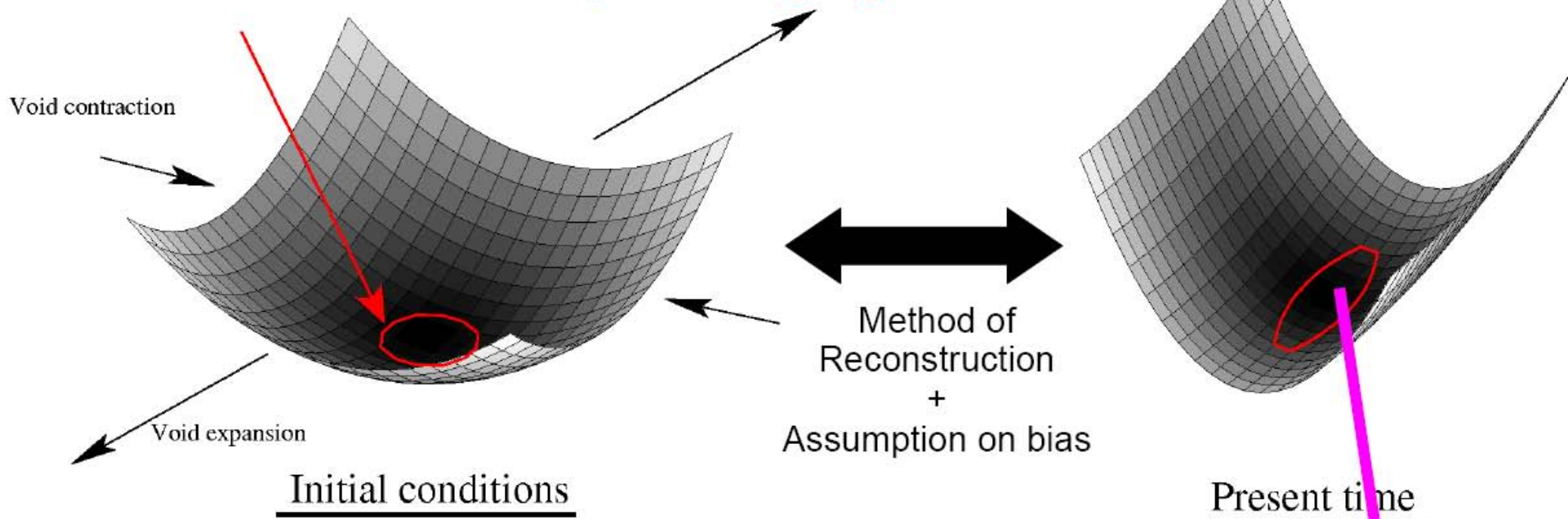
How many ?

~ 0.05 by $(10 \text{ Mpc}/h)^3$
or $\sim 9,000$ voids } in SDSS $z \leq 0.2$

A dynamical definition of voids



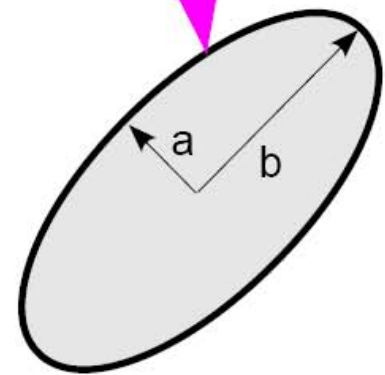
Void center = minima in the primordial density field
= "source" of velocity field in Lagrangian coordinates

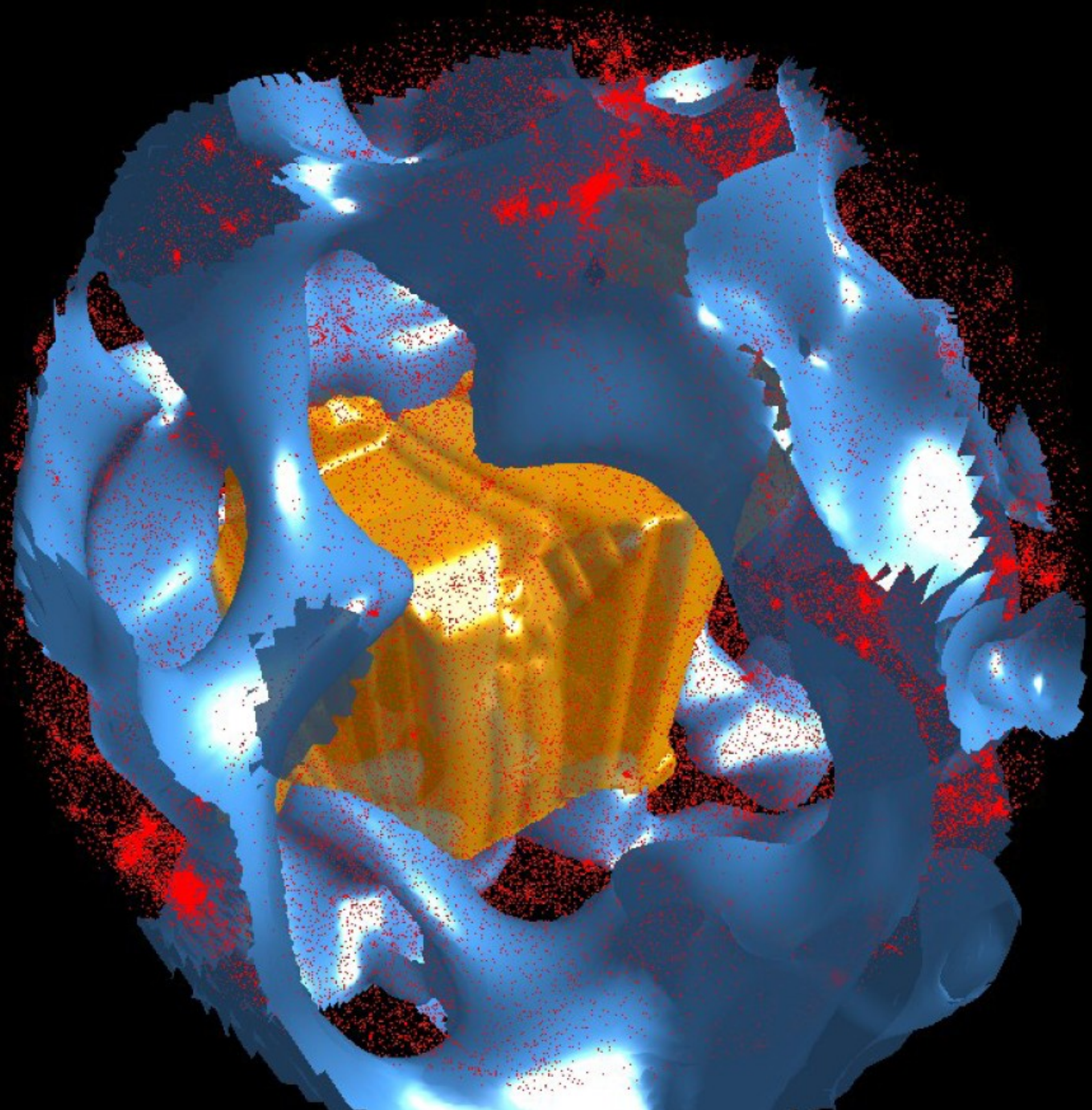


How many ?

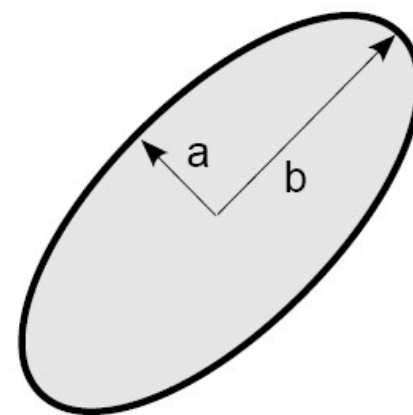
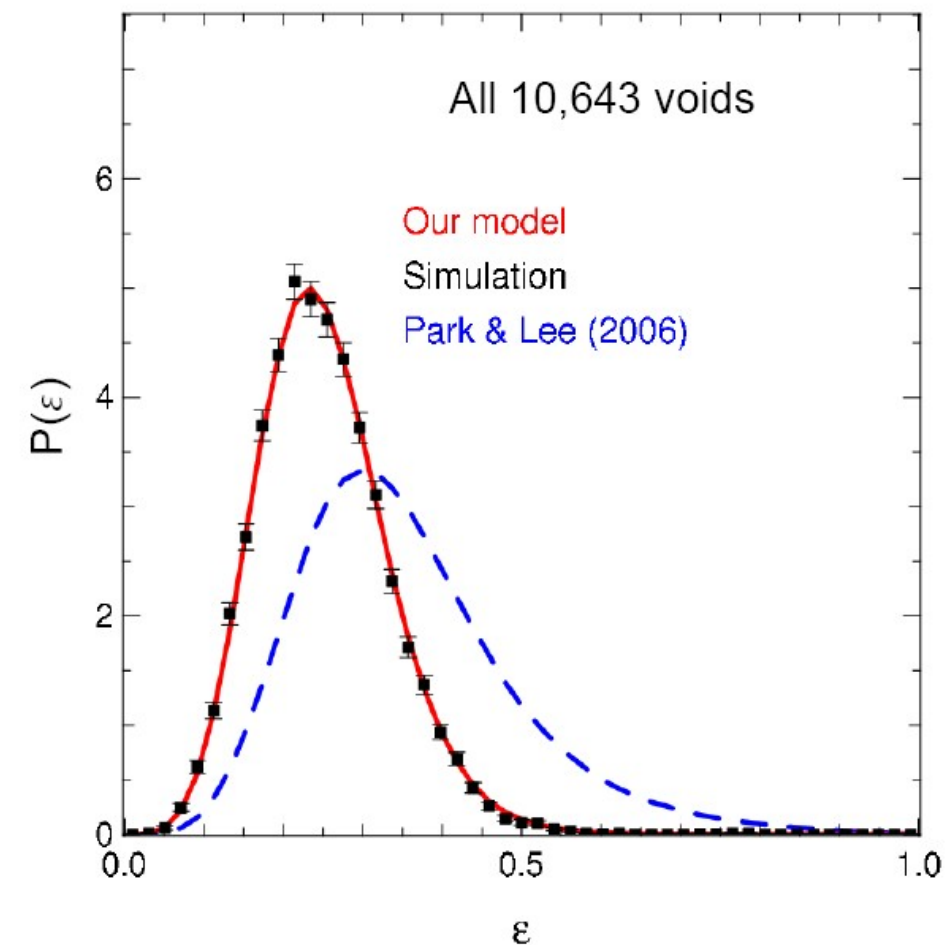
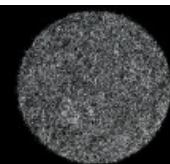
~ 0.05 by $(10 \text{ Mpc}/h)^3$
or $\sim 9,000$ voids } in SDSS $z \leq 0.2$

$$\varepsilon = 1 - \sqrt{\frac{a}{b}}$$





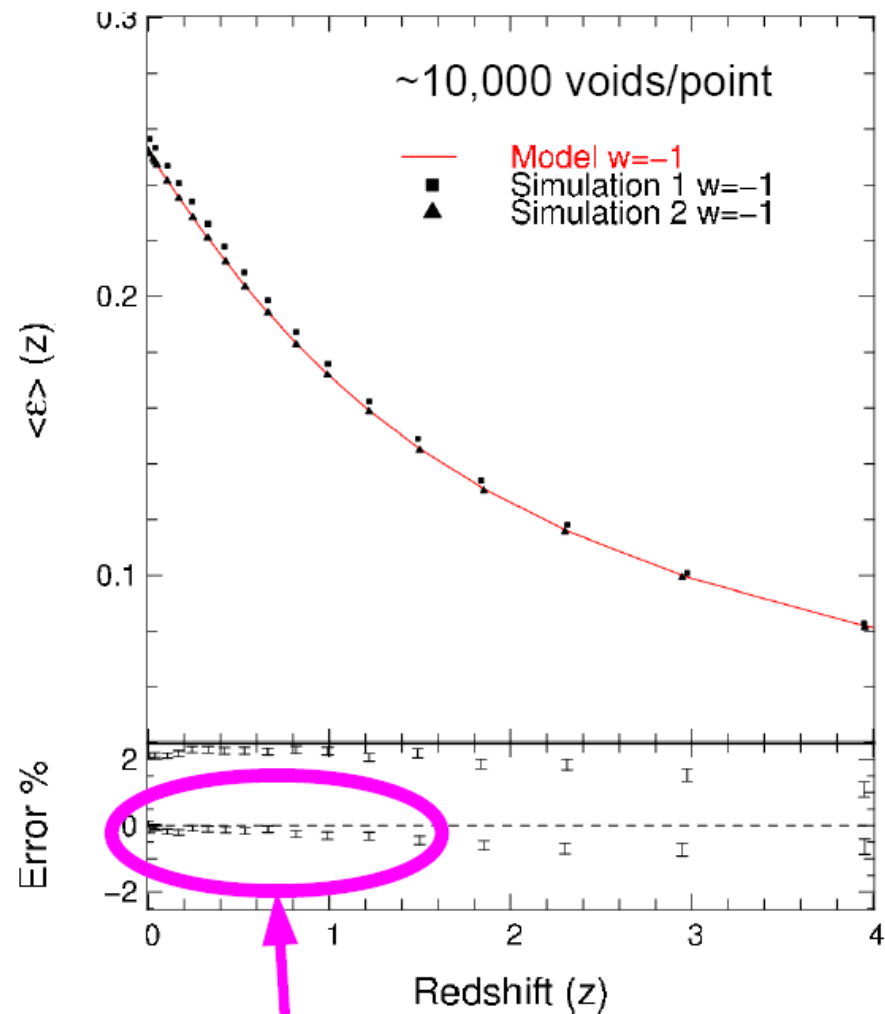
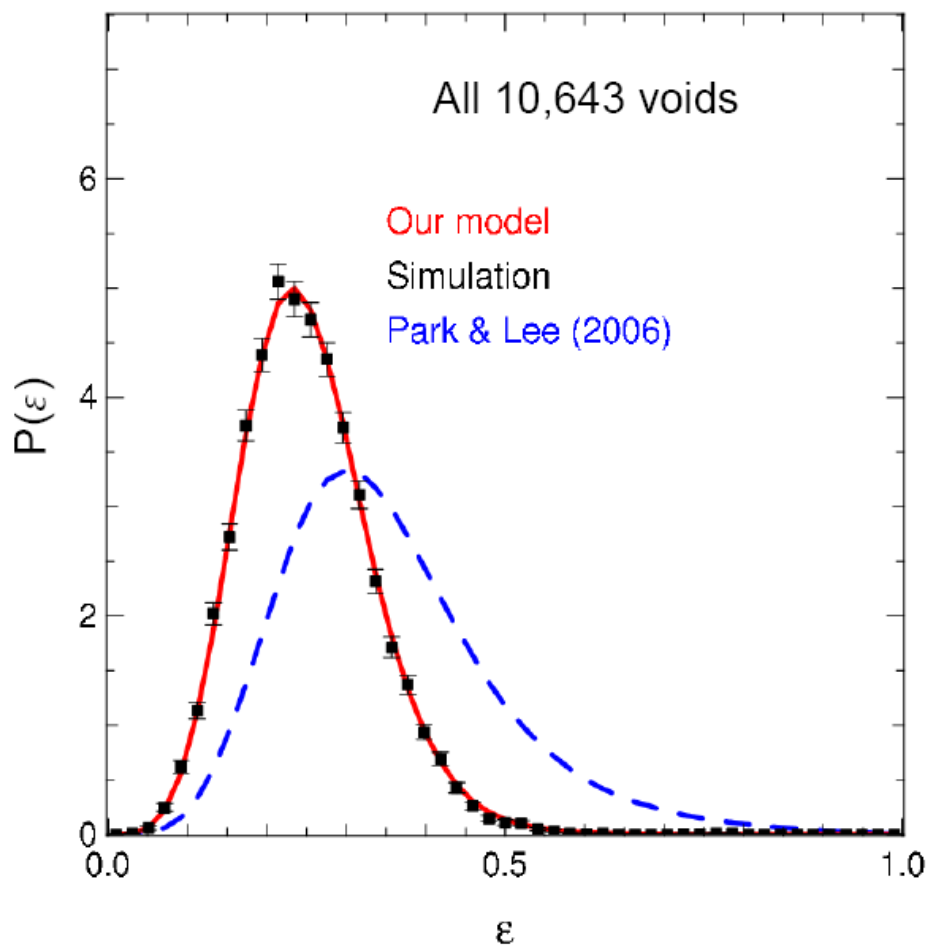
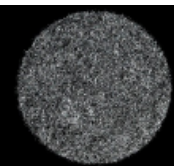
Simulation vs Theory



$$\varepsilon = 1 - \sqrt{\frac{a}{b}}$$

Simulation of $(500 \text{ Mpc}/h)^3$
lagrangian smoothing $4 \text{ Mpc}/h$

Simulation vs Theory

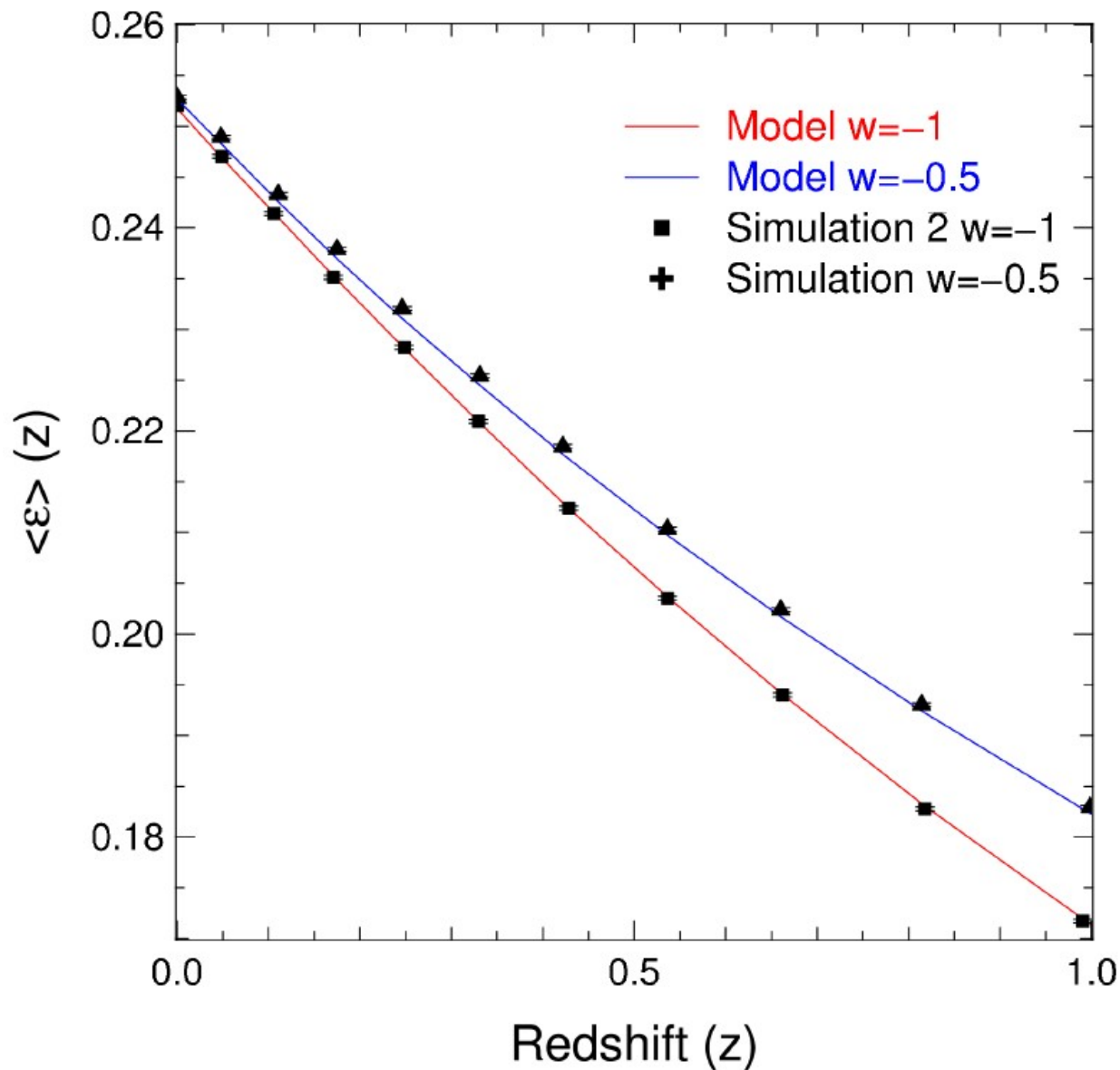
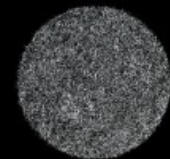


$\sim 0.1\%$ error

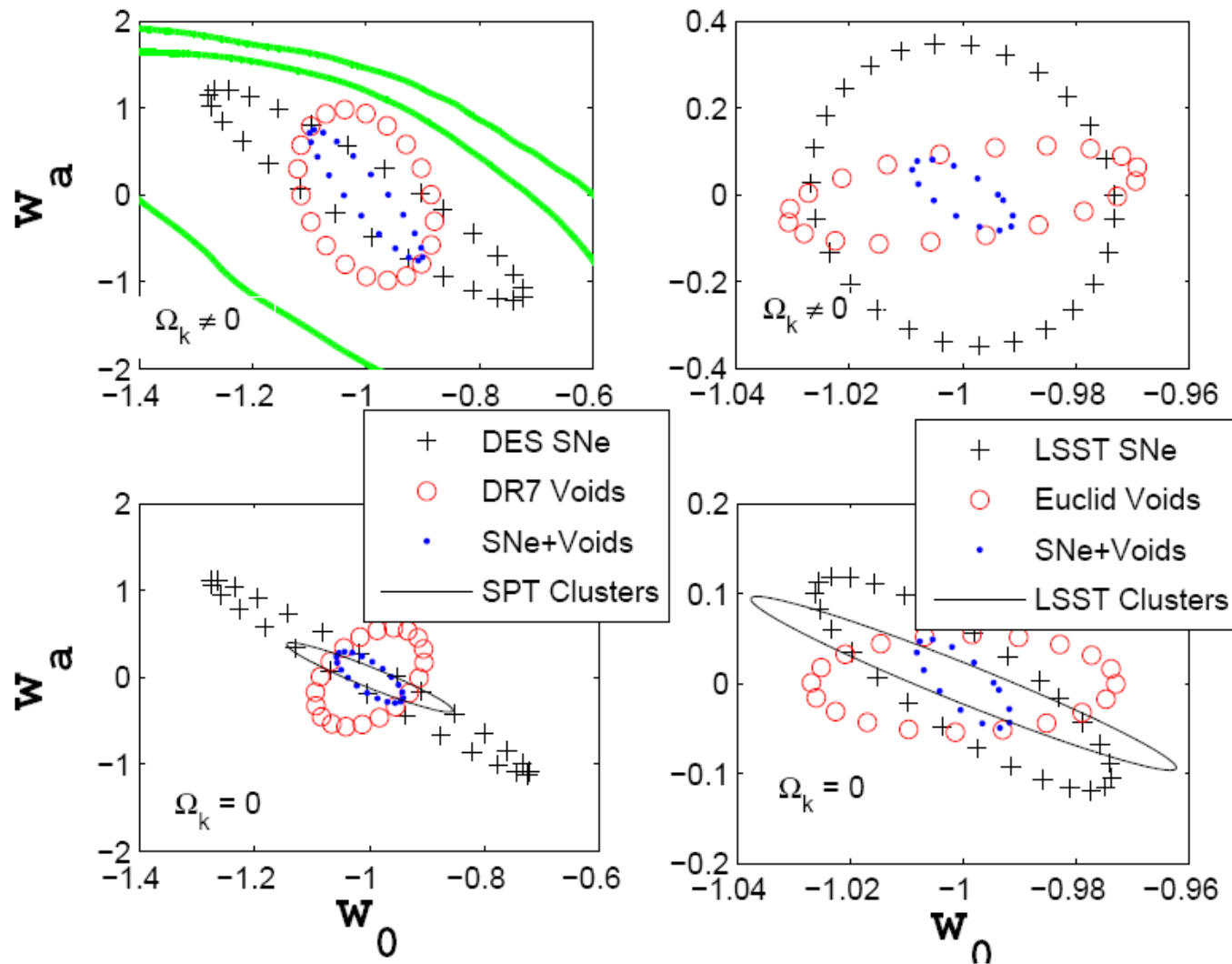
Lavaux & Wandelt (2009, MNRAS)

Simulation of $(500 \text{ Mpc}/h)^3$
lagrangian smoothing $4 \text{ Mpc}/h$

Mean ellipticity for different w CDM



Voids a promising complementary probe of dark energy



APPLE: Acceleration through Parallel Precomputation and LEarning.

- Developed to enable high precision cosmological parameter estimation from Planck
- Implemented in Pico (Parameters for the impatient cosmologist) (Fendt and Wandelt 2006,8)
- Planck will produce spectra of such high accuracy that standard methods for extracting cosmological parameters will be either be
 - to inaccurate, or
 - too slow
- Allows using massively distributed computing for sequential problems

Pico

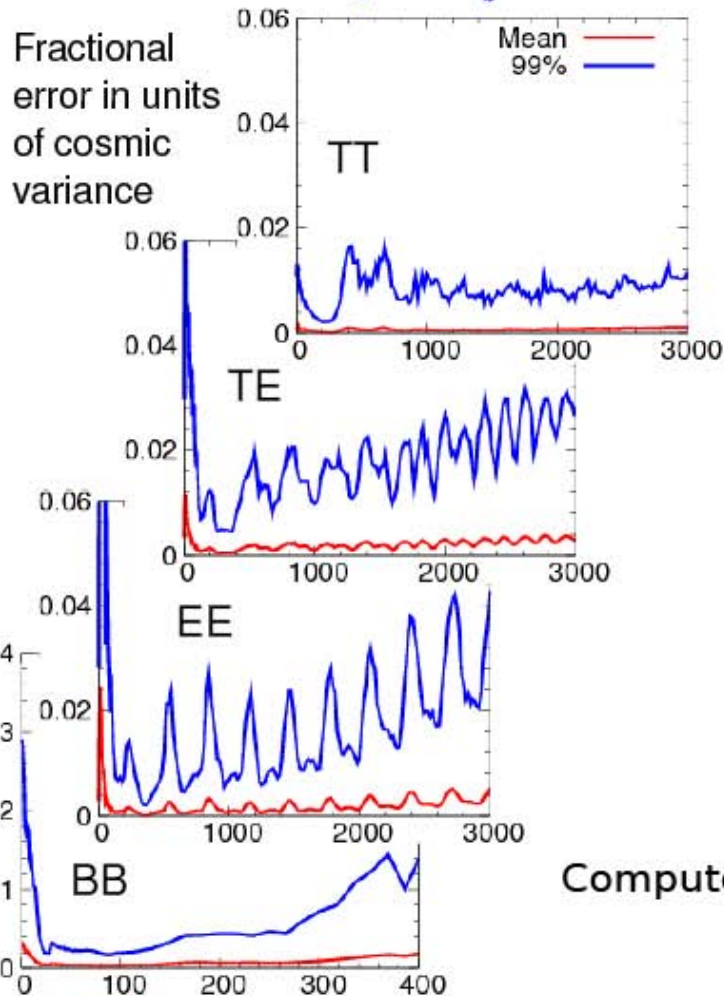
Pico performs regression on a training set of $\{\theta, C_\ell\}$

Fast: ~ 25 ms per C_ℓ

Accurate

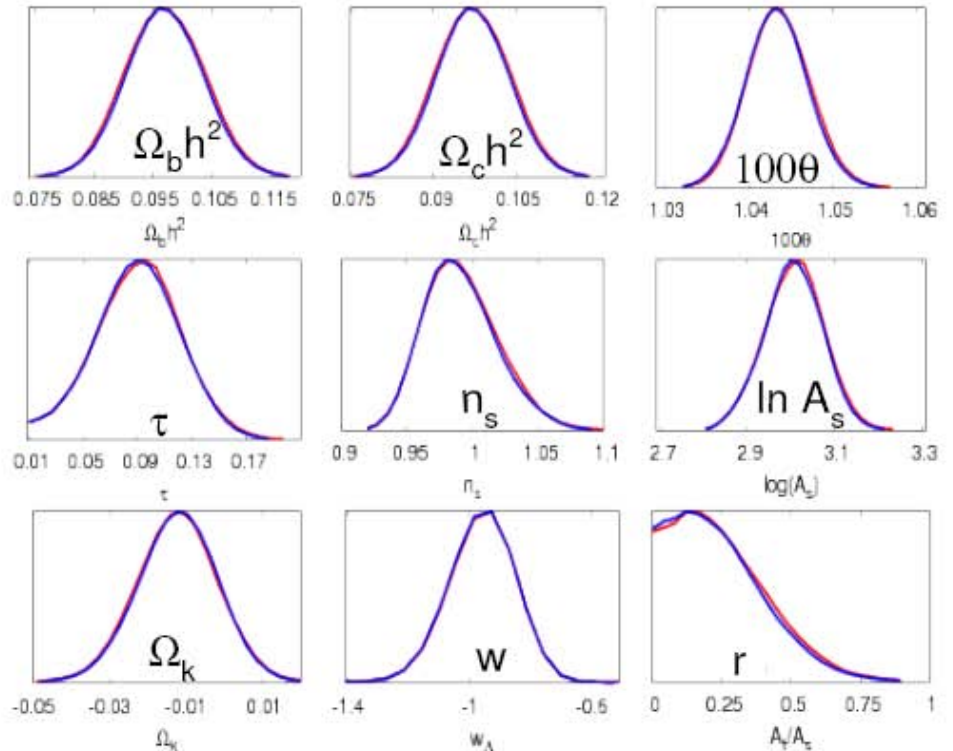
WMAP

+ SDSS Posteriors



PICO — (blue)

CAMB — (red)

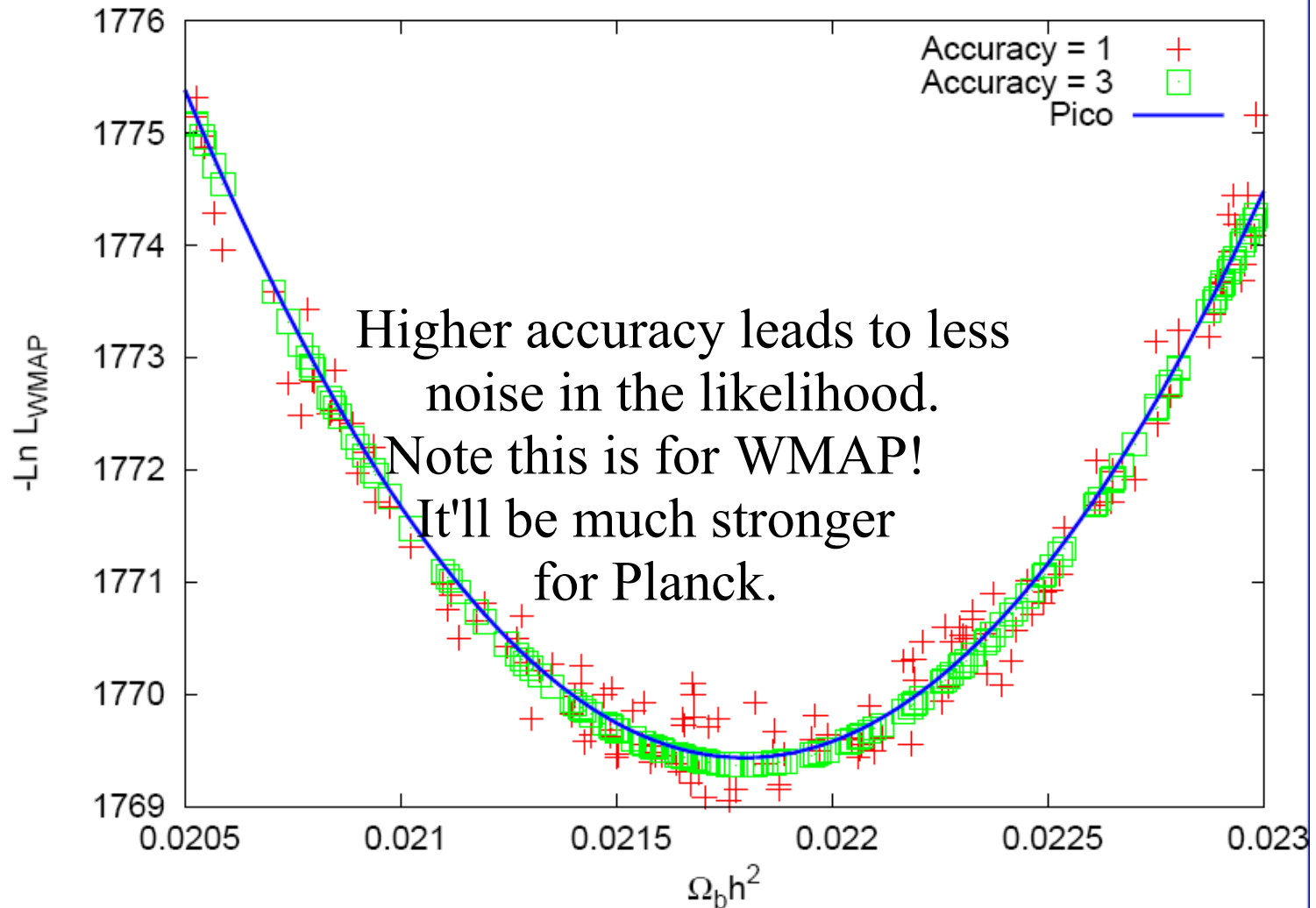


Computes scalar C_ℓ 's, tensor C_ℓ 's, matter transfer function and jacobian C_ℓ 's of w.r.t to parameters

Trained on high accuracy C_ℓ 's

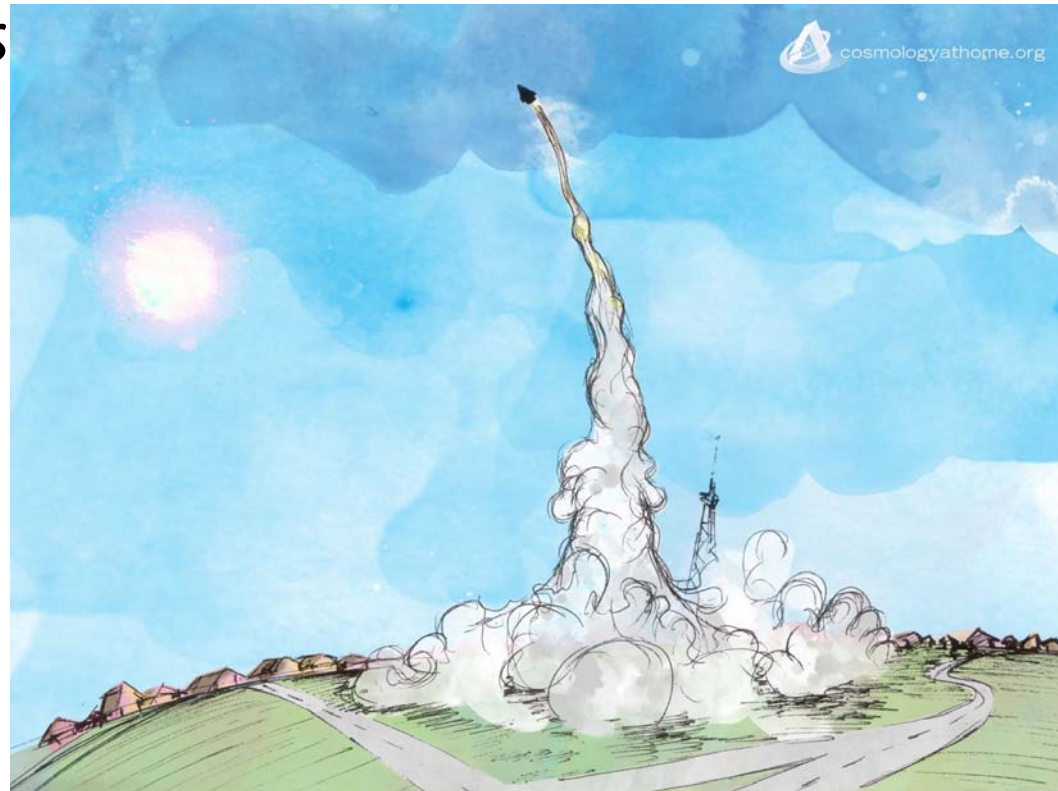
Download: cosmos.astro.uiuc.edu/pico

PICO reduces noise in the likelihood



cosmology@home

- Use BOINC platform to enable people everywhere to donate CPU time
- many 1000s of users
- 10,000s of CPUs
- can generate training sets very quickly
- turns homes into cosmology research centers worldwide



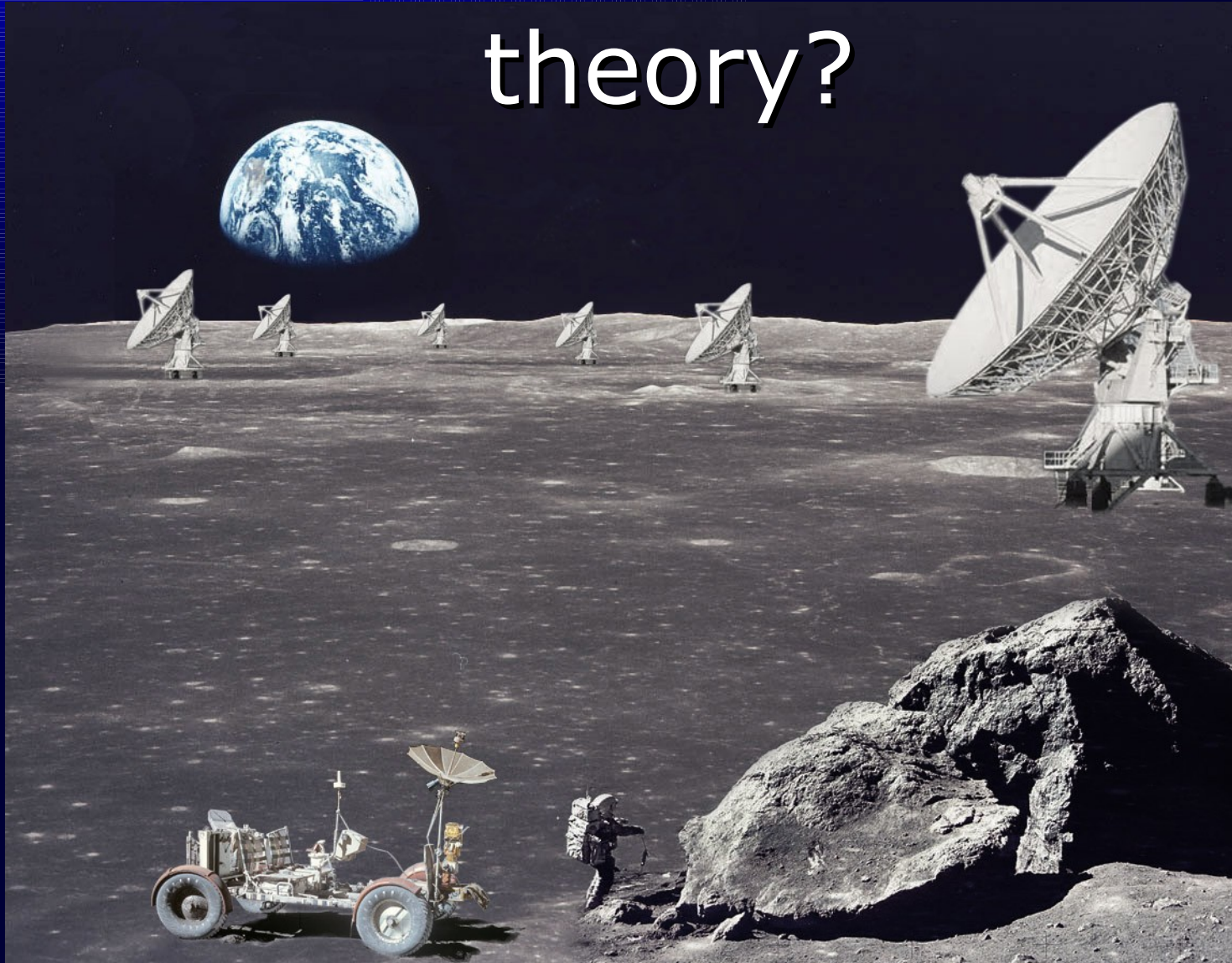
PICO application: RICO

- RICO is PICO applied to detailed cosmological recombination physics
- Reduces the main theoretical uncertainty in CMB power spectrum calculations
- Brute force Codes take days to finish for a single run.
- We were able to fit $n(z)$ with a few 100 training samples => running time is now 25ms.
- Can now be included in Boltzmann codes.

<http://cosmos.astro.uiuc.edu/rico>
[Fendt et al. 2008]

Onto the far future

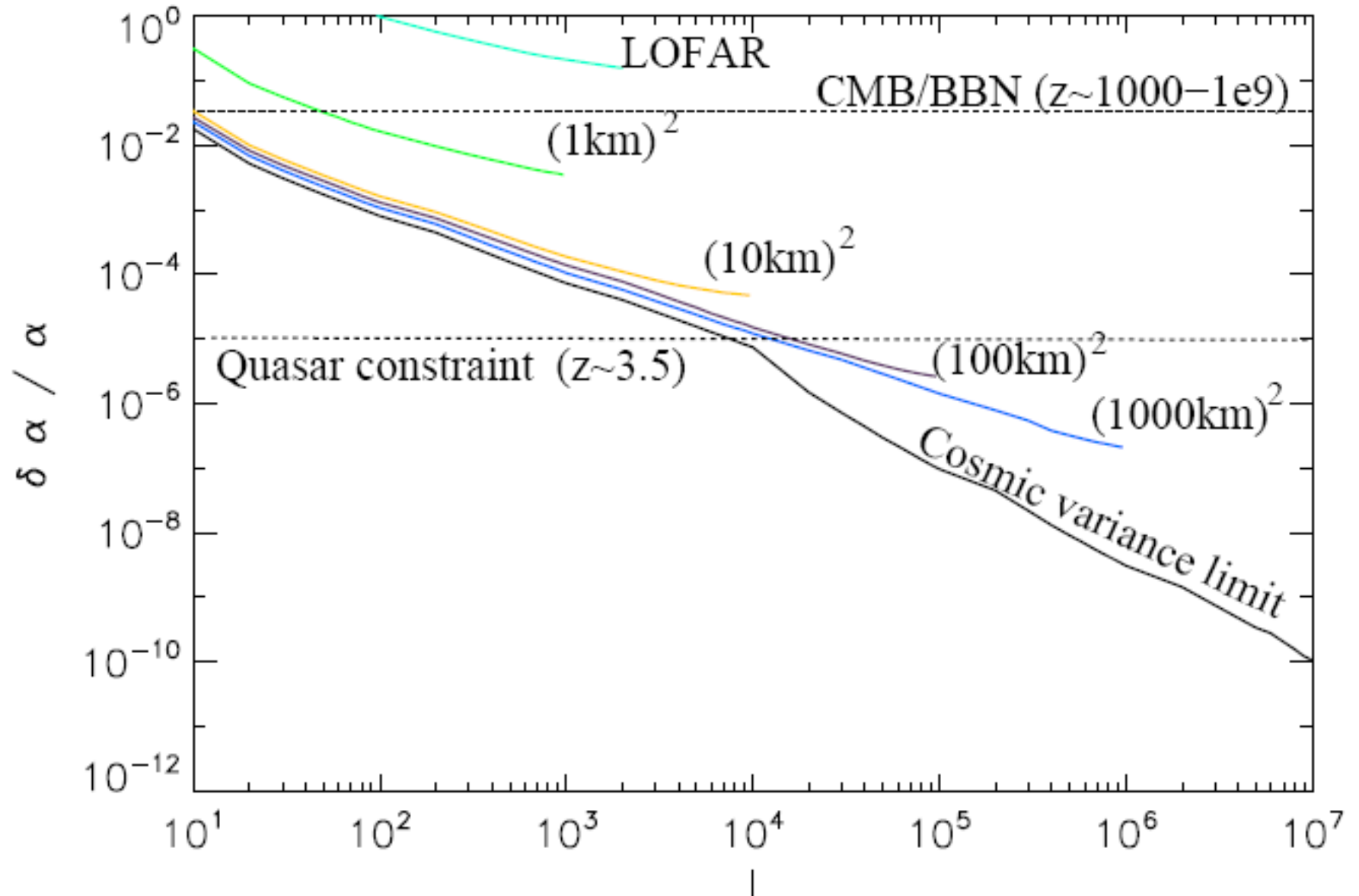
21cm observations from the Moon – tests of string theory?



Cooray 2007

Khatri and
Wandelt
2007, 2008

$\delta\alpha/\alpha$ from 21cm

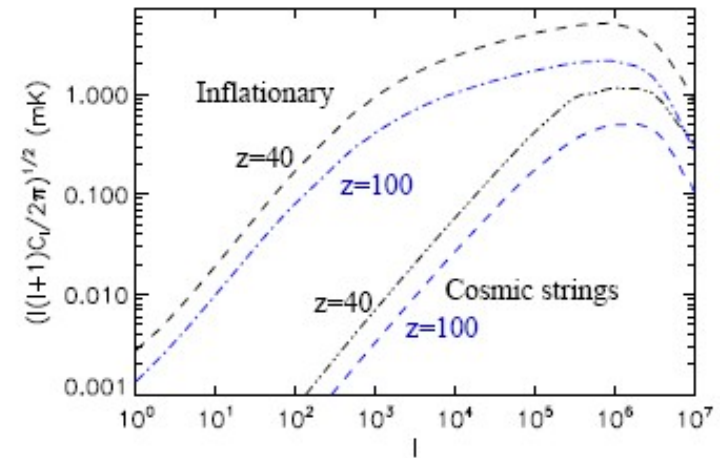


Cosmic string induced perturbations from CMBACT

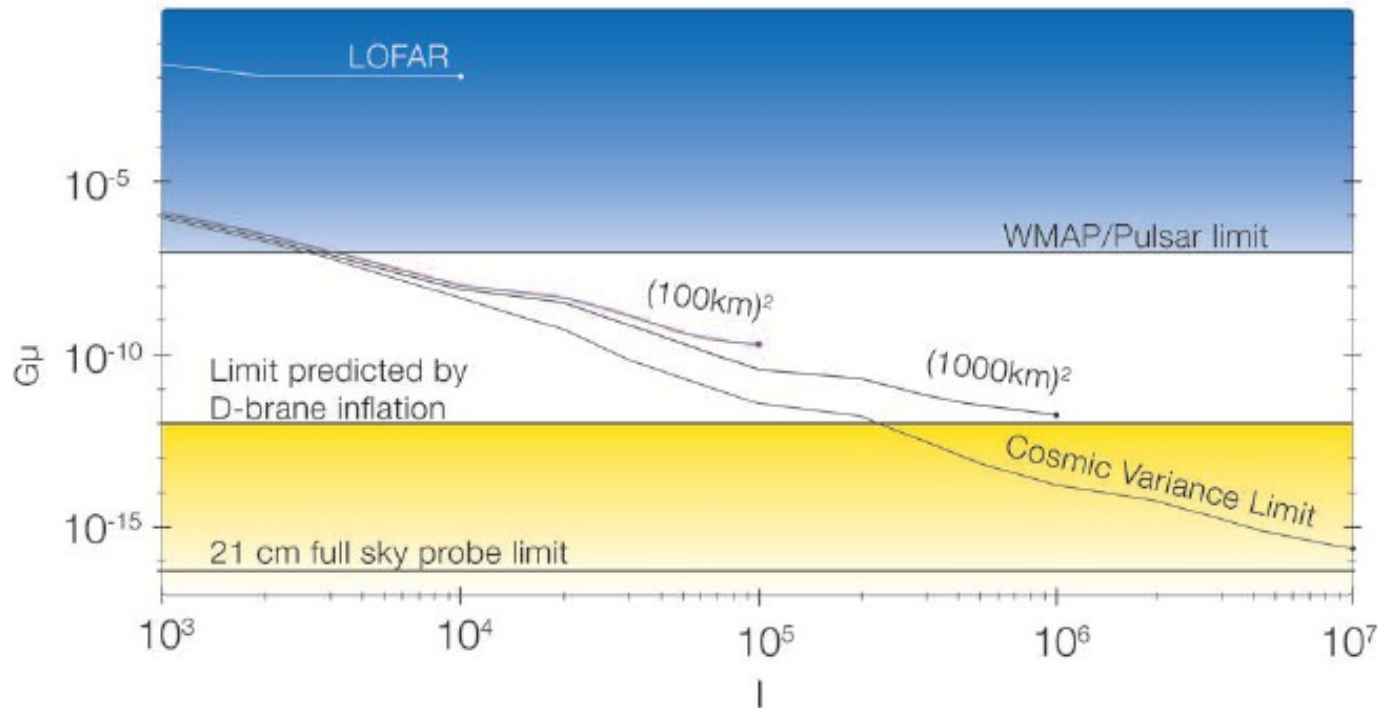
Pogosian and Vachaspati 1999

$$\mu \sim M_s^2, M_{GUT}^2$$

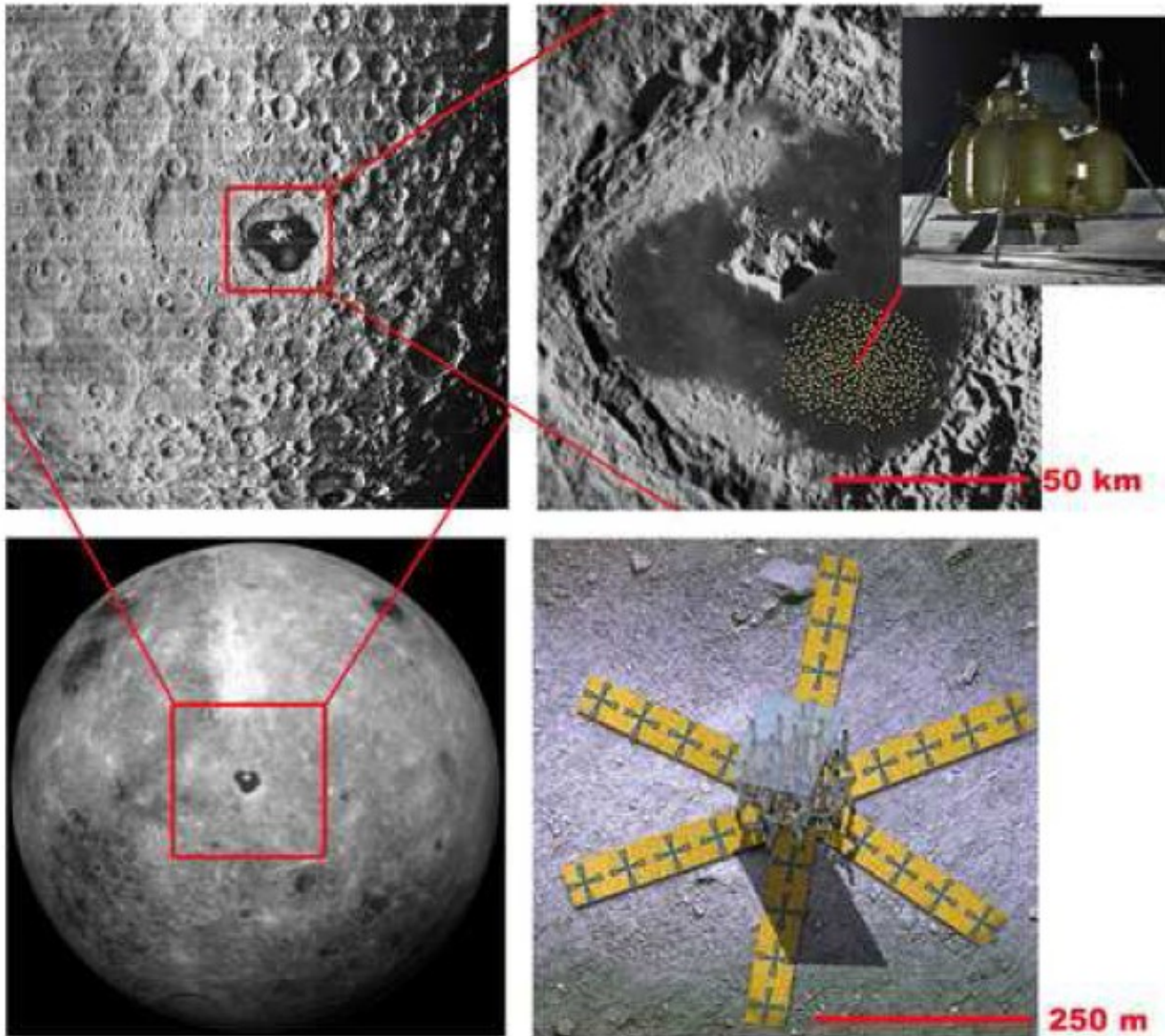
$$G\mu = 10^{-12} \Rightarrow M_s, M_{GUT} \sim 10^{13} \text{ GeV.}$$



Khatri & Wandelt 2008

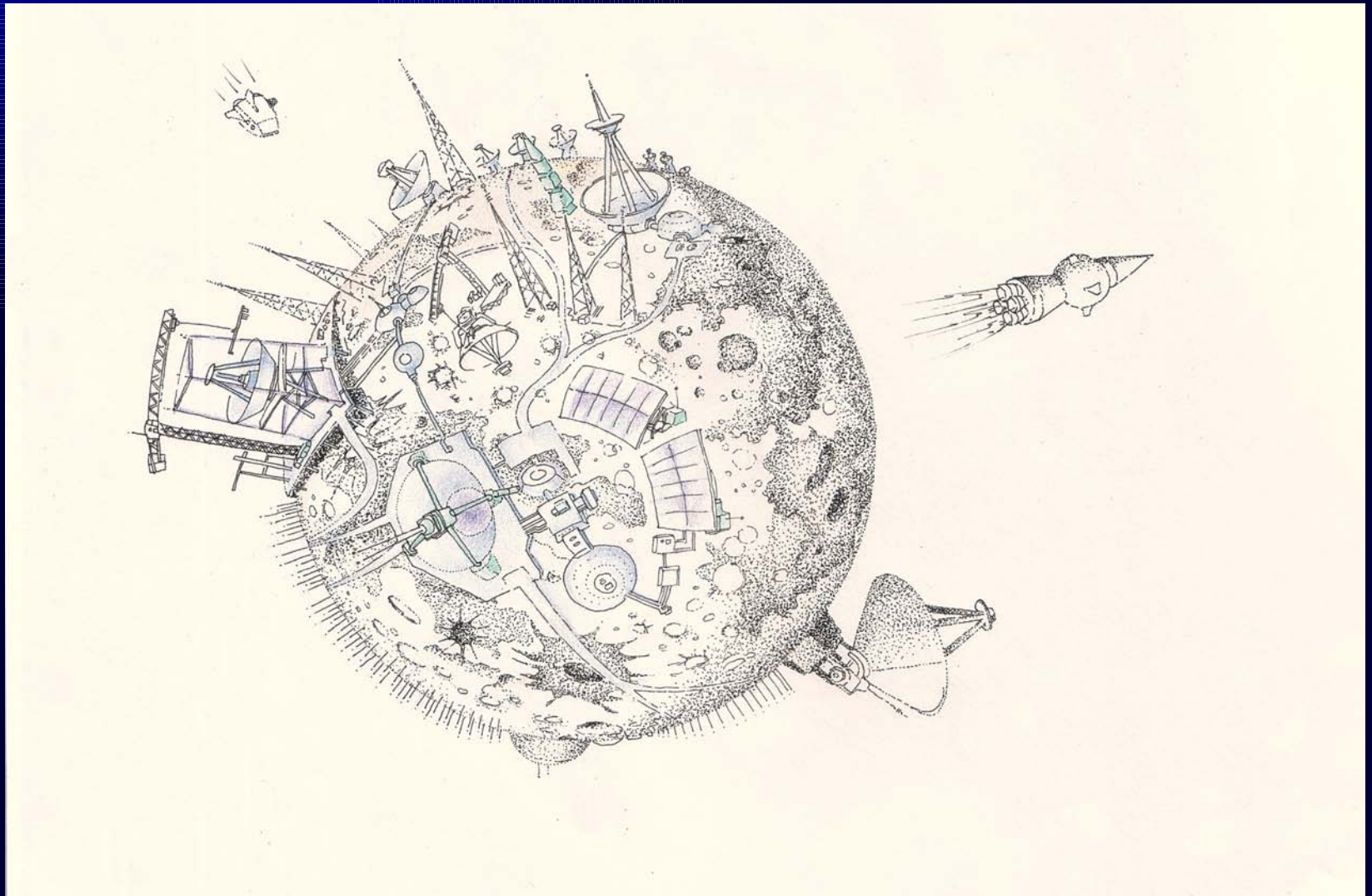


Dark Ages Lunar Interferometer



Source: Naval Research Lab

A scientific future for the Moon?



Conclusions

- The non-Gaussian revolution is here
- Non-Gaussian sources of information probe the cosmic beginning and cosmic fate
- Many opportunities for cross-checks between different primordial NG channels: E and T, large scale structure power spectrum, void morphology
- Exciting time ahead for cosmological probes of fundamental physics
- Planck is the Next Big Thing in CMB non-Gaussianity



cosmologyathome.org

TRANSFORM YOUR HOME!

COSMOLOGY@HOME



Fendt and Wandelt 2007, 2008; <http://cosmos.astro.uiuc.edu/pico>

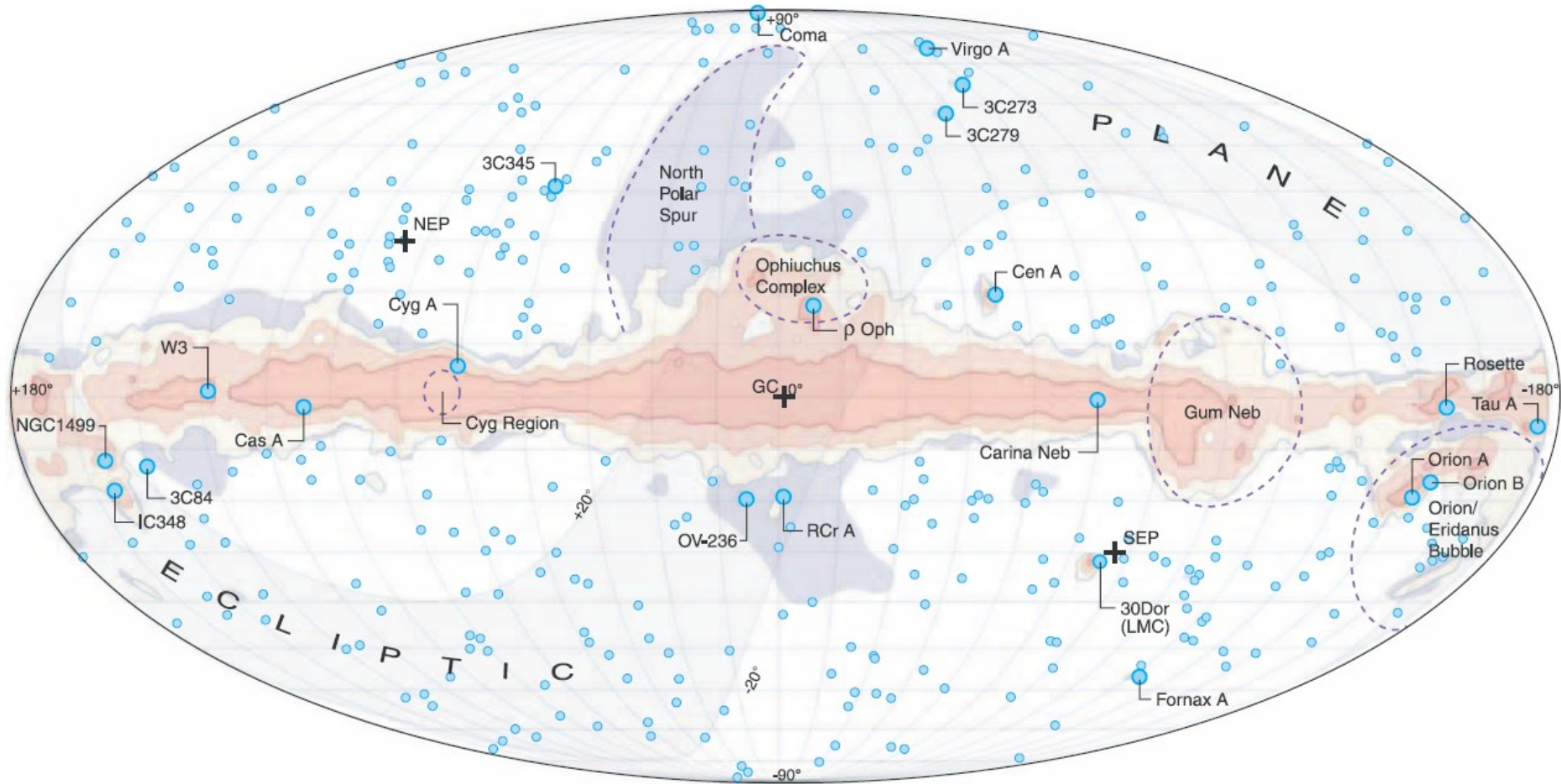


Credits

- Many thanks to my current graduate students
 - Efsandiar Alizadeh
 - Charmaine Armitage
 - Rahul Biswas
 - Chad Fendt
 - Rishi Khatri
 - Amit Yadav
 - Franz Elsner (external: MPA)
- Senior Thesis student: Scott Kruger
- Former group members (cosmos.astro.uiuc.edu)
- **Artwork: Nikita Sorokin**

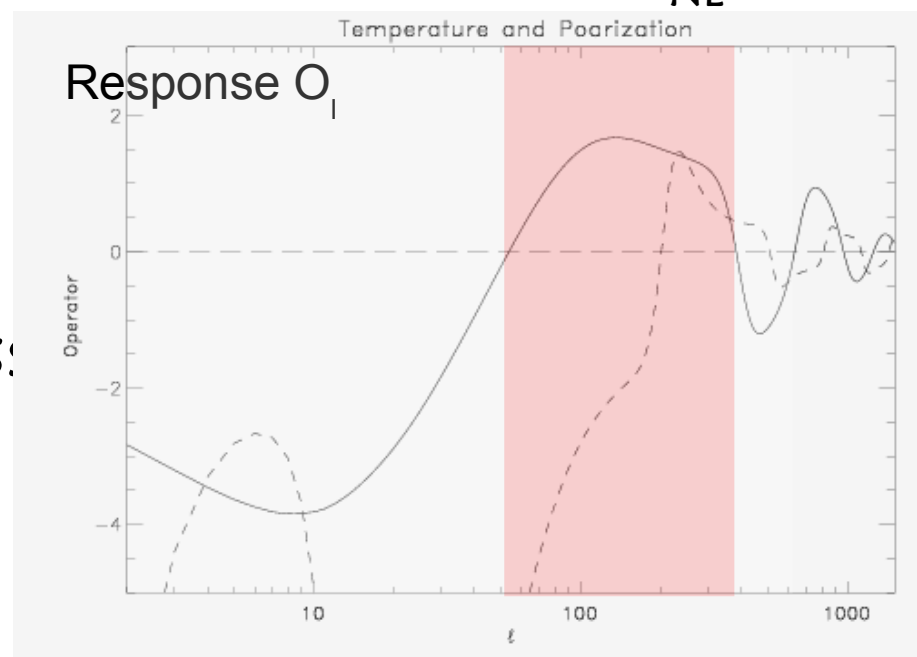
The Appendices

Supplementary slides



Foregrounds?

- Remember – large scale skewness in the Temperature map corresponds to *negative* f_{NL} .
- The added l modes at $400 < l < 550$ correspond to modes where positive skewness also gives *negative* contributions.



- At intermediate scales positive skewness gives *positive* f_{NL} .

Filter functions

$$\beta_\ell^i(r) = \frac{2b_\ell^i}{\pi} \int k^2 dk P_\phi(k) g_\ell^i(k) j_\ell(kr),$$

$$\alpha_\ell^i(r) = \frac{2b_\ell^i}{\pi} \int k^2 dk g_\ell^i(k) j_\ell(kr).$$

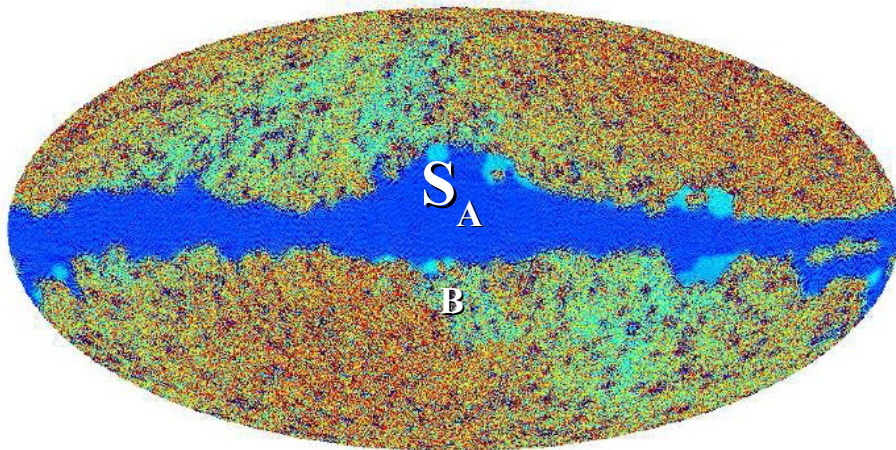
Anisotropic noise

- Linear weight maps make linear term maximally anticorrelated with the cubic term to reduce its variance due to anisotropic noise

$$S_{AB}(\hat{n}, r) \equiv \sum_{ipqr} \sum_{\ell_1 m_1 \ell_2 m_2} \beta_{\ell_1}^i(r) (C^{-1})^{ip}_{\ell_1} Y_{\ell_1 m_1}(\hat{n}) \alpha_{\ell_2}^j(r) (C^{-1})^{jq}_{\ell_2} Y_{\ell_2 m_2}(\hat{n}) \langle a_{\ell_1 m_1}^p a_{\ell_2 m_2}^q \rangle$$

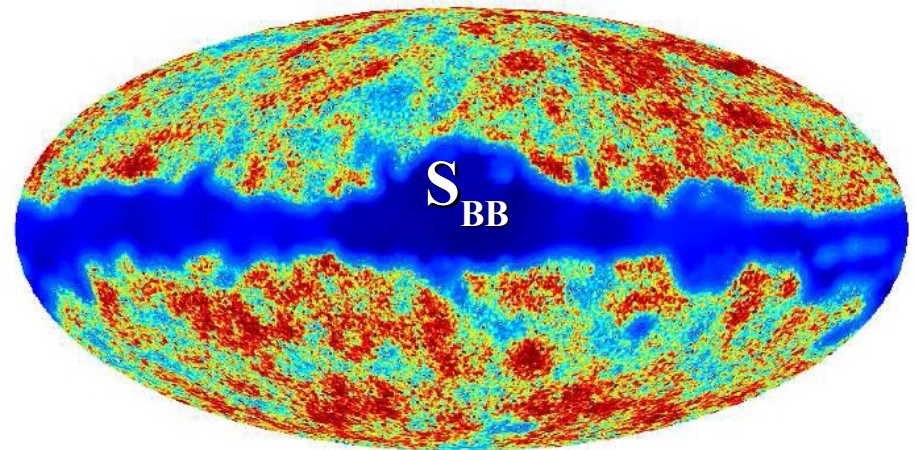
$$S_{BB}(\hat{n}, r) \equiv \sum_{ipqr} \sum_{\ell_1 m_1 \ell_2 m_2} \beta_{\ell_1}^i(r) (C^{-1})^{ip}_{\ell_1} Y_{\ell_1 m_1}(\hat{n}) \beta_{\ell_2}^j(r) (C^{-1})^{jq}_{\ell_2} Y_{\ell_2 m_2}(\hat{n}) \langle a_{\ell_1 m_1}^p a_{\ell_2 m_2}^q \rangle$$

$\langle A(r)B(r) \rangle_{\text{MC}}$



-2.3e-06  1.0e-05

$\langle B(r)B(r) \rangle_{\text{MC}}$



1.8e-10  2.0e-08

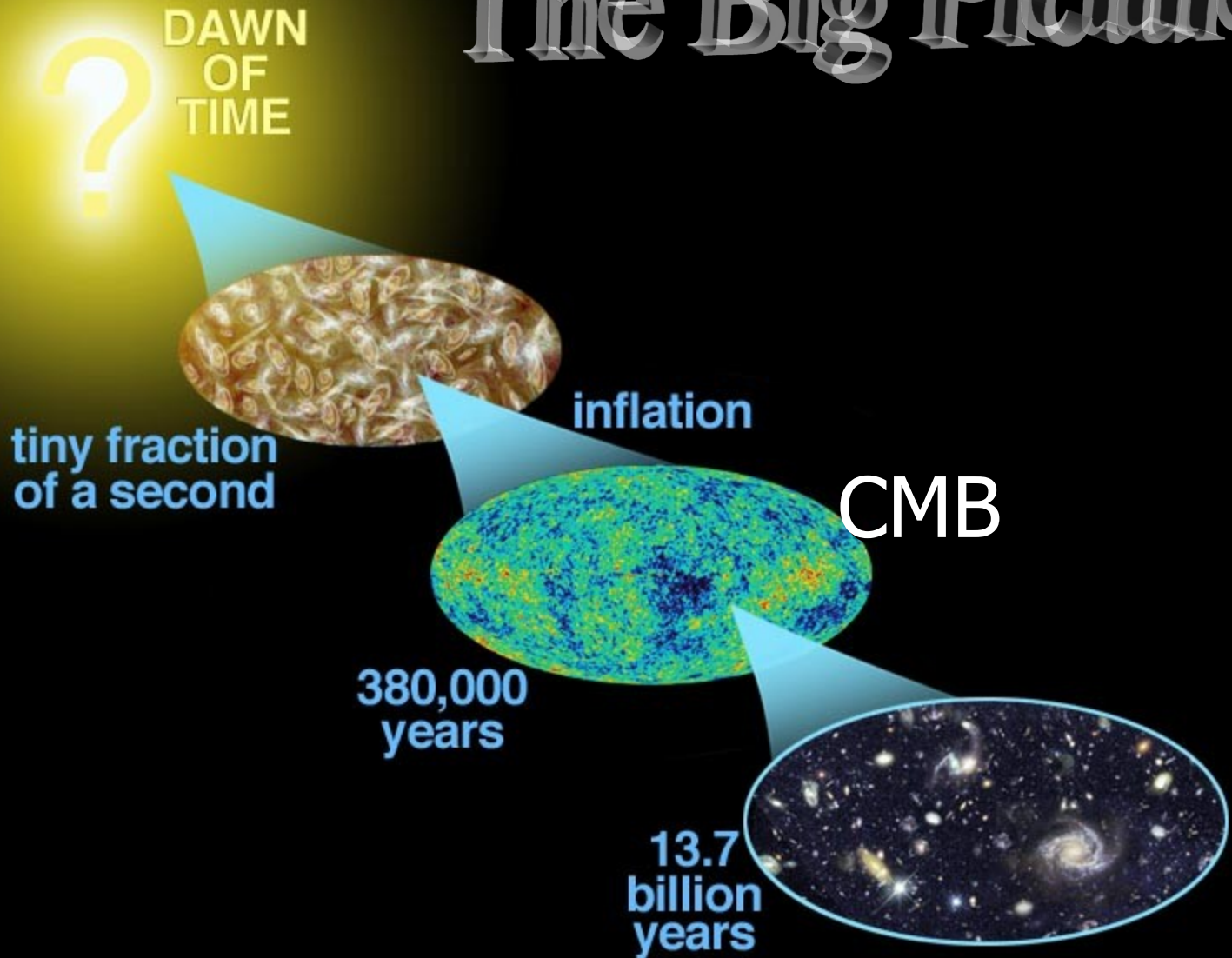
Q+V+W Channels

ℓ_{\max}	f_{NL}			
	$f_{\text{sky}} = 94.2\%$ Kp12	$f_{\text{sky}} = 84.7\%$ Kp2	$f_{\text{sky}} = 76.8\%$ Kp0	$f_{\text{sky}} = 64.3\%$ giant mask
350	-2383.67	-75.16	24.91	8.32
450	-2791.83	-79.79	55.36	65.31
550	-3135.82	-93.49	65.57	79.93
650	-3307.15	-93.7	62.91	77.02
750	-3368.26	-108.23	64.75	78.35

V+W channels

ℓ_{\max}	f_{NL}			
	$f_{\text{sky}} = 94.2\%$ Kp12	$f_{\text{sky}} = 84.7\%$ Kp2	$f_{\text{sky}} = 76.8\%$ Kp0	$f_{\text{sky}} = 64.3\%$ giant mask
350	-3145.22	-26.68	34.62	19.24
450	-1425.06	-15.63	67.94	64.69
550	-1509.92	-13.09	79.99	83.53
650	-1559.91	-22.43	79.18	81.29
750	-1575.11	-22.81	86.81	86.52

The Big Picture



Testing the Inflationary Paradigm

- Probes of inflation:
 - Inflation generates primordial fluctuations in space-time
 - Fluctuations in radiation
 - Cosmic Microwave Background Temperature anisotropies
 - CMB E-polarization anisotropies
 - Fluctuations in matter
 - Dark matter distribution (Gravitational lensing etc.)
 - Galaxy and gas distribution (Redshift surveys, Lyman-alpha clouds, cosmological 21-cm radiation, etc)
 - Fluctuations in space time itself
 - Primordial Gravitational Waves (eg. Primordial B-modes of CMB)

Instrument systematics?

1) Beam asymmetries

- If the CMB is Gaussian, no asymmetry of the main beam can produce non-vanishing bispectrum.
- If there are large side-lobes that spread foreground around the sky they will produce large scale features – unlikely to affect the high l regime. Further, we do not see evidence for frequency dependence.

Instrument systematics? II: WMAP Noise

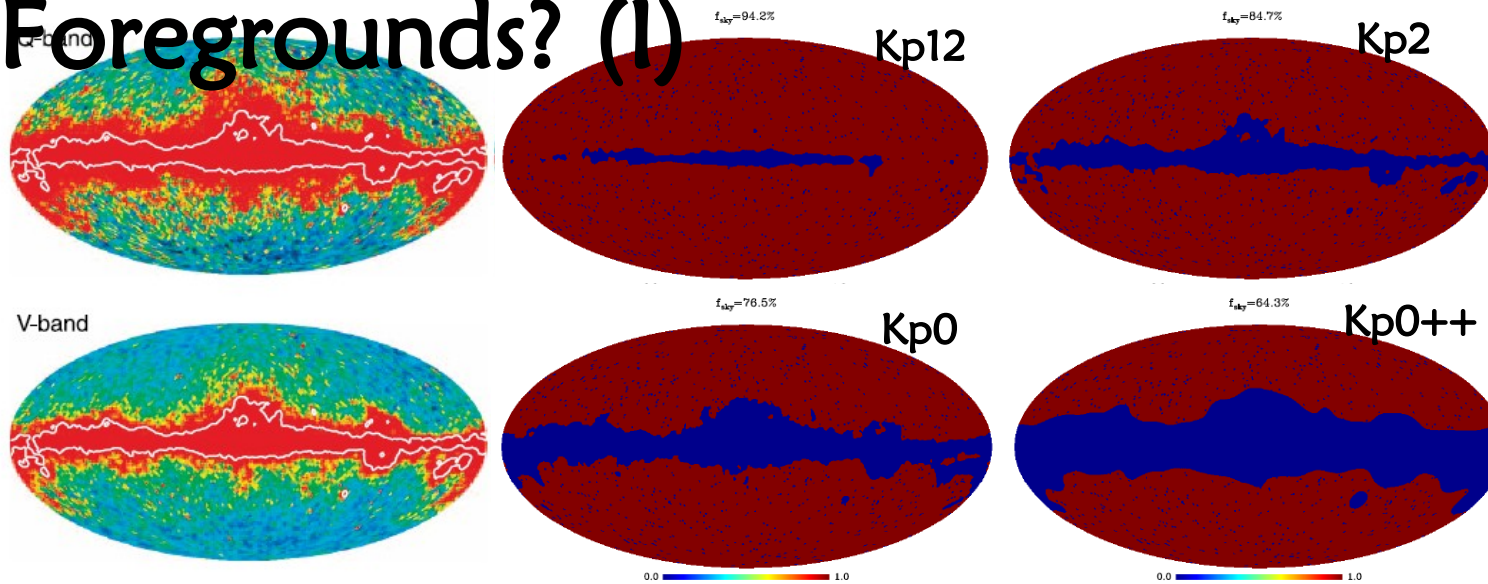
- Noise correlations (striping)
 - As long as noise is Gaussian, **no** noise correlations will produce a bispectrum.

- Non-Gaussian noise?

Analyzed differences of WMAP yearly maps

- year1-year2 $f_{NL}=1.1$ (+/- ~ 60 at 95% C.L.)
 - year2-year3 $f_{NL}=1.8$
 - year1-year3 $f_{NL}=-3.4$
- So to explain our results an instrumental systematic has to be 1) non-Gaussian, 2) the same in individual years and 3) mimic the specific bispectrum signature of f_{NL} .

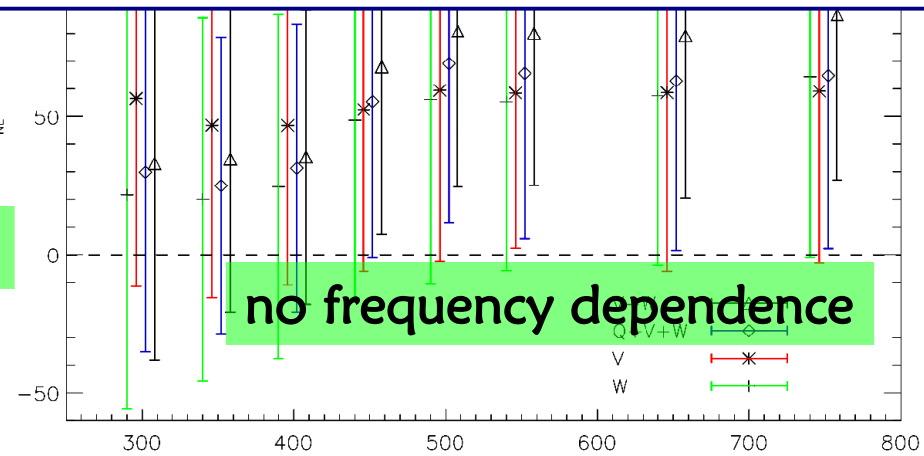
Foregrounds? (I)



We test the impact of foregrounds as a function of frequency and as a function of mask. V and W channels are the least foreground contaminated. Choice of V+W is driven by foreground considerations. Analysis on *raw* maps to avoid FG oversubtraction.

ℓ_{\max}	$f_{\text{sky}} = 94.2\%$		$f_{\text{sky}} = 84.7\%$	
	Kp12	Kp2	Kp0	Kp0++
350	-3145.22	-26.68	34.62	19.24
450	-1425.06	-15.63	67.94	64.69
550	-1509.92	-13.09	79.99	83.53
650	-1559.91	-22.43	88.21	86.21
750	-1575.11	-22.81	86.81	86.52

stable beyond kp0



no frequency dependence

Benjamin

Foregrounds? (II)

- WMAP raw maps vs WMAP cleaned maps
 - Foreground subtracted maps do not show negative f_{NL} behavior
 - Same level of f_{NL} , uniformly higher for FG subtracted maps
 - We quote the result from raw maps to be conservative and because the cleaned maps could contain *oversubtracted* foregrounds giving a positive bias.

Foregrounds (III)

- **Simulations of Gaussian CMB + Foregrounds + WMAP Noise**
 - negative for smaller masks
 - goes to zero by the time you reach Kp0 mask
 - is consistent with zero for masks greater than kp0

ℓ_{\max}	VW				Q	QVW			
	Kp12	Kp2	Kp0	Kp0+	Kp0	Kp12	Kp2	Kp0	Kp0+
350	-1290	-27	35	19	1	-2384	-75	25	8
450	-1425	-16	68	65	-6	-2792	-80	55	65
550	-1510	-13	80	84	-11	-3136	-94	66	80
650	-1560	-22	79	81	-14	-3307	-94	63	77
750	-1575	-23	87	87	-20	-3368	-108	65	78
750*	$-1105 \pm_{19}^{19}$	$-42 \pm_5^5$	$-6 \pm_4^4$	$-0.3 \pm_4^4$				$-13 \pm_5^5$	$1 \pm_6^6$

Secondary Anisotropies?

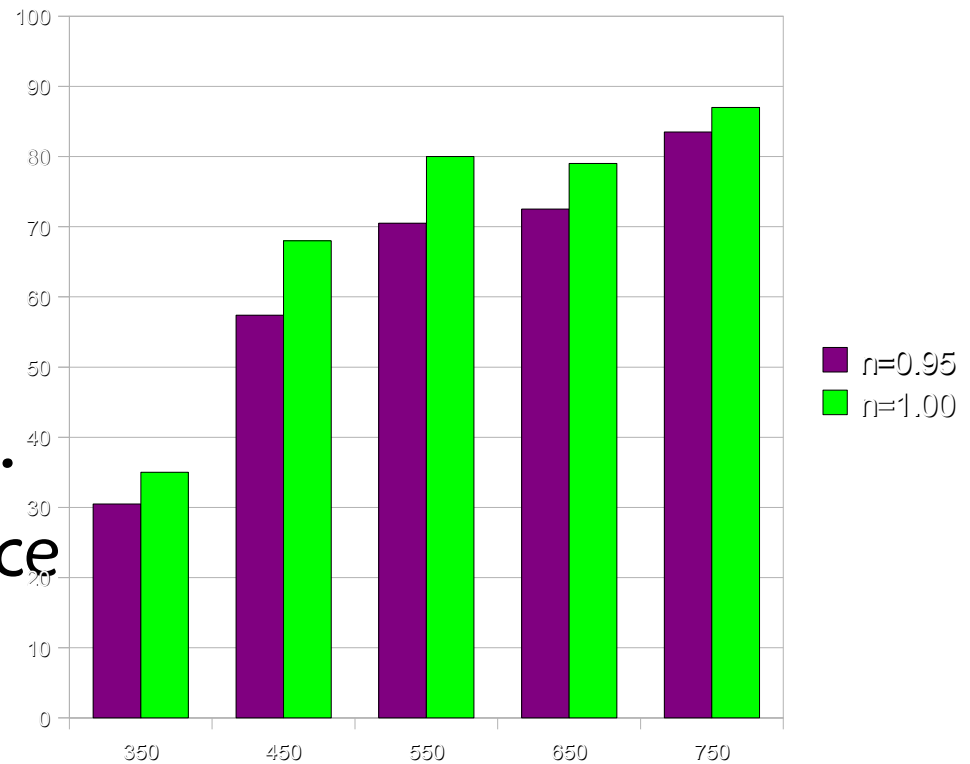
- Point sources, including SZ
 - Orthogonal overlap with primordial bispectrum. Bias of $|f_{NL}| < 1$. SZ and point sources have opposite signs.
- Serra and Cooray (arxiv:0801.3276)
 - dominant secondary confusion level to WMAP bispectrum arises from
 - ISW-lensing bispectrum (positive bias)
 - SZ-lensing bispectrum (negative bias)
 - If $f_{NL} = 20$ effective bias around 10%. **Negligible** for $f_{NL} > 20$, because effects add in quadrature.

Re-discovery of another non-Gaussian signal?

- Larson/Wandelt (hot and cold spots not hot or cold enough):
 - at smaller angular scales **X**
 - symmetric-> no odd correlation. Probably noise model.
- The Cold Spot (Vielva et al. 2004) is localized in the map and covers a particular range in scale. **X**
Preliminary result: $f_{NL} = 94 \pm 60$ (95% C.L.)
- Large Scale anomaly? Can check by removing large scale signal. Preliminary result: **X**
Removing $l < 21$, $f_{NL} = 135 \pm 96$ (95% C.L.)

Sensitivity to assumed cosmology

- The filters depend weakly on assumed cosmology. We used $n=1$.
- Choosing $n=0.95$ reduces the error bars by 10%, and reduces the central values between 5% and 15%.
- At $l_{\max}=750$, significance *increases* to just over 3 sigma; at lower l_{\max} significance *decreases slightly*.



Noise fluctuation?

- Possible.
- It's a 2.5-3 sigma result. $P \leq 0.01$

2.5 sigma for conservative increase of error bar for possible systematics

The most aggressive interpretation of the data would be a 3.3 sigma effect (correcting for negative foreground bias and using best fit WMAP parameters)

Summary and Conclusions

- $\Delta f_{NL} \sim 30$ for all of WMAP 3 using YKWLHM07 and WMAP best fit parameters (statistical)
- First bispectrum-based analysis of the full WMAP3 data
- First significant departure of f_{NL} from 0 at $>99\%$ C.L.
- Estimators tested against Gaussian and non-Gaussian simulations with and without inhomogeneous noise
- If any bias, it is likely to be negative. Guess of systematic error bar: $-0/+5$
- 2.5-2.8 sigma, depending on choices and assumptions

Conclusion

We wrote:

“If our result holds up to scrutiny and the statistical weight of future data [...] we conclude that single field slow roll inflation is disfavored by the WMAP data.”

WMAP 5-year analysis

- Komatsu et al. 2008
- Somewhat more conservative analysis:
 - mask shape that enhances the statistical error compared to the 3-yr mask;
 - stop at $l_{\max} = 500$
 - subtract very generous estimate of point source bias.

- Quoted result: $f_{\text{NL}}^{\text{local}} = 51 \pm 60$ (95%)

- Significance: 1.7 sigma

- 2.3 sigma for analysis closer to ours

- Differences understood \Rightarrow Consistent with our

WMAP 5 year constraint on f^{equil}

$$-151 < f_{\text{NL}}^{\text{equil}} < 253$$

- Of interest for DBI inflation, ghost condensation

WMAP 5 year continued...

- A *very preliminary* result by Kendrick Smith et al., obtained at the Perimeter Workshop 4 days ago:

$$f_{\text{NL}}^{\text{local}} = 21 \pm 44 \text{ (95\%)}$$

- Note that this uses the exact same data as the WMAP 5, so the difference is entirely due to different weighting in the estimator.
 - Smaller error bar due to optimal weighting
 - This remains to be checked and the differences remain to be understood.